

## Chapter 5

# Computational Results

This chapter intends to show the computational results obtained during the realization of this Master Thesis.

The problem under study is composed by a several number of instances. Regardless, the basic principles of all of them are the same, their characteristics will be different from instance to instance. The different characteristics of the problem (capacity, number of available vehicles, demands on each street, service and deadheading costs associated with distinct streets and dump costs) are known for every tested instance.

This problem is composed by two distinct sets of instances. The first set, *mval* instances, contains the ones that have a fewer number of nodes (24-50) and links (43-138) which are all required. The second set, the *lpr* instances, contains a higher number of nodes (28-401) and a higher number of links (50-1056) but just a subset of these are required.

The present chapter is divided into two main sections. Each one presents the characteristics of different instances and then the results attained in each phase of the methodology explained in the previous chapter, Chapter 4. The results obtained through the application of this approach are compared with the best known value given by the work developed by [18] to evaluate the quality of the approach followed in this work.

The different tests were performed on an Intel(R) Core(TM) i5 CPU 2.40GHz with 4.00GB RAM.

### 5.1 *mval* Instances

This set of instances is characterized for different aspects exposed below:

- All the vehicles begin and end their trips on a special node, called depot.
- When servicing an arc/edge, this will be served just one time by the assigned vehicle.
- The deadheading cost and the service cost of each arc/edge will be different from instance to instance.

- The disposal cost isn't charged on these instances.
- The objective function of the problem is given by the sum of two different costs: deadheading cost and service cost since the disposal cost is no charged in this set of instances.
- The number of required edges is always greater than the number of required arcs.

After the description of the main characteristics of these instances, the main values of the different parameters are presented in Table 5.1.

Table 5.1: Characteristics of the *mval* instances

<i>File</i>	$ N $	$ A \cup E $	$ A_r $	$ E_r $
<b>mval1A</b>	24	55	20	35
<b>mval1B</b>	24	51	13	38
<b>mval1C</b>	24	53	17	36
<b>mval2A</b>	24	44	16	28
<b>mval2B</b>	24	52	12	40
<b>mval2C</b>	24	49	14	35
<b>mval3A</b>	24	48	15	33
<b>mval3B</b>	24	45	16	29
<b>mval3C</b>	24	43	18	25
<b>mval4A</b>	41	95	26	69
<b>mval4B</b>	41	102	19	83
<b>mval4C</b>	41	103	21	82
<b>mval4D</b>	41	104	21	83
<b>mval5A</b>	34	96	22	74
<b>mval5B</b>	34	91	35	56
<b>mval5C</b>	34	98	17	81
<b>mval5D</b>	34	92	29	63
<b>mval6A</b>	31	69	22	47
<b>mval6B</b>	31	66	22	44
<b>mval6C</b>	31	68	23	45
<b>mval7A</b>	40	86	36	50
<b>mval7B</b>	40	91	25	66
<b>mval7C</b>	40	90	28	62
<b>mval8A</b>	30	96	20	76
<b>mval8B</b>	30	91	27	64
<b>mval8C</b>	30	83	28	55
<b>mval9A</b>	50	132	32	100
<b>mval9B</b>	50	120	44	76
<b>mval9C</b>	50	125	42	83
<b>mval9D</b>	50	131	38	93
<b>mval10A</b>	50	138	32	106
<b>mval10B</b>	50	134	33	101
<b>mval10C</b>	50	136	36	100
<b>mval10D</b>	50	129	42	87

Column 2 of the Table 5.1 contains the number of the nodes of each instance. Column 3 shows the set of arcs and edges of the respective instance. The last two columns, 4 and 5, show the set of required arcs and required edges, respectively.

The results obtained to these instances are divided into three subsections, each one related with the corresponding phase of the methodology.

### 5.1.1 Phase1 - Mega-Route

Table 5.2 shows the results obtained to this set of instances tested.

Table 5.2: Phase 1 - Results obtained to *mval* Instances

<b>Phase 1 - Mega-Route</b>		
<b>File</b>	<b>Nodes</b>	<b>Objective Function</b>
<b>mval1A</b>	24	230
<b>mval1B</b>	24	261
<b>mval1C</b>	24	255
<b>mval2A</b>	24	324
<b>mval2B</b>	24	351
<b>mval2C</b>	24	313
<b>mval3A</b>	24	113
<b>mval3B</b>	24	128
<b>mval3C</b>	24	88
<b>mval4A</b>	41	566
<b>mval4B</b>	41	616
<b>mval4C</b>	41	609
<b>mval4D</b>	41	616
<b>mval5A</b>	34	597
<b>mval5B</b>	34	581
<b>mval5C</b>	34	670
<b>mval5D</b>	34	705
<b>mval6A</b>	31	326
<b>mval6B</b>	31	313
<b>mval6C</b>	31	303
<b>mval7A</b>	40	364
<b>mval7B</b>	40	412
<b>mval7C</b>	40	393
<b>mval8A</b>	30	581
<b>mval8B</b>	30	531
<b>mval8C</b>	30	527
<b>mval9A</b>	50	458
<b>mval9B</b>	50	453
<b>mval9C</b>	50	426
<b>mval9D</b>	50	478
<b>mval10A</b>	50	630
<b>mval10B</b>	50	653
<b>mval10C</b>	50	615
<b>mval10D</b>	50	562

The results presented above are divided into three columns that contain information about the number of the nodes (Column 2) and the value obtained in this phase to the objective function of the respective instance (Column 3).

These results were obtained through the use of some functions belonging to the C++ libraries from the CPLEX software. These existing functions were incorporated with the C++ code written using Visual Studio 2008 C++.

### 5.1.2 Phase2 - Intermediate Solution

The computational results obtained to this phase are shown in Table 5.3.

Table 5.3: Phase 2 - Results obtained to *mval* Instances

<b>Phase 2 - Intermediate Solution</b>			
<b>File</b>	<b>Objective Value</b>	<b>Total Demand</b>	<b>Number of Vehicles</b>
<b>mval1A</b>	272	358	2
<b>mval1B</b>	335	358	3
<b>mval1C</b>	413	328	8
<b>mval2A</b>	362	310	2
<b>mval2B</b>	427	310	3
<b>mval2C</b>	684	310	8
<b>mval3A</b>	121	137	2
<b>mval3B</b>	167	137	3
<b>mval3C</b>	196	137	7
<b>mval4A</b>	648	627	3
<b>mval4B</b>	788	627	4
<b>mval4C</b>	811	627	5
<b>mval4D</b>	1039	627	9
<b>mval5A</b>	689	614	3
<b>mval5B</b>	688	614	4
<b>mval5C</b>	815	614	5
<b>mval5D</b>	1118	614	9
<b>mval6A</b>	368	451	3
<b>mval6B</b>	368	451	4
<b>mval6C</b>	475	451	10
<b>mval7A</b>	434	559	3
<b>mval7B</b>	493	559	4
<b>mval7C</b>	603	559	9
<b>mval8A</b>	663	566	3
<b>mval8B</b>	633	566	4
<b>mval8C</b>	872	566	9
<b>mval9A</b>	556	654	3
<b>mval9B</b>	528	654	4
<b>mval9C</b>	545	654	5
<b>mval9D</b>	746	654	10
<b>mval10A</b>	705	704	3
<b>mval10B</b>	782	704	4
<b>mval10C</b>	766	704	5
<b>mval10D</b>	888	704	10

Table 5.3 contains information about the available vehicles (column 4), total demand collected (Column 3) and the value obtained by this phase for the objective function of the respective instance (Column 2).

### 5.1.3 Phase3 - Final Solution

Results obtained in this phase are exposed in Table 5.4.

Table 5.4: Phase 3 - Results obtained to *mval* Instances

Phase 3 - Final Solution				
File	Best known value	Objective Value	Time(sec)	Gap(%)
mval1A	230*	245	272	6,52%
mval1B	261*	277	233	6,13%
mval1C	309*	357	734	15,53%
mval2A	324*	350	420	8,02%
mval2B	395*	413	193	4,56%
mval2C	521*	602	700	15,55%
mval3A	115*	119	352	3,48%
mval3B	142*	151	750	6,34%
mval3C	166*	192	669	15,66%
mval4A	580*	640	660	10,34%
mval4B	650*	718	677	10,46%
mval4C	630*	762	851	20,95%
mval4D	746	949	1263	27,21%
mval5A	597*	659	809	10,39%
mval5B	613*	685	502	11,75%
mval5C	697*	786	875	12,77%
mval5D	719	928	2124	29,07%
mval6A	326*	337	355	3,37%
mval6B	317*	356	5206	12,30%
mval6C	365	457	666	25,21%
mval7A	364*	407	1079	11,81%
mval7B	412*	483	774	17,23%
mval7C	424	546	1117	28,77%
mval8A	581*	658	2147	13,25%
mval8B	531*	601	524	13,18%
mval8C	617	795	1368	28,85%
mval9A	458*	532	1020	16,16%
mval9B	453*	524	764	15,67%
mval9C	428	524	1262	22,43%
mval9D	514	696	7709	35,41%
mval10A	634*	694	935	9,46%
mval10B	661*	730	1170	10,44%
mval10C	623*	727	1405	16,69%
mval10D	643	829	2248	28,93%
<b>Average</b>			1230,38	15,41%
<b>Maximum</b>			7709	35,41%
<b>Minimum</b>			193	3,37%

In the above table are shown the final results for the instances under test. The second column shows the best known results obtained to the respective instance and if it's the optimal value is marked with an (\*). These results were demonstrated by [18].

Column 3 contains the values achieved by the approach used in this Master Thesis. Column 4 has the time in seconds and finally, the last column contains the difference in percentage between the best known result and the value obtained by the approach followed in this work.

## Results Discussion

Bellow is presented the discussion of the results attained by the new approach developed during this Master Thesis. These results were compared with the ones obtained by [18] as already mentioned.

The first phase of the methodology provides lower values for the objective function than the best known value for the same instance. This happens because the solution retrieved by this phase is an infeasible one composed by just one route travelled by one vehicle.

The solutions obtained in the second phase have values much higher than the best known values of the respective instances and that's the reason why other phase is applied. Since this solution is the one used as an input in the next phase, if it has a very high value for the objective function the Metaheuristic applied in the next phase may not be able to find a solution near to the optimal one.

The difference in percentage, called gap, between the best known result and the result achieved by this approach are depicted in the last column of the Table 5.4 and is calculated by:

$$[(BestKnownValue - ObjectiveValue) \div BestKnownValue] \times 100$$

The approach applied to obtain a solution to this set of instances doesn't provide the optimal value to none of them, as already observed in Table 5.4. As previously explained, Metaheuristics are not always able to provide the optimal solution to a given problem since it's an approximative method.

The worst scenarios were obtained for the more complex instances with a higher number of available vehicles - *mval4D*, *mval5D*, *mval6C*, *mval7C*, *mval8C*, *mval9D* and *mval10D* - as shown in Table 5.4. The results attained to these instances are between 15% and 36%.

The gap values verified to the instances *mval1A*, *mval1B*, *mval2A*, *mval2B*, *mval3A*, *mval3B* and *mval6A* are no greater than 10%. And the best value obtained is for the instance *mval6A*, with a gap near to 3.4%. In general, to the instances with a least number of vehicles are obtained good final results.

The average gap obtained to these different instances is near to the 15%, with a maximum value of 35.41% to the instance called *mval9D* that is composed by 50 nodes and 10 available vehicles.

Finally, the average CPU time obtained to this set of instances is close to 1230 s. The instance that takes longer to obtain the final solution is *mval9D* and the one that obtains faster the final solution is *mval2B*.

## 5.2 *lpr*-Instances

Some of the characteristics referred for the *mval* instances can be also applied to the *lpr* instances, like:

- All the vehicles begin and end their trips on a special node, called depot.

- When servicing an arc/edge it will be served just one time by that vehicle.
- The deadheading cost and the service cost of each arc/edge will be different from instance to instance

The main differences between these two types of instances lie on the characteristics listed beneath.

- The disposal cost, 300, is charged on this set of instances.
- The objective function of the *lpr* instances is given by the sum of the three different costs: deadheading cost, service cost and disposal cost.
- The instances *lpr-a* and *lpr-b* are composed for more required arcs than required edges while the instances *lpr-c* contains more required edges than required arcs.

These instances have a larger number of nodes and of required arcs/edges. This information can be observed in Table 5.5.

Table 5.5: Characteristics of the *lpr* instances

<i>File</i>	$ N $	$ A \cup E $	$ A_r $	$ E_r $
<b>lpr-a-01</b>	28	94	52	0
<b>lpr-a-02</b>	53	169	99	5
<b>lpr-a-03</b>	146	469	271	33
<b>lpr-a-04</b>	195	651	469	34
<b>lpr-a-05</b>	321	1056	748	58
<b>lpr-b-01</b>	28	63	45	5
<b>lpr-b-02</b>	53	117	92	9
<b>lpr-b-03</b>	163	361	279	26
<b>lpr-b-04</b>	248	582	493	8
<b>lpr-b-05</b>	401	876	764	37
<b>lpr-c-01</b>	28	52	11	39
<b>lpr-c-02</b>	53	101	23	77
<b>lpr-c-03</b>	163	316	61	241
<b>lpr-c-04</b>	277	604	142	362
<b>lpr-c-05</b>	369	841	416	387

Like the first Table presented in the section about the results obtained to the *mval* instances, this table contains a column to present the number of the nodes (column 2) of the respective instance, a column with information about the total required arcs plus required edges (column 3), and two separated columns comprising information about required arcs (column 4) and required edges (column 5).

The same approach used to solve the *mval* instances was followed to solve the *lpr* instances.

After the specification of the main principles, the results found to this set of instances are exposed in the next sections.

### 5.2.1 Phase1 - Mega-Route

The results obtained by this phase are shown in Table 5.6.

Table 5.6: Phase 1 - Results obtained to *lpr* Instances

Phase 1 - Mega-Route		
File	Nodes	Objective Function
<b>lpr-a-01</b>	28	13484
<b>lpr-a-02</b>	53	27666
<b>lpr-a-03</b>	146	74367
<b>lpr-a-04</b>	195	122732
<b>lpr-a-05</b>	321	<u>193915</u>
<b>lpr-b-01</b>	28	14474
<b>lpr-b-02</b>	53	28483
<b>lpr-b-03</b>	163	75792
<b>lpr-b-04</b>	248	<u>122624</u>
<b>lpr-b-05</b>	401	<u>200850</u>
<b>lpr-c-01</b>	28	18295
<b>lpr-c-02</b>	53	<u>35152</u>
<b>lpr-c-03</b>	163	<u>106822</u>
<b>lpr-c-04</b>	277	<u>164058</u>
<b>lpr-c-05</b>	369	<u>250365</u>

Column 2 shows the number of nodes of the respective instance and column 3 the value obtained for the objective function to the different tested instances.

It was specified a time limit to CPLEX software provide the final solution of this phase. If this maximum time is attained before the optimal solution is reached the methods used by this software should stop and return the solution found at that moment.

Observing Table 5.6 it's noticed that in some values obtained for some instances for the objective function are underlined. These values represent the instances where the maximum time (one hour) specified previously was reached.



### 5.2.2 Phase2 - Intermediate Solution

Table 5.7 contains the results obtained to the Phase 2 of the approach followed by this work.

Table 5.7: Phase 2 - Results obtained to *lpr* Instances

<b>Phase 2 - Intermediate Solution</b>			
<b>File</b>	<b>Objective Value</b>	<b>Total Demand</b>	<b>Number of Vehicles</b>
<b>lpr-a-01</b>	13591	11235	2
<b>lpr-a-02</b>	29457	23446	3
<b>lpr-a-03</b>	81430	64709	7
<b>lpr-a-04</b>	136283	108635	11
<b>lpr-a-05</b>	221676	170514	18
<b>lpr-b-01</b>	14950	12142	2
<b>lpr-b-02</b>	29575	23312	3
<b>lpr-b-03</b>	83000	63624	7
<b>lpr-b-04</b>	137664	103770	11
<b>lpr-b-05</b>	229634	171408	18
<b>lpr-c-01</b>	18927	16662	2
<b>lpr-c-02</b>	37581	31718	4
<b>lpr-c-03</b>	119294	97917	10
<b>lpr-c-04</b>	179548	149531	15
<b>lpr-c-05</b>	280251	227186	23

The aforementioned table is composed by four different columns. The first one represents the name of the respective instance, and the others contain information about the value obtained to the objective function (column 2), total demand that needs to be collected in the respective instance (column 3) and the number of available vehicles (column 4).

### 5.2.3 Phase3 - Final Solution

The final results obtained to this set of instances are presented in Table 5.8.

Table 5.8: Phase 3 - Results obtained to *lpr* Instances

Phase 3 - Final Solution				
File	Best known value	Objective Value	Time(sec)	Gap(%)
<b>lpr-a-01</b>	13484*	13554	312	0,52%
<b>lpr-a-02</b>	28052*	29300	1076	4,45%
<b>lpr-a-03</b>	76039	80665	5121	6,08%
<b>lpr-a-04</b>	126941	135280	8355	6,57%
<b>lpr-a-05</b>	202736	219715	18525	8,37%
<b>lpr-b-01</b>	14835*	14950	489	0,78%
<b>lpr-b-02</b>	28654*	29384	527	2,55%
<b>lpr-b-03</b>	77821	82693	5051	6,26%
<b>lpr-b-04</b>	126754	137277	11547	8,30%
<b>lpr-b-05</b>	209791	227983	53836	8,67%
<b>lpr-c-01</b>	18639*	18897	377	1,38%
<b>lpr-c-02</b>	36255*	37472	4330	3,36%
<b>lpr-c-03</b>	109980	118233	8196	7,50%
<b>lpr-c-04</b>	168441	178755	14591	6,12%
<b>lpr-c-05</b>	257890	278993	54467	8,18%
<b>Average</b>			12453,33	5,27%
<b>Maximum</b>			54467	8,67%
<b>Minimum</b>			312	0,52%

This table contains information about the best known value depicted on [18] (column 2), the value obtained by the application of the approach during the realization of this work (column 3), the CPU time in seconds (column 4) and finally the gap (column 5).

It's important to mention that if the best known value of an instance is the optimal solution it is marked with an (\*).

### Results Discussion

In spite of to some instances (*lpr-a-05*, *lpr-b-04*, *lpr-b-05*, *lpr-c-02*, *lpr-c-03*, *lpr-c-04*, *lpr-c-05*) the values obtained may or may not be the optimal solution to the Mega-Route of the respective instance the different values obtained by this phase of the methodology are lower than the best known results attained by [18].

In what concerns this set of instances the values obtained to the Intermediate Solution (Phase 2 of the approach developed during this work) are much higher than the best known result of the respective instance. The Metaheuristic (Phase 3) used by next phase will guarantee that the final solutions obtained are better than the solution given by the previous phase. If the value obtained

to the Intermediate solution is far from the optimal solution, the Tabu Search may not find a value near to the optimal value of the respective instance.

The values obtained to the final solution of this set of instances are close to the best known value obtained by other authors. These values are between 0.52% and 8.67%.

The instance where this approach was more effective is the instance called *lpr-a-01* with a value registered to the gap close to 0.5%. The worst scenario verified was acquired for the instance *lpr-b-05* with a gap value near to 9%.

The average of the values obtained to all the instances of this set is close to 5%. This means that the solutions obtained are near to the best known results to the same instances studied by other authors, guaranteeing that this approach when applied to a set of complex instances, will be able providing good final results.

The main disadvantage verified to the more complex instances lies on the time demanded to find the final solution. To these instances the average time calculated is close to 9500 seconds. This time will increase with the complexity of the problem under study and that's the reason why in the *lpr* instances the time needed to obtain the final solutions is much higher than the one obtained to the *mval* instances.

### 5.3 Summary

This chapter intends to show the results obtained for two different sets of instances. The first set, called *mval* instances, comprises the simplest instances that contain (24-50) nodes and (43-138) links and all of them are required. The second set, designated *lpr* instances, is composed by complex instances with (28-401) nodes and (40-1056) links where just a subset of these are required.

To evaluate the quality of the approach followed in this work should be observed two different parameters:

1. The difference between the value obtained to the objective function by this approach and the value obtained by other authors
2. The time needed to find the final solution by the approach.

To the *mval* instances the average value obtained to the gap was near to 15% while to the *lpr* instances this value is near to 5%. Concerning the average obtained to the CPU time the *lpr* instances take much longer (12453 seconds) to obtain the final solution than the *mval* instances (1230 seconds). This happens due to the complexity of the instances that belongs to each set.

In general, the approach used in this work obtains good results to the instances under test but when it is applied to complex problems this will need much time to obtain the final solution.