# Control and communication of distributed hybrid systems 

ACC 2001 Tutorial
July 27th, 2001

Tunc Simsek<br>Joao Sousa<br>Pravin Varaiya

## Hybrid automata



- Labeled state machine
- Hybrid state

$$
(x, s) \in \mathfrak{R} \times\{\text { Foo, Bar }\}
$$

- Discrete modes model the distinct behaviors of the continuous time plant/controller
- Transitions model mode switches and discrete control actions


## Hybrid Automata - composition



## Synchronous composition

## Input/output composition



Image from E.A. Lee, P. Varaiya, Structure and Interpretation of Signals and Systems, 2000. (available from http://ptolemy.eecs.berkeley.edu/eecs20/)

## Hybrid Automata - Execution traces

- Evolution in alternating phases of discrete transitions and time passage
- Multiple discrete transitions



## Models

A model of the operation of distributed dynamic systems should capture two essential features

- Switched mode operation
- Dynamic interactions


Click here to view
Quicktime movie

## Dynamic networks of hybrid automata (DNHA)

nodes refer to each other using links

each node is a hybrid automaton

- A network of hybrid automata that evolve in parallel
- Network is dynamic because nodes may be created and destroyed as system evolves


## DNHA - execution traces

- Evolution in alternating phases of discrete transitions and time passage
- State vectors reconfigured on discrete transitions



## DNHA:

## SHIFT visual syntax



## SHIFT syntax

- Prototype-based description: type Component \{ input ... what we feed to it
output ... what we see on the outside
state ... what's internal
discrete ... discrete symbolic actions export ... event (transition) labels setup ... actions executed at create time
data model flow ... transition ...
continuous and discrete evolution \}
- Prototypes are instantiated:
create(Component)


## SHIFT models

- Primitives:
- hybrid automata
- encapsulated input/output/state variables
- arbitrarily complex flows
- structured transitions
- strong typing (write syntactically correct programs)
- numbers, sets, arrays (first order predicate calculus)
- Combination facilities:
- continuous input/output connections
- synchronous composition
- Abstraction facilities:
- prototyping
- inheritance


## SHIFT models: one-to-one composition



- synchronous composition


## SHIFT models: <br> Combination



- synchronous composition
- simple
- existential quantification (illustrated above)
- universal quantification
- existentially quantified automata may be used in actions


## SHIFT models:

 Combinationinput/output composition

- algebraic readouts through links: $u=y(c 1)$
- explicit connections



## SHIFT models: Inheritance

First define a general interface:
type VehicleDynamics \{
output continuous number xDot, yDot, zDot; continuous number wx, wy, wz;
\}

## SHIFT models: Inheritance

## Specialize generic interface:

```
type k_vehicle_dynamics: VehicleDynamics {
    input continuous number xDDot, yDotIn;
        number xDotInit;
    output number vehicle_length := 0;
    export exiting, stopping, running;
    discrete cruise, stopped, exit2;
flow
    default { xDot' = xDDot; yDot = yDotIn; };
transition
    cruise -> stopped {stopping} do {xDot := 0;},
    stopped -> cruise {running},
    cruise -> exit2 {exiting};
}
```

