COMPUTER SECURITY

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Cryptography: more advanced topics (cont.)

One-way cryptography

Motivation

• «Hash functions are everywhere in cryptography — everywhere!»¹

Applications of one-way functions

- data integrity protection
 - *P* public: $\vec{F} = h(P)$ is characteristic of *P*
- confirmation of knowledge
 - *P* secret: publish F = h(P); later, when *P* is turned public, *F* proves previous knowledge of *P*
- key derivation
 - known k1, k2 = h(k1) is new key that does not compromise k1!
- pseudo-random number generation
 - *seed* secret: *h*^{*n*}(*seed*) is apparently random for any successive *n*
- ...
- Real-World Cryptography, D. Wong, Manning, 2021



Definitions¹

- (minimum) **hash** function H^2
 - compression: maps input *P* of arbitrary finite bit-length, to output *h* of fixed bit-length
 - \circ ease of computation: for any *P*
- **compression** function³
 - hash function with fixed-size inputs
- **one-way** hash function
 - impractical⁴ to invert function
- collision-resistant hash function
 - \circ impractical to find two inputs with same output



- 1 Somewhat based on Handbook of Applied Cryptography, A.J. Menezes et. al., 5th Printing, CRC Press, 2001.
- 2 can use (secret) keys or not... If unkeyed, are also called MDC (Modification Detection Code) functions.
- 3 this definition is different from the one commonly adopted see ahead!
- 4 impractical = currently, computationally infeasible

Simple examples ($P = P_1 P_2 P_3... = P_1 || P_2 || P_3...$)

• (minimum) **hash** function (*in*, len(*P*); *out*, len(*h*))¹

• $h = P_1 \bigoplus P_2 \bigoplus P_3 \bigoplus \dots$, length $(P_i) = \text{length}(h)$

- **compression** function (*in*: *m* bits ; *out*: *n* bits)
 - out = (in's first *n* bits) \oplus (in's last (*m*-*n*) bits || (2*n*-*m*) 0 bits)
- **one-way** hash function (*in*: *m* bits ; *out*: *n* bits)

• $h = P \mod \operatorname{len}(h)$

• **collision-resistant** hash function

o **?...**

1 len --> length



Note on compression function's definition:

- here adopted definition:
 - Compression function (*in*: *m* bits ; *out*: *n* bits)
- common used definition:
 - Common "Compression" function (*in*: *b* bits, *n* bits ; *out*: *n* bits)



Fig. a) Adopted definition of Compression function; b) Commonly defined "Compression" function.



Construction of hash functions

- iterated hash functions (e.g. Merkle–Damgård construction) [FIG]
 - block cipher based hash functions (e.g. Davies-Meyer construction) [FIG]
 - using existing secure cipher functions
 - customized (e.g. SHA-1)
 - specifically designed "from scratch" for optimized performance
 - modular arithmetic based¹ (e.g. MASH-1)
 - quite few implementations as research interest is low:
 - sluggish relative to customized hash functions
 - *«embarrassing history of insecure proposals»* (Menezes et al.)
 - \circ sponge constructions (e.g. SHA-3) [FIG]
 - new paradigm, allowing easy adjustment of output length

1 ISO/IEC 10118-4:1998, Hash-functions using modular arithmetic



...One-way cryptography (cont.): Iterated hash functions - Merkle–Damgård construction



Fig. Two views of the Merkle–Damgård construction: a) software-view ; b) time-view.



...One-way cryptography (cont.): Block cipher based - Davies-Meyer construction



Fig. Structure of Davies-Meyer construction (block-cipher based):
a) enciphering snippet with general idea: if *in* is fixed, *E*_{key} is one-way for mapping *key* --> *out* !
b) Davies-Meyer construction: final hashing result is iteration for all *P*_i blocks .



...One-way cryptography (cont.)

Case study (simplified): SHA-3 (sponge construction)



sponge

Fig. Sponge construct (time-view): *M* is input that, after padding, is divided in blocks of *r* (rate) bits; *Z* is output of *l* bits of length (specified by input parameter), concatenation of *r* bits' blocks; *c* is capacity, inner, never output, state bits. (*in* <u>keccak.team/sponge_duplex.html</u>)

...One-way cryptography (cont.): SHA-3 (sponge construction)

Sponge construction (cont.)

- function Keccak-*f*[1600]¹:
 - \circ group of permutations on
 - internal state: *b* bits ($5 \times 5 \times 2^6$ bits = 1600)
 - b = r + c bits
 - *r*: bits affected by input
 - *c*: always internal bits
 - group permutation:
 - $12 + 2 \times 6$ rounds of five steps: $\theta \rho \pi \chi \iota$
- specific padding rules
- Fig. Inner aspects of sponge structure: a) bits of state; b) sponge function operations.
- 1 Keccak is pronounced as "ketchak" (<u>keccak.team/keccak_specs_summary.html</u>).

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...One-way cryptography (cont.)

Overall weaknesses of irreversible systems

Problem:

- The number produced by the hashing operation is usually fixed (finite)
 - So, there **have to be** collisions, in an infinite universe of inputs!
 - Will they be likely or easy to cause?

Answer:

- that depends
 - $\circ ~~$ on the randomness of the values resulting from the operation
 - $\circ~$ on the size of those values (number of bits)
 - \circ on the intended application



...One-way cryptography: Irreversible (cont.)

Attacks

- certain: only brute force! (if one can live for enough time...)
 - the intention is to find an entry with a specific result?
 - try 2ⁿ inputs (n, number of bits of hash)
- likely: perhaps by using certain curious techniques...
 - \circ the intention is to find two entries with the same result?
 - **birthday attack**: try $\sqrt{2^n} = 2^{n/2}$ inputs for 50% chance of success
 - 2 sets of documents with the same *hash*: one "good" set, one "evil"!¹
- possible: scientifically search for construction weaknesses
 - research, research, research
 - MD5: <u>MD5 considered harmful today</u>
 - SHA-1: <u>We have broken SHA-1 in practice</u>
 - **...**

1 Diversity of possibilities for trying different documents are as simple as varying the number of spaces between words...



...One-way cryptography: Irreversible (cont.)

Ideal strength of hash function of n-bit output:

- security is as good as a random oracle with output truncated to *n* bits
- implies resistance of size:
 - $2^{n/2}$ for strong collision attacks
 - 2^n for weak collision attacks

Example: sponge construction (SHA-3) strength

- with random permutation: as strong as a random oracle
- capacity *c* determines resistance size:
 - \circ 2^{*c*} for both strong and weak collision attacks
 - unfortunately, security is traded for speed, for constant b (= r+c) size
 - higher security (*c*), lower speed (more *r*-bit input blocks to process)



Integrity & Confidentiality protection

- fact: (*confidentiality*) operation modes do not guarantee *integrity* protection¹
- so, some type of integrity protection must be added
 - basic example: combine secrecy with digital signatures [FIG]
 - in general: use *authenticated encipherment* protocols



Fig. Confidentiality with integrity protection.

1 E.g. for CBC operation mode, see Kaufman et. al, Network Security, pp. 98-101. Exercise: show the vulnerability with One time pad!

...Integrity Protection (cont.)...

Authenticated ciphering protocols (modes)¹

- special protocols developed to aggregate both protections
 - in general, integrity protection is provided by Message Integrity² Codes
 - but digital signing can also be used (of course) [previous FIG]
- the main approaches are:
 - (external) combination of protective techniques³
 - prone to vulnerabilities due to incorrect implementation
 - "intrinsic" combination
 - several standardized schemes
 - sponge functions can be used in *duplex mode*!
 - signcryption: "low-cost" combination of digital signing and ciphering⁴
- 1 *Authenticated Encryption with Associated Data* (AEAD) applies when it is explicitly necessary to assure integrity protection of plaintext data that is to accompany ciphertext (e.g. network packets might need a visible header that should be integrity protected as well as the secret payload).
- 2 or Authentication ;-)
- 3 also called "generic composition" of schemes used separately for achieving confidentiality and integrity protection
- 4 Digital Signcryption or How to Achieve Cost(Signature & Encryption)..., Y. Zheng, CRYPTO '97



...Integrity Protection with Authenticated Modes...

Authenticated Modes - "generic composition"

Encrypt-then-MAC, EtM

- ISO/IEC 19772:2009
- process: [FIG in Wikipedia]
 - 1st, encipher; 2nd, calculate MIC
 - o non-parallelizable
- different keys K_E, K_{MAC} !
- "normal" padding
- reverse process:
 - verify integrity of ciphertext; decipher to get plaintext
 - o parallelizable
- considered the more secure method (compared with the following)¹
- 1 see, for instance, Bellare & Namprempre "Authenticated Encryption: Relations among Notions and Analysis of the Generic Composition Paradigm" (2008)



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...Integrity Protection with Authenticated Modes - "generic composition" (cont.)

Encrypt-and-MAC (E&M)

- process: [FIG *in* Wikipedia]
 - encipher; calculate MIC
 - parallelizable
- apparently, a single key is enough!
- "normal" padding
- reverse process:
 - 1st, decipher to get plaintext;
 2nd, verify integrity of plaintext
 - o non-parallelizable





...Integrity Protection with Authenticated Modes - "generic composition" (cont.)

MAC-then-Encrypt (MtE)

- process: [FIG *in* Wikipedia]
 - 1st, calculate MIC; 2nd, encipher
 - o **non-parallelizable**
- apparently, a single key is enough!
- padding after hashing
- reverse process:
 - 1st, decipher to get plaintext and MAC; 2nd, verify integrity of plaintext
 - \circ non-parallelizable





...Integrity Protection with Authenticated Modes (cont.)

Authenticated Modes - "intrinsic"

- here, there is an integration of the 2 protections
 - \circ the schemes are built with provision to provide both
- the usual procedure is
 - use a primary key (*seed*) to feed an extended key-generation function
 - \circ use the generated long key, to encipher *P* in *stream* mode
 - typically, a variant of Counter Mode is used [FIG]
 - $\circ~$ use part of the generated key to produce a MIC of the ciphered (or plain) text



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... Integrity Protection with Authenticated Modes - "intrinsic" (cont.)

Some "famous" examples

Galois/Counter Mode (GCM)

- NIST 800-38D
- process: [FIG]
- confidentiality:
 - AES-128b is typical
- integrity protection: GMAC [FIG next page]
 - ciphertext + Associated Data
- apparently, highly performative (parallelization by inter-leaving & pipelining?)
- some obs:
 - *AD¹* and *C* are padded separately before being concatenated; *IV* is used sequentially in GMAC first and then in CTR; internal intermediate states are to be kept private
- 1 Associated Data





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...Integrity Protection with Authenticated Modes - "intrinsic"

ChaCha20-Poly1305

- RFC 8439
- designed by D. J. Bernstein
 - \circ ChaCha20¹ stream cipher
 - Poly1305 authenticator
- process: [FIG]
 - key stream feeds
 - first, message integrity code function (counter=0)
 - then, XOR cipher (counter>0)
 - *AD* and *C* are padded separately before being concatenated



1 20 is because it performs 10 times a double set of operations.



...Integrity Protection with Authenticated Modes - "intrinsic": ChaCha20-Poly1305

ChaCha20-Poly1305 (cont.): Chacha20

- input: 32B (256b) key, 12B (96b) IV (*nonce*), 4B (32b) counter [FIG]
- output: stream key in 64B (512b) blocks
- internal state: 4 x 4 x 4B (16 32b-integers) = 64 B (512b)
- block function: [FIG]
 - sequence of 10 double¹ "quarter"-rounds
 - quarter-round: set of operations on 4 numbers (addition modulo 2^{32} , XOR, left-shift of *n* bits)
 - o final sum with input
- encipher algorithm:
 - for each iteration (increasing counter), use key stream to cipher 64B block of Plaintext
- deciphering is obvious

state (4x4 32b ints) in:





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^{1 10 * 2 = 20 (}Chacha20!)

...Integrity Protection with Authenticated Modes - "intrinsic": ChaCha20-Poly1305



- input:
 - two-part key (r (16B) , k (16B)), 16B nonce,
 - arbitrary-length message (sequence of bytes)
- output: 16B (128b) MAC
- arithmetic operations with 16B groups used as numbers



Fig. D. J. Bernstein's Poly1305 authenticator: 128b MAC.

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nonce P

Poly1305

Κ

...Integrity Protection with Authenticated Modes - "intrinsic"

SpongeWrap

• sponge construct in duplex mode



Fig. Sponge construct in duplex-mode for authenticated enciphering (AEAD): notice that plaintext P is XORed, block by block, with f's outputs - the *keystream*, k_i ! The function *pad* is used for padding blocks.

Exercise: adapt the picture to a stream cipher in which the "sponge" generates the key(s).

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(could be continued...)

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Pointers...

- **"Block cipher mode of operation"**, -2024 Wikipedia
 - en.wikipedia.org/wiki/Block cipher mode of operation
- "Recommendation for Block Cipher Modes of Operation: Galois/Counter Mode (GCM) and GMAC", 2007 M. Dworkin, NIST
 - <u>nvlpubs.nist.gov/nistpubs/Legacy/SP/nistspecialpublication800-38d.pdf</u>
- "The Poly1305-AES Message-Authentication Code", 2005 D. Bernstein
 - <u>link.springer.com/content/pdf/10.1007/11502760_3.pdf</u>
- "ChaCha, a variant of Salsa20", 2008 D. Bernstein
 cr.yp.to/chacha/chacha-20080120.pdf
- **"Duplexing the sponge: single-pass authenticated encryption...**", 2011 G. Bertoni, J. Daemen, M. Peeters, G.Van Assche
 - eprint.iacr.org/2011/499.pdf
- **"The sponge and duplex constructions**", -2023, G. Bertoni, J. Daemen, S. Hoffert, M. Peeters, G. Van Assche, R. Van Keer
 - <u>keccak.team/sponge_duplex.html</u>

