

(adaptado de Grainger e Stevenson)

Tópico: Exemplificação de cálculos do efeito de contingências usando a matriz Z

Rede

Todos os valores em p.u

Linhas (z)		Produção	
1-2	j0.1	nó 1	CR
1-4	j0.05	nó 5	1.45
2-3	j0.0625	$V_1=V_5=1$ pu	
2-5	j0.04	Carga	
3-5	j0.05	2	1.4+j0.10
4-5	j0.08	3	1.0+j0.20
2	j5	4	0.8+j0.15

Tensões /caso base (obtidas executando um TP)

```
>> V=[1 0.986301-0.083834j 0.984789-0.095108j 0.993653-0.045583j 0.998498-0.054795j].'
```

V =

```
1.0000
0.9863 - 0.0838i
0.9848 - 0.0951i
0.9937 - 0.0456i
0.9985 - 0.0548i
```

Matrizes Y e Z

```
>> Y=[1/0.1j+1/0.05j -1/0.1j 0 -1/0.05j 0;
-1/0.1j 1/0.1j+1/0.04j+1/0.0625j+1/5j -1/0.0625j 0 -1/0.04j;
0 -1/0.0625j 1/0.0625j+1/0.05j 0 -1/0.05j;
-1/0.05j 0 0 1/0.05j+1/0.08j -1/0.08j;
0 -1/0.04j -1/0.05j -1/0.08j 1/0.04j+1/0.05j+1/0.08j]
```

Y =

Columns 1 through 4

```
0 -30.0000i 0 +10.0000i 0 0 +20.0000i
0 +10.0000i 0 -51.2000i 0 +16.0000i 0
0 0 +16.0000i 0 -36.0000i 0
0 +20.0000i 0 0 0 -32.5000i
0 0 +25.0000i 0 +20.0000i 0 +12.5000i
```

Column 5

```
0
0 +25.0000i
0 +20.0000i
0 +12.5000i
0 -57.5000i
```

» Z=inv(Y)

Z =

Columns 1 through 4

0 + 5.0615i	0 + 5.0000i	0 + 5.0063i	0 + 5.0422i
0 + 5.0000i	0 + 5.0000i	0 + 5.0000i	0 + 5.0000i
0 + 5.0063i	0 + 5.0000i	0 + 5.0358i	0 + 5.0095i
0 + 5.0422i	0 + 5.0000i	0 + 5.0095i	0 + 5.0633i
0 + 5.0114i	0 + 5.0000i	0 + 5.0145i	0 + 5.0171i

Column 5

0 + 5.0114i
0 + 5.0000i
0 + 5.0145i
0 + 5.0171i
0 + 5.0262i

Saída da linha 2-5: efeito na linha 5-3

» L5352=- (0.04j/0.05j) * (Z(5,5) -Z(5,2) -Z(3,5) +Z(3,2)) / (Z(2,2) +Z(5,5) -2*Z(2,5) -0.04j)

L5352 =

0.6715

» I53a=(V(5) -V(3))/0.05j

I53a =

0.8063 - 0.2742i

» I52a=(V(5) -V(2))/0.04j

I52a =

0.7260 - 0.3049i

» I53b=I53a+ L5352*I52a

I53b =

1.2938 - 0.4789i

» abs(I53b), angle(I53b)*180/pi

ans =

1.3796 (correcto: 1.381)

ans =

-20.3142 (correcto: -18.51°)

Saída da linha 2-5: efeito nas tensões

» $A_c = [0 \ 1 \ 0 \ 0 \ -1]$

$A_c =$

$$\begin{matrix} 0 & 1 & 0 & 0 & -1 \end{matrix}$$

» $I_a = A_c * V / (0.04j - A_c * Z * A_c')$

$I_a =$

$$- 2.0971 + 0.8808i$$

» $I_a = (V(2) - V(5)) / (0.04j - Z(5,5) + Z(2,2) - 2 * Z(2,5))$

$I_a =$

$$- 2.0971 + 0.8808i$$

» $V_1 = V + I_a * Z * A_c'$

$V_1 =$

$$\begin{matrix} 1.0100 + 0.0238i & (1 + j0) & \text{Notar que é CR} \\ 0.9863 - 0.0838i & (0.9689 - j0.1081) & \\ 0.9976 - 0.0646i & (0.9778 - j0.0885) & \\ 1.0087 - 0.0098i & (0.9944 - j0.0334) & \\ 1.0215 + 0.0001i & (0.9997 - j0.0231) & \text{Notar que é PV} \end{matrix}$$

» $I_{53c} = (V_1(5) - V_1(3)) / 0.05j$

$I_{53c} =$

$$1.2938 - 0.4789i \quad \text{Igual ao obtido anteriormente, claro!}$$

Transferência de 0.45 pu do barramento 5 para 1: efeito na linha 4-5

» $K_{541} = (Z(5,1) - Z(4,1)) / 0.08j$, $K_{545} = (Z(5,5) - Z(4,5)) / 0.08j$

$K_{541} =$

$$-0.3853 \quad (\text{a corrente no sentido 5-4 diminui quando aumenta a corrente no nó 1})$$

$K_{545} =$

$$0.1137 \quad (\text{a corrente no sentido 5-4 aumenta quando aumenta a corrente no nó 5})$$

» $I_{54a} = (V(5) - V(4)) / 0.08j$

$I_{54a} =$

$$-0.1152 - 0.0606i$$

» $I_{54b} = I_{54a} + K_{541} * 0.45 + K_{545} * (-0.45)$

$I_{54b} =$

$$-0.3397 - 0.0606i \quad (\text{exacto: } -0.3424 - j0.0483)$$