

## Métodos Formais em Eng.<sup>a</sup> de Software

### EXERCÍCIOS

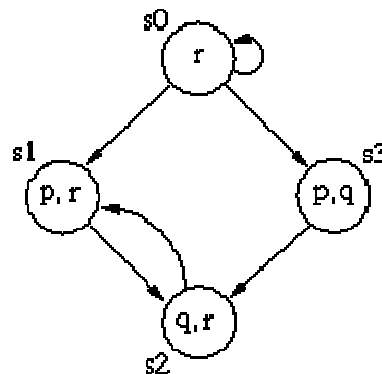
- 1) Which of the specifications in plain English below convey the mathematical meaning of the CTL formula  $AG(p \rightarrow A[q U r])$  ?
  - a. Any reachable state in which  $p$  is true has a path from it on which  $r$  is eventually true, and until then  $q$  is true.
  - b. If  $p$  is true in every reachable state, then there is a path along which  $q$  is continuously true, until  $r$  becomes true.
  - c. If  $p$  is true in every reachable state, then for any path along which  $q$  is continuously true,  $r$  becomes true.
  - d. For any reachable state in which  $p$  is true, then, on any path from that state,  $q$  is continuously true until  $r$  becomes true, and  $r$  is guaranteed to become true.
  - e. If  $p$  is true in every reachable state, then on every path there is a state at which  $r$  is true, and  $q$  is true continuously until then.
  
- 2) Consider the transition system  $(S, \rightarrow, L)$  where,

the set of states  $S$  equals  $\{s_0, s_1, s_2, s_3\}$ ;

the state transitions are  $(s_0, s_0)$ ,  $(s_0, s_1)$ ,  $(s_0, s_3)$ ,  $(s_1, s_2)$ ,  $(s_2, s_1)$  and  $(s_3, s_2)$ ; and

the labeling function is given by  $L(s_0) = \{r\}$ ,  $L(s_1) = \{p, r\}$ ,  $L(s_2) = \{q, r\}$ , and  $L(s_3) = \{p, q\}$ .

This model may be pictured as follows:



Which of the CTL formulas below are satisfied in state  $s_0$ ?

- a.  $AF(q \wedge r)$
- b.  $AG(p \rightarrow AF(p \wedge r))$
- c.  $A[r U q]$
- d.  $AG(p \rightarrow AG(p \vee q))$
- e.  $AG EF \neg r$

3) Which of the following pairs of CTL formulas are equivalent?

- a.  $EF p$  and  $EG p$
- b.  $EF p \vee EF q$  and  $EF (p \vee q)$
- c.  $AF p \vee AF q$  and  $AF (p \vee q)$
- d.  $AF p$  and  $A[p \cup \top]$
- e.  $EF \neg p$  and  $\neg AF p$

4) Consider the SMV program fragment:

```

MODULE main()
VAR
  a : boolean;
  b : boolean;
ASSIGN
  init(a) := 0;
  init(b) := 0;
  next(a) :=
    case
      ~a : 1;
      1 : {0,1};
    esac;
  next(b) :=
    case
      ~a : 0;
      b : 1;
      1 : {0,1};
    esac;

```

Which of the following CTL models is adequately modeled by this SMV program fragment?

