

Software Testing, Verification and Validation

October 26, 2022
Week #6 — Lecture #5

Last week, we introduced model-based testing as part of our set of black-box techniques. This week we are moving to white-box techniques and therefore we will use the source code itself as a source of information to create tests.



Brenan Keller

@brenankeller

A QA engineer walks into a bar.
Orders a beer. Orders 0 beers.
Orders 999999999999999 beers.
Orders a lizard. Orders -1 beers.
Orders a ueicbksjdhd.



Brenan Keller

@brenankeller

A QA engineer walks into a bar.
Orders a beer. Orders 0 beers.
Orders 999999999999 beers.
Orders a lizard. Orders -1 beers.
Orders a ueicbksjdhd.

First real customer walks in
and asks where the bathroom
is. The bar bursts into flames,
killing everyone.

White-box testing

Knowledge sources

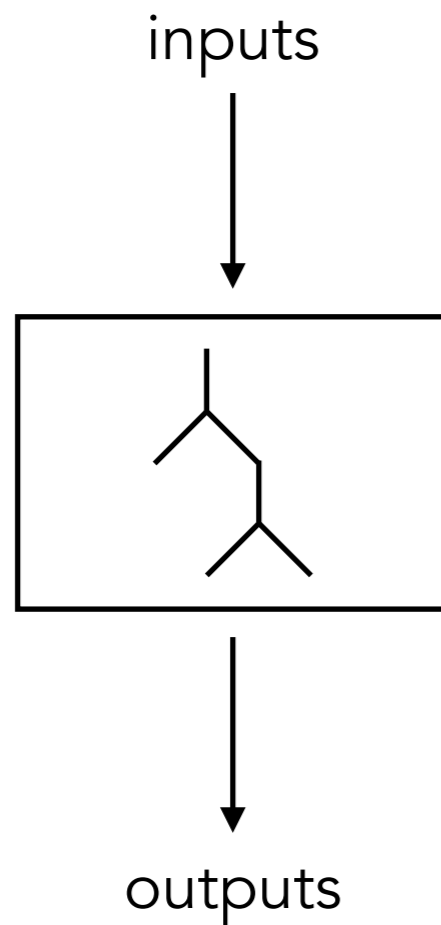
Source code

Control flow graphs

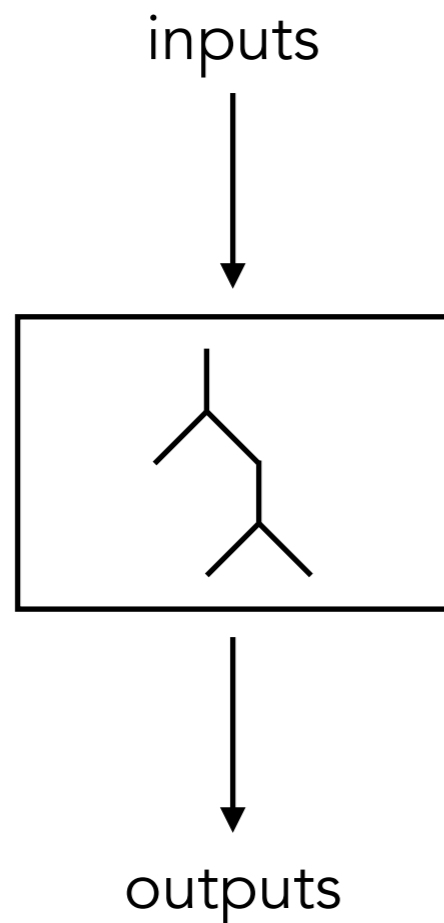
Data flow graphs

Cyclomatic complexity

...



White-box testing



Techniques

Control flow analysis

- Statement coverage

- Branch coverage

- Condition coverage

- Modified Condition/Decision coverage

- Path coverage

Data flow testing/coverage

- All def

- All p-uses

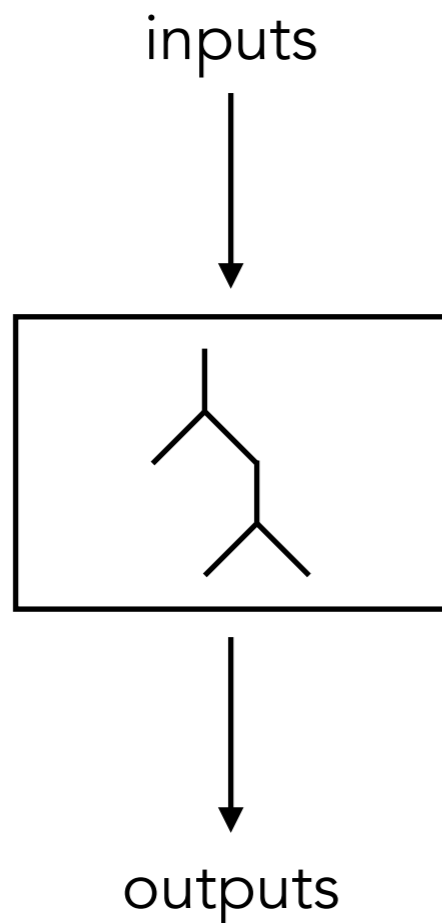
- All c-uses

Mutation testing

...

White-box testing

Techniques



- 👉 Control flow analysis
- 👉 Statement coverage
- 👉 Branch coverage
- Condition coverage
- Modified Condition/Decision coverage
- Path coverage
- Data flow testing/coverage
 - All def
 - All p-uses
 - All c-uses
- Mutation testing
- ...

White-box Testing

Adequacy

Since we cannot exhaustively test a software system, the two central questions in software testing are

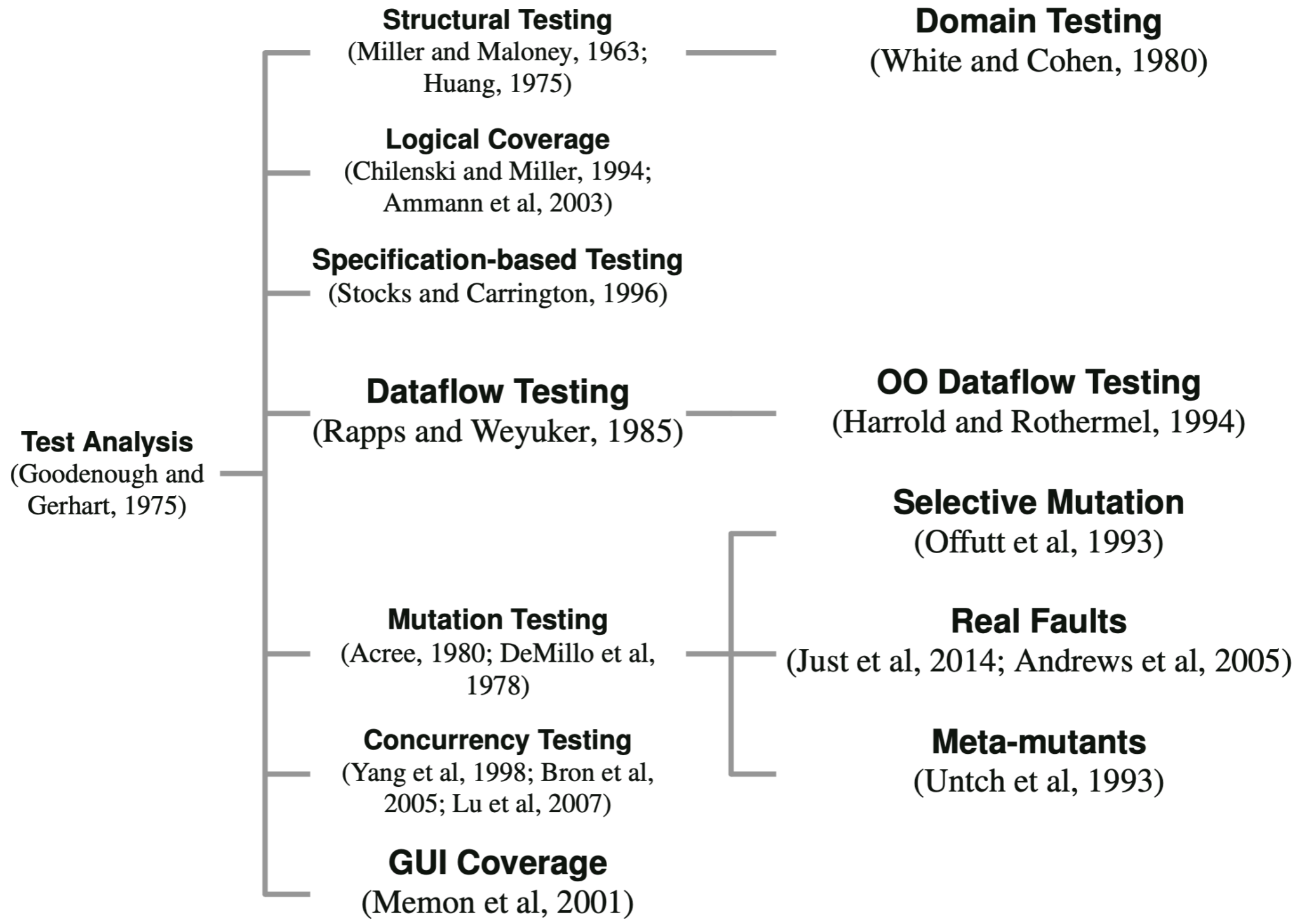
- (a) what does constitute an **adequate** set of test cases?
- (b) how do we generate a finite set of test cases that satisfies these adequacy criteria?

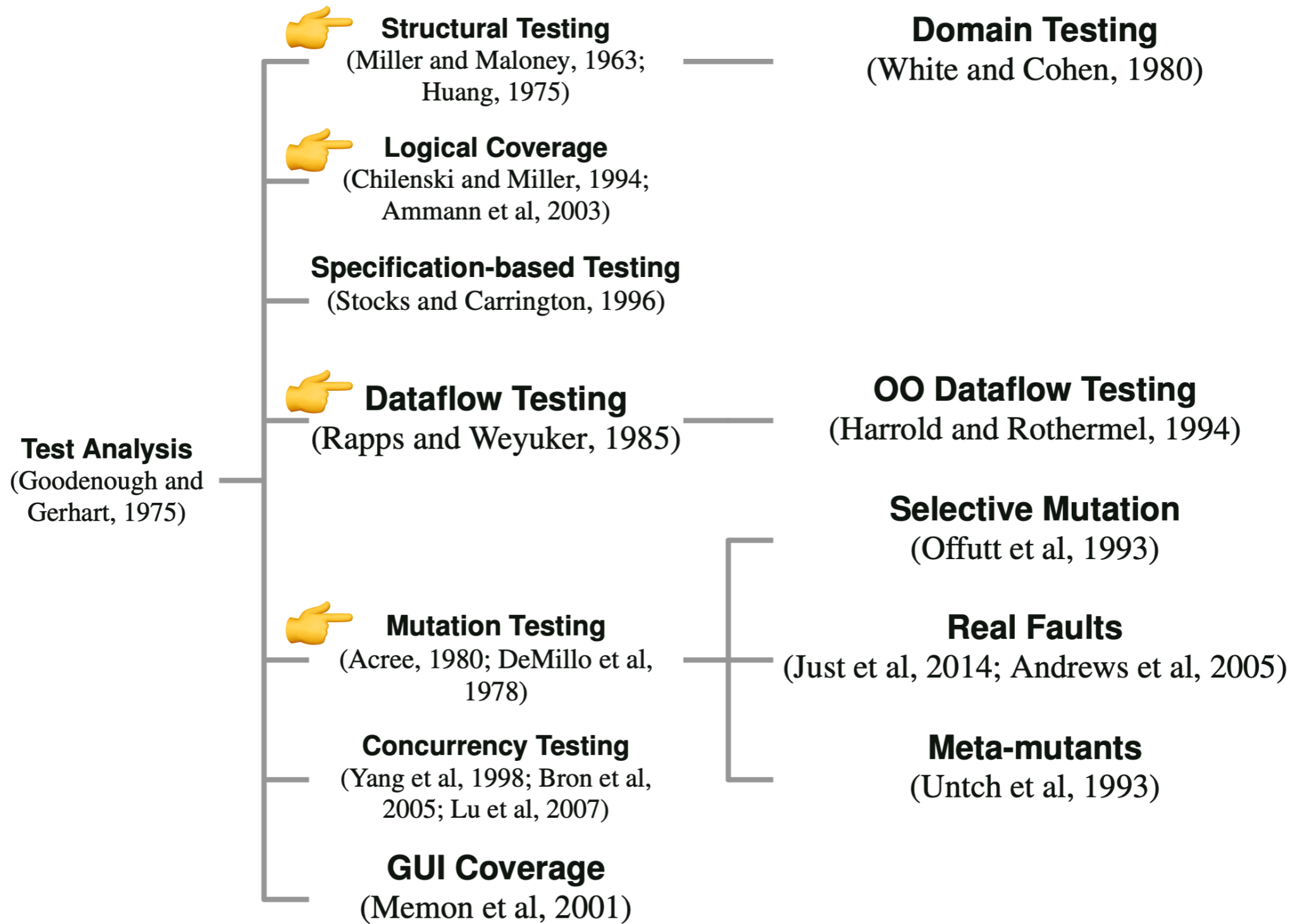
Goodenough and Gerhard defined a set of tests as adequate if its correct execution implies no errors in the program, more pragmatic solutions are based on a basic insight: **If some unit of code is not executed, i.e., covered, then by definition, testing cannot reveal any faults contained in it.** The adequacy of a set of tests can therefore be measured by how much of a program is covered by the set. While ideally one would like to know how much of the possible behavior of the program is covered, there is no easy way to quantify coverage of behavior, and therefore the majority of adequacy criteria revolve around proxy measurements related to program code or specifications.

Measurement of Adequacy

Many **coverage criteria** have been proposed over time. A coverage criterion in software testing serves three main purposes.

1. It answers the question of adequacy: Have we tested enough? If so, we can stop adding more tests, and the coverage criterion thus serves as a stopping criterion.
2. It provides a way to quantify adequacy: We can measure not only whether we have tested enough based on our adequacy criterion, but also *how much* of the underlying proxy measurement we have covered. Even if we have not fully covered a program, does a given set of tests represent a decent effort, or has the program not been tested at all?
3. Coverage criteria can serve as generation criteria that help a tester decide what test to add next.





Structural Testing

Structural Testing

The idea of code coverage is intuitive and simple: If no test executes a *faulty* statement, then the defect cannot be found; hence every statement should be covered by some test.

Why do we need structural testing?

- 1) To systematically derive tests from source code.
- 2) To know when to stop testing.

As a tester, when performing specification-based testing, your goal was clear: to derive classes out of the requirement specifications, and then to derive test cases for each of the classes. You were satisfied once all the classes and boundaries were systematically exercised.

The same idea applies to structural testing. First, it gives us a systematic way to devise tests. As we will see, a tester might focus on testing all the lines of a program; or focus on the branches and conditions of the program. Different criteria produce different test cases.

Second, to know when to stop. It is easy to imagine that the number of possible paths in a mildly complex piece of code is just too large, and exhaustive testing is impossible. Therefore, having clear criteria on when to stop helps testers in understanding the costs of their testing.

Line Coverage

Line Coverage

Line coverage is the most basic criterion; a set of test cases is considered to be adequate according to line coverage if all lines of code have been executed.

Let's assume a program that receives the number of points of two blackjack players. The program must return the number of points of the winner. In blackjack, whoever gets closer to 21 points wins. If a player goes over 21 points, the player loses. If both players lose, the program must return 0.

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public class BlackJack {  
  
    public int play(int left, int right) {  
        int ln = left;  
        int rn = right;  
        if (ln > 21)  
            ln = 0;  
        if (rn > 21)  
            rn = 0;  
        if (ln > rn)  
            return rn;  
        else  
            return ln;  
    }  
}
```

The program receives the number of points of two blackjack players. The program must return the number of points of the winner. In blackjack, whoever gets closer to 21 points wins. If a player goes over 21 points, the player loses. If both players lose, the program must return 0.

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            return rn;  
        else  
            return ln;  
    }  
}
```

**What would
you test?**
(now, only looking to the
source code)

The program receives the number of points of two blackjack players. The program must return the number of points of the winner. In blackjack, whoever gets closer to 21 points wins. If a player goes over 21 points, the player loses. If both players lose, the program must return 0.

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}
```

First idea: "going through all the lines".

If our test suite exercises all the lines, we should be happy, right? 🤔

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t1 = (30, 30)

The program receives the number of points of two blackjack players. The program must return the number of points of the winner. In blackjack, whoever gets closer to 21 points wins. If a player goes over 21 points, the player loses. If both players lose, the program must return 0.

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8            return rn;  
9        else  
10           return ln;  
    }  
}
```

First idea: "going through all the lines".

If our test suite exercises all the lines, we should be happy, right? 🤔

t1 = (30, 30)
9/10 = 90% line coverage

$$\text{line coverage} = \frac{\# \text{ lines covered}}{\# \text{ lines}} \times 100\%$$

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t1 = (30, 30)

t2 = (?, ?)

The program receives the number of points of two blackjack players. The program must return the number of points of the winner. In blackjack, whoever gets closer to 21 points wins. If a player goes over 21 points, the player loses. If both players lose, the program must return 0.

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t1 = (30, 30)

t2 = (10, 9)

10/10 = 100%

The program receives the number of points of two blackjack players. The program must return the number of points of the winner. In blackjack, whoever gets closer to 21 points wins. If a player goes over 21 points, the player loses. If both players lose, the program must return 0.

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t1 = (30, 30)

t2 = (10, 9)

10/10 = 100%

An interesting aspect of line coverage is that it is quite easy to visualize the achieved coverage, in order to help developers improve the code coverage of their tests.

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Is this useful?

Yes. We actually just found a defect!

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5        if (rn > 21)  
6            rn = 0;  
7        if (ln > rn)  
8            return rn; ← ln  
9        else  
10       return ln; ← rn  
    }  
}
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Is this useful?

Yes. We actually just found a defect!

Using lines of code as a way to determine line coverage is a simple and straightforward idea. However, counting the covered lines is not always a good way of calculating the coverage. The number of lines in a piece of code depends on the decisions taken by the programmer who writes the code.

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public class Blackjack {  
  
    public int play(int left, int right) {  
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t2 = (10, 9)
6/10 = 60% line
coverage, previously

5/6 = 83% line
coverage, now

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Some coverage tools measure coverage at statement level. Statements are the unique instructions that your JVM, for example, executes. This is a bit better, as splitting one line of code in two would not make a difference.

Decision (or branch) Coverage

Statement/Line coverage is generally seen as a weak criterion, although in practice it is one of the most common criteria used. One reason for this is that it is very intuitive and easy to understand. Stronger criteria are often based on the control flow graph of the program under test. For example, consider the following snippet:

```
if (e < 0)
    e = 0;
if (b == 0)
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```
if (e < 0)
    e = 0;
if (b == 0)
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```

It is possible to achieve 100% statement coverage of this snippet with a single test where `e` is less than 0 and `b` equals 0. This test case would make both if conditions evaluate to `true`, but there would be no test case where either of the conditions evaluates to `false`. **Branch coverage captures the notion of coverage of all edges in the control flow graph, which means that each if condition requires at least one test where it evaluates to `true`, and at least one test where it evaluates to `false`.** In the case of above snippet, we would need at least two test cases to achieve 100% branch coverage, i.e., t1: `e<0` and `b==0`; t2: `e>=0` and `b!=0`.

Decision (or Branch) Coverage

Complex programs often rely on lots of complex conditions (e.g., if statements composed of many conditions). When testing these programs, aiming at 100% line coverage might not be enough to cover all the cases we want. We need a stronger criterion.

Branch coverage (or decision coverage) works similar to line and statement coverage, except with branch coverage we count (or aim at covering) all the possible decision outcomes.

A set of test cases will achieve 100% branch (or decision) coverage when tests exercise all the possible outcomes of decision blocks.

Decision (or Branch) Coverage

Decisions (or branches) are easy to identify in a **Control-Flow Graph (CFG)**. A control-flow graph is a representation of all paths that might be traversed during the execution of a piece of code. It consists of **basic blocks, decision blocks, and arrows/edges** that connect these blocks.

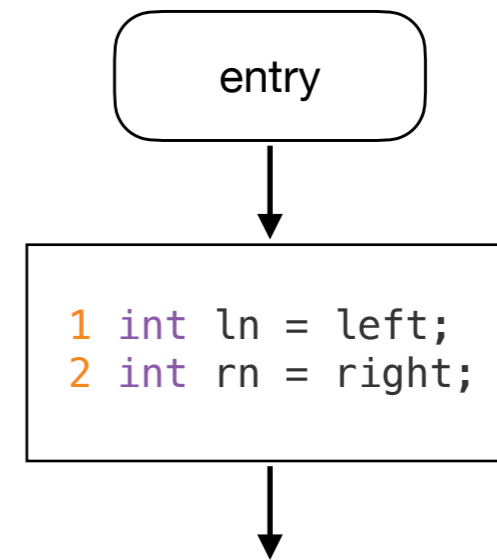
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```

A basic block is composed of "the maximum number of statements that are executed together no matter what happens". In the code below, lines 1-2 are always executed together. Basic blocks are often represented by a square:

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public class Blackjack {  
  
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}
```

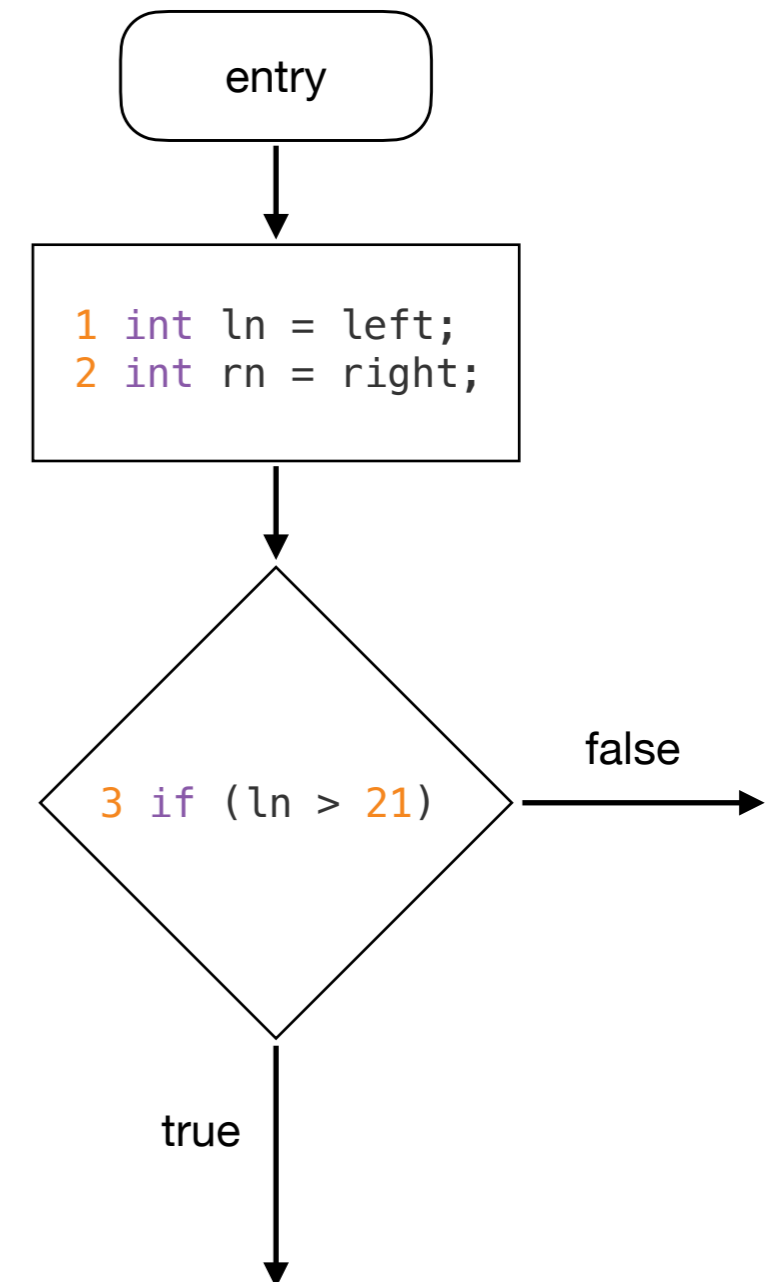
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7       if (ln > rn)  
8           return rn;  
9       else  
10          return ln;  
    }  
}
```



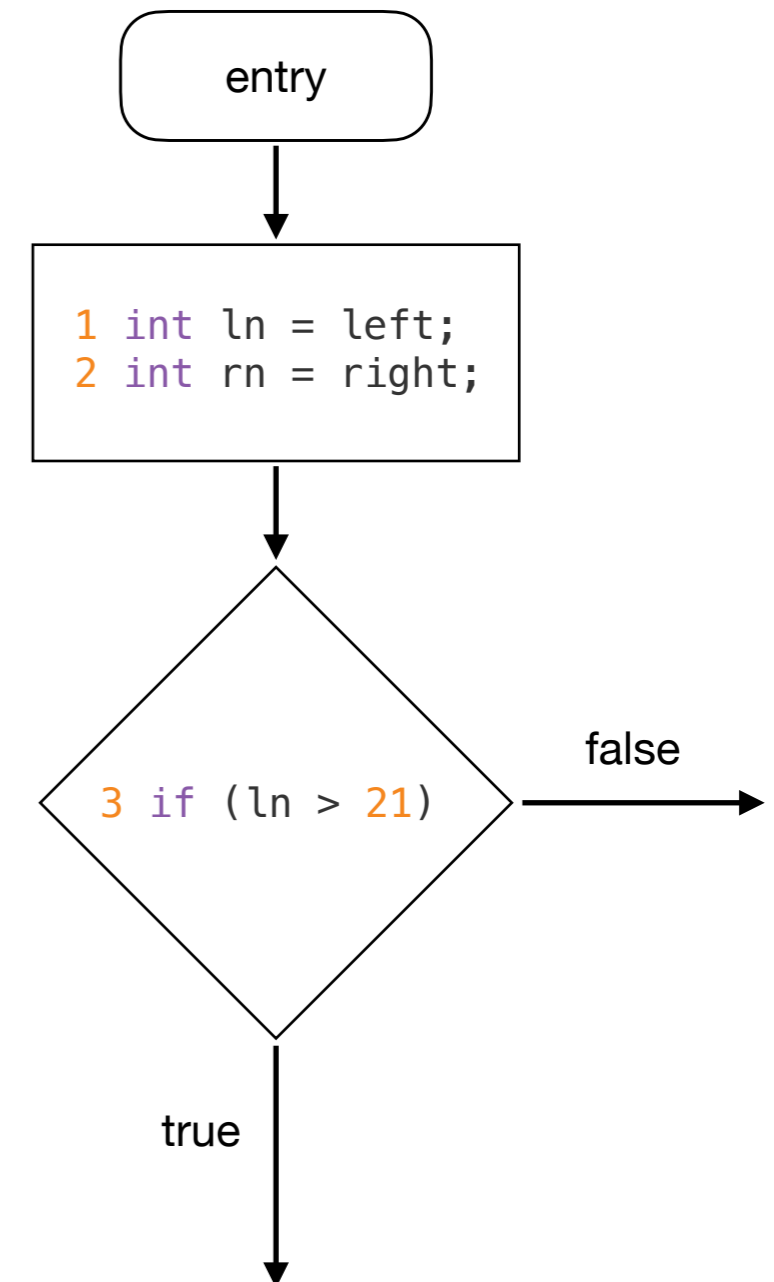
A decision block, on the other hand, represents all the statements in the source code that can create different branches, e.g., line 3. This if statement creates a decision moment in the application: based on the condition, it is decided which code block will be executed next. Decision blocks are often represented by diamonds. This decision block happens right after the basic block we created above, and thus, they are connected by means of an edge.

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public class Blackjack {  
    public int play(int left, int right) {  
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6           rn = 0;  
7       if (ln > rn)  
8           return rn;  
9       else  
10          return ln;  
    }  
}
```



A basic block has always a single outgoing edge. A decision block, on the other hand, always has two outgoing edges (indicating where you go in case of the decision being evaluated to `true`, and where you go in case the decision is evaluated to `false`). In case of the decision block being evaluated to `true`, line 4 is executed, and the program continues to line 5. Otherwise, it proceeds straight to line 5, which is another decision block.

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public class Blackjack {  
    public int play(int left, int right) {  
1         int ln = left;  
2         int rn = right;  
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4             ln = 0;  
5         if (rn > 21)  
6             rn = 0;  
7         if (ln > rn)  
8             return rn;  
9         else  
10            return ln;  
    }  
}
```



$$\text{branch coverage} = \frac{\text{\# decision outcomes covered}}{\text{\# decision outcomes}} \times 100\%$$

```
public class BlackJack {  
  
    public int play(int left, int right) {  
1        int ln = left;  
2        int rn = right;  
3        if (ln > 21) // True ? False ?  
4            ln = 0;  
5        if (rn > 21) // True ? False ?  
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    }  
  
}
```

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public class BlackJack {  
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t1 = (30, 30)

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9      else
10         return ln;
    }
}

```

t1 = (30, 30)

3/6 = 50%
branch
coverage

McCabe's Cyclomatic Complexity

McCabe's Cyclomatic Complexity

Cyclomatic Complexity (CC) is a metric used for measuring the complexity of a software program.

This metric was developed by Thomas J. McCabe in 1976 and it is based on a control-flow representation of the program. In other words, it is a quantitative measure of linearly independent paths in the source code of a software program. **A linearly independent path is defined as a path that has at least one edge which has not been traversed by any other path.**

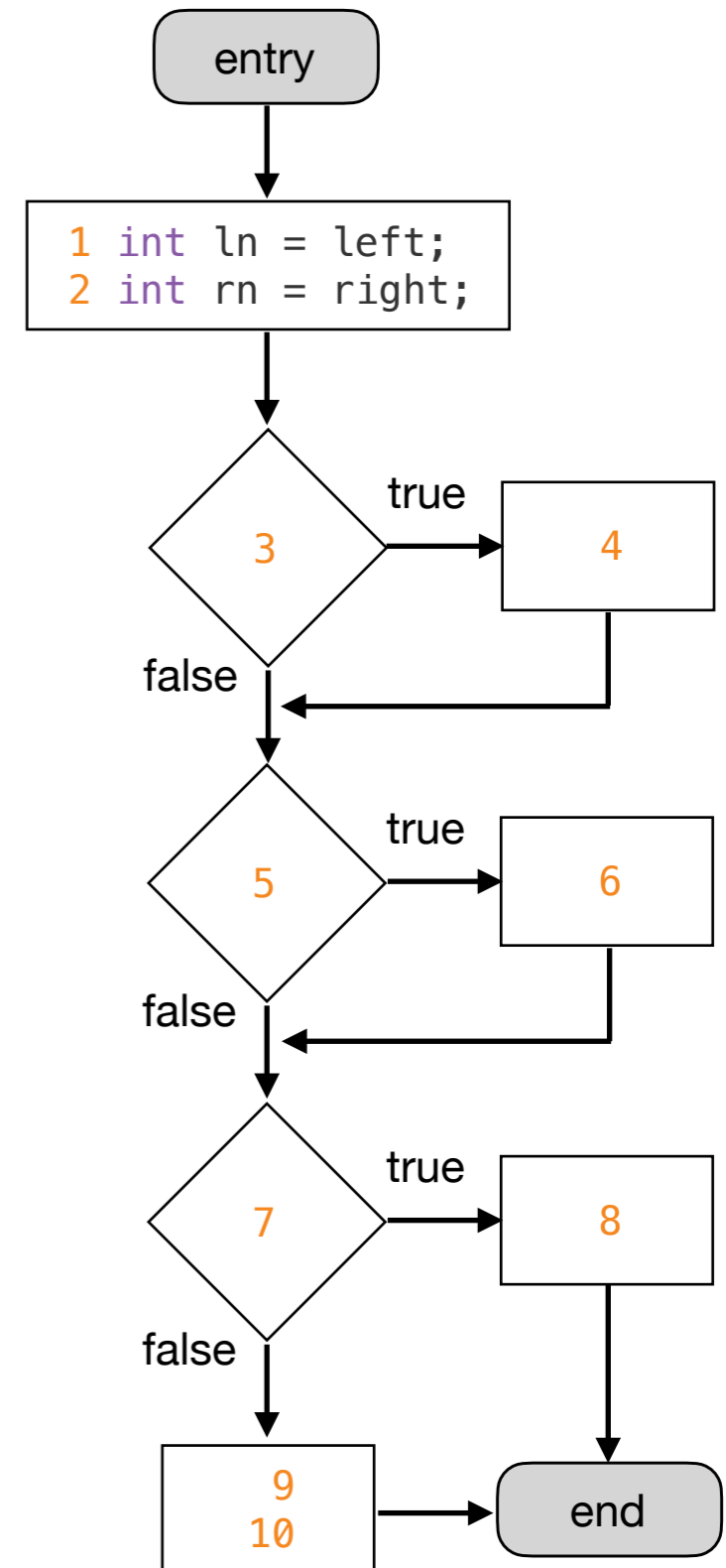
How to compute CC?

1. Construct the control-flow graph with nodes and edges from the source code.

CC, example

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10          return ln;  
    }  
}
```



How to compute CC?

1. Construct the control-flow graph with nodes and edges from the source code.
2. Compute CC (lower CC == better code)
 - of a structured function, e.g., a function with a single exit point, aka return statement, as

$$E - N + 2P$$

- of a non-structured function, e.g., a function with more than one exit point, in each exit point is connected back to the entry point, as

$$E - N + P$$

E = number of edges

N = number of nodes

P = number of connected components, aka graphs, P is always 1 for single functions

CC, example

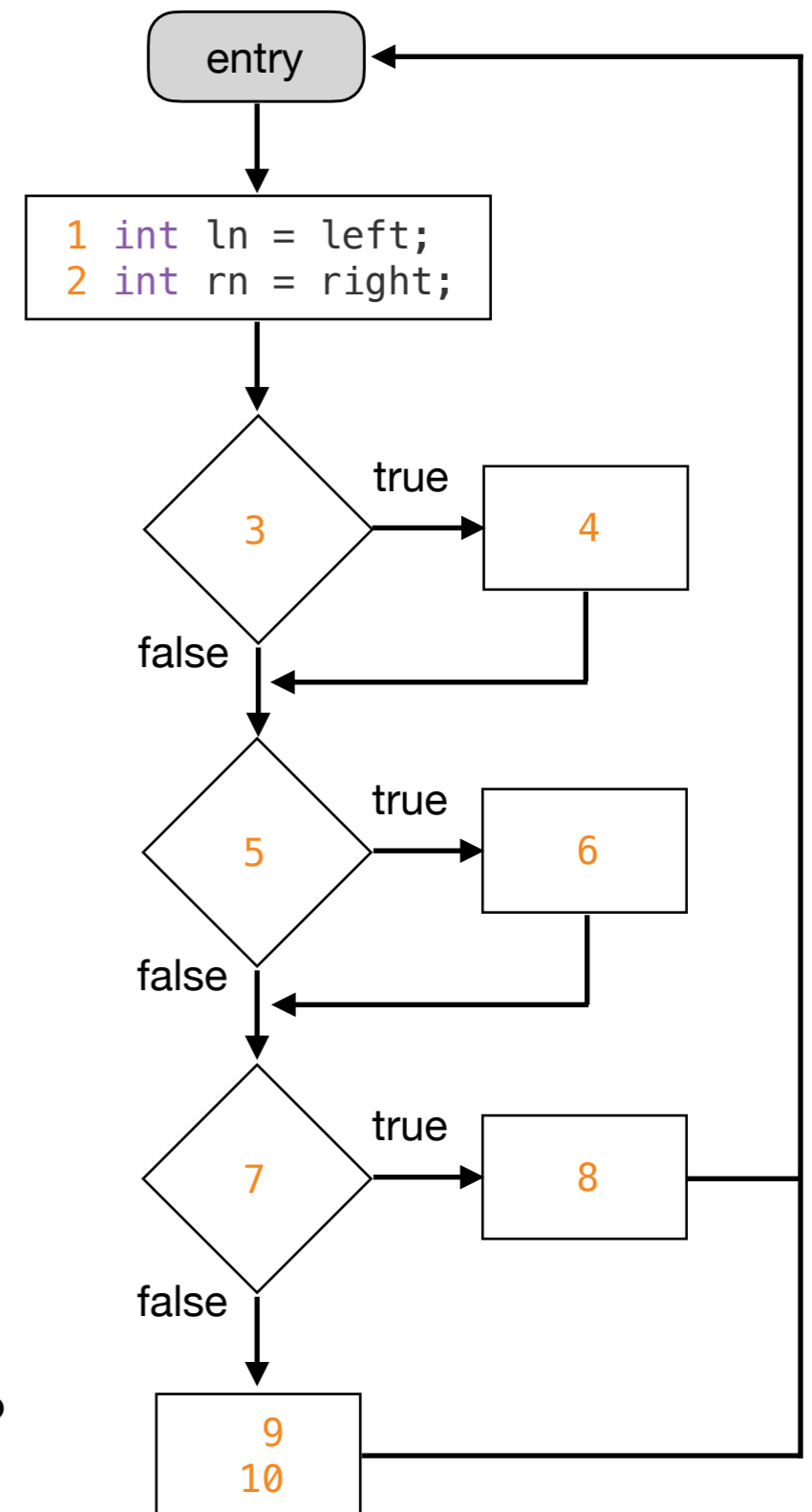
2. Compute CC as, $E - N + P$

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    public int play(int left, int right) {  
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3       if (ln > 21)  
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6           rn = 0;  
7       if (ln > rn)  
8           return rn;  
9       else  
10          return ln;  
    }  
}
```

Edges = 12

Nodes = 8 "normal" nodes + 1 entry node

CC = $12 - 9 + 1 = 4$ independent paths, but which ones?



CC, example

3. Identify the independent paths. Recall that a linearly independent path is defined as a path that has at least one edge which has not been traversed by any other path.

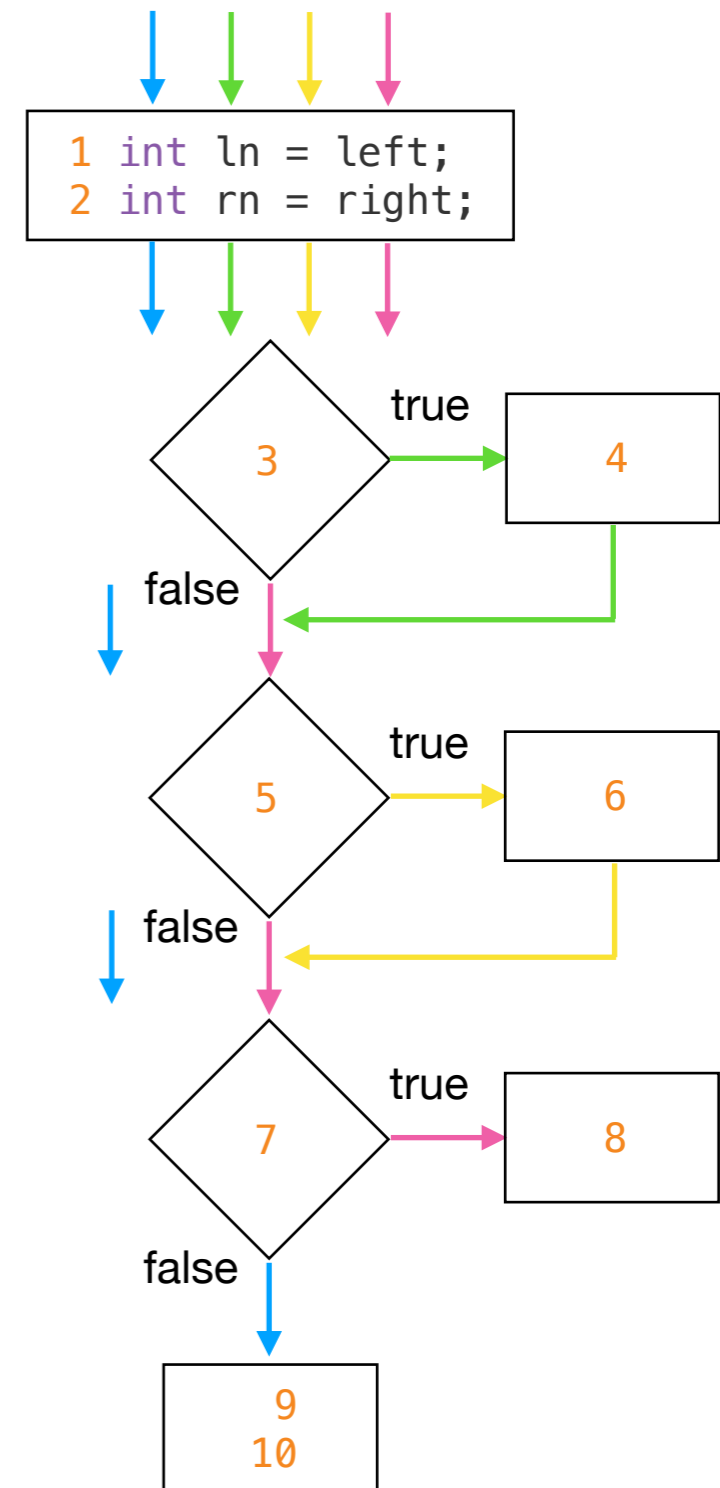
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2         int rn = right;  
3         if (ln > 21)  
4             ln = 0;  
5         if (rn > 21)  
6             rn = 0;  
7         if (ln > rn)  
8             return rn;  
9         else  
10            return ln;  
    }  
}
```

path 1: 1, 2, 3, 5, 7, 9, 10

path 2: 1, 2, 3, 4, 5, 7, 9, 10

path 3: 1, 2, 5, 6, 7, 9, 10

path 4: 1, 2, 3, 5, 7, 8



How to compute CC?

1. Construct the control-flow graph with nodes and edges from the source code.

2. Compute CC (lower CC == better code)

- of a structured function, e.g., a function with a single exit point, aka return statement, as

$$E - N + 2P$$

- of a non-structured function, e.g., a function with more than one exit point, in each exit point is connected back to the entry point, as

$$E - N + P$$

3. Identify the independent paths.

4. Derive the tests.

CC, example

4. Derive the tests. Tip: the number of tests is basically the cyclomatic complexity value of the program.

```
public class Blackjack {  
  
    public int play(int left, int right) {  
1       int ln = left;  
2       int rn = right;  
3       if (ln > 21)  
4           ln = 0;  
5       if (rn > 21)  
6           rn = 0;  
7       if (ln > rn)  
8           return rn;  
9       else  
10          return ln;  
    }  
  
}
```

Cyclomatic Complexity, 👍 and 👎

Advantages 👍

- It is easy to apply.
- It is able to guide the testing process, i.e., it helps developers and testers to determine independent path executions.
- Developers can assure that all the paths have been tested at least once.
- Helps developers and testers to focus more on the uncovered paths.

Disadvantages 👎

- It is the measure of the programs' control complexity and not the data complexity.

Tools

- EclEmma: Java Code Coverage for Eclipse

<https://www.eclemma.org>

- JaCoCo

<https://www.jacoco.org/jacoco>

- Cobertura: A code coverage utility for Java

<http://cobertura.github.io/cobertura/>

- Code2flow: automatic generation of diagrams from source code

<https://app.code2flow.com>

- MetricsTree: an IntelliJ IDEA plugin to compute source code metrics as cyclomatic complexity, for example

<https://github.com/b333vv/metricstree>

References

- Gordon Fraser and José Miguel Rojas; Software Testing, 2019. ISBN 978-3-030-00262-6.
- Chapter 5 of the Practical software testing a process-oriented approach. Ilene Burnstein, 2002.
- Chapter 12 of the Software Testing and Analysis: Process, Principles, and Techniques. Mauro Pezzè, Michal Young, 1st edition, Wiley, 2007.
- Chapter 4 of the Foundations of software testing: ISTQB certification. Graham, Dorothy, Erik Van Veenendaal, and Isabel Evans, Cengage Learning EMEA, 2008.
- Zhu, H., Hall, P. A., & May, J. H. (1997). Software unit test coverage and adequacy. ACM computing surveys.