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**FEUP**

**Estimation of the glottal pulse  
from speech or singing voice**

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**Master's Thesis submitted in partial fulfillment of the requirements for  
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# **ESTIMATION OF THE GLOTTAL PULSE FROM SPEECH OR SINGING VOICE**

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## ***Abstract***

The human speech production system is, briefly, the result of the convolution between the excitation signal, the glottal pulse, and the impulse response resulting from the transfer function of the vocal tract. This model of voice production is often referred to in the literature as a source-filter model, where the source represents the flow of the air leaving the lungs and passing through the glottis (space between the vocal folds), and the filter representing the resonances of the vocal tract and lip/nostrils radiation.

The estimation of the shape of the glottal pulse from the speech signal is of significant importance in many fields and applications, since the most important features of speech related to voice quality, vocal effort and speech disorders, for example, are mainly due to the voice source. Unfortunately, the glottal flow waveform which is at the origin of the glottal pulse, is a very difficult signal to measure directly and non-invasively.

Several methods for estimating the glottal pulse have been proposed over the last few decades, but there is not yet a complete and automatic algorithm which performs reliably. Most of the developed methods are based on an approach called inverse filtering. The inverse filtering approach represents a deconvolution process, i.e., it seeks to obtain the source signal by applying the inverse of the vocal tract transfer function to the output speech signal. Despite the simplicity of the concept, the inverse filtering procedure is complex because the output signal may include noise and it is not straightforward to accurately model the characteristics of the vocal tract filter.

In this dissertation we discuss a new glottal pulse prototype and a robust frequency-domain approach for glottal source estimation that uses a phase-related feature based on the Normalized Relative Delays (NRDs) of the harmonics. This model is applied to several speech signals (synthetic and real), and the results of the estimation of the glottal pulse are compared with the ones obtained using other state-of-the-art methods.

**Key words:** glottal pulse, glottal model, estimation of the glottal pulse, inverse filtering, integration in the frequency-domain, Normalized Relative Delays (NRDs), frequency-domain glottal source estimation.

## Resumo

O processo de produção humana de voz é, resumidamente, o resultado da convolução entre o sinal de excitação, o impulso glótico, e a resposta impulsiva resultante da função de transferência do trato vocal. Este modelo de produção de voz é frequentemente referido na literatura como um modelo fonte-filtro, em que a fonte representa o fluxo de ar que sai dos pulmões e passa pela glote (espaço entre as pregas vocais), e o filtro representa as ressonâncias do trato vocal e a radiação labial/nasal.

Estimar a forma do impulso glótico a partir do sinal de voz é de importância significativa em diversas áreas e aplicações, uma vez que as características de voz relacionadas, por exemplo, com a qualidade da voz, esforço vocal e distúrbios da voz, devem-se, principalmente, ao fluxo glotal. No entanto, este fluxo é um sinal difícil de determinar de forma direta e não invasiva.

Ao longo das últimas décadas foram desenvolvidos vários métodos para estimar o impulso glótico mas ainda não existe um algoritmo completo e automático. A maioria dos métodos desenvolvidos baseia-se num processo designado por filtragem inversa. A filtragem inversa representa, portanto, a desconvolução, ou seja, procura obter o sinal de entrada aplicando o inverso da função de transferência do trato vocal ao sinal de saída. Apesar da simplicidade do conceito, o processo de filtragem inversa não é simples uma vez que o sinal de saída pode incluir ruído e não é simples modelar com precisão as características do filtro do trato vocal.

Nesta dissertação apresentamos um novo protótipo de impulso glótico e um método robusto de estimação da fonte glótica, no domínio das frequências, que usa uma característica de fase baseada nos Atrasos Relativos Normalizados (NRDs) dos harmónicos. Este modelo é aplicado a diversos sinais de voz (sintéticos e reais), e os resultados obtidos da estimação do impulso glótico são comparados com os obtidos usando outros métodos analisados no estado da arte.

**Palavras chave:** impulso glótico, modelos de impulso glótico, estimação do impulso glótico, filtragem inversa, integração no domínio das frequências, Atrasos Relativos Normalizados (NRDs), estimação do impulso glótico no domínio das frequências.

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“A mind without instruction can no more bear fruit than a field, however fertile, without cultivation.”  
(Cicero).

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# Notations

- $f_s$  : Sampling frequency of a discrete signal.
- F0 or  $f_0$  : Fundamental frequency in Hz of a periodic signal.
- $T_0 = 1 / f_0$  : Fundamental period.
- $x(t)$  : Continuous signal with respect to time  $t$ .
- $x[n]$  : Discrete signal with respect to sample  $n$ .
- $x(t) * y(t)$  : Convolution between  $x(t)$  and  $y(t)$ .
- $A_v$  : Peak amplitude of the glottal pulse.
- $\alpha_m$  : Asymmetry coefficient of the glottal pulse.
- $ceps$  : Smooth magnitude of the spectral envelope based on the spectral peaks of the harmonics of the voiced speech signal.
- $dif$  : Difference between the magnitude of the spectral peaks of the voiced speech signal and the magnitude of the interpolation of the spectral envelope.
- $m_F$  : Magnitude of the (vocal tract) filter.
- $m_{HM}$  : Magnitude of the spectral peaks of the hybrid LF - Rosenberg glottal model.
- $m_S$  : Magnitude of the spectral peaks of the harmonics of the speech signal.
- $nrd_G$  : Normalized Relative Delay (NRD) coefficients of the source signal.
- $nrd_F$  : Normalized Relative Delay (NRD) coefficients of the (vocal tract) filter.
- $nrd_S$  : Normalized Relative Delay (NRD) coefficients of the speech signal.
- $NRD_{slope\ dif}$  : Difference between the slope of the Normalized Relative Delays (NRDs) of the speech signal and the slope of the NRDs of the source signal.
- $T_p$  : Opening glottal phase length.
- $T_l$  : Closing glottal phase length.
- $T$  : Total length of the glottal cycle.
- $t_c$  : Duration of the period of the glottal flow waveform ( $t_c = T_0 = 1 / f_0$ ).
- $t_p$  : Time of the maximum of the glottal pulse.
- $t_e$  : Time of the minimum of the time-derivative of the glottal pulse.
- $t_a$  : Return phase duration.

# Acronyms

<b>AQ</b>	Amplitude Quotient
<b>AR</b>	AutoRegressive
<b>CALM</b>	Causal-Anticausal Linear Model
<b>CC</b>	Complex Cepstrum
<b>CIQ</b>	Closing Quotient
<b>DAP</b>	Discrete All-Pole Modelling
<b>DCT</b>	Discrete Cosine Transform
<b>DFT</b>	Discrete Fourier Transform
<b>DTFT</b>	The Discrete Time Fourier Transform
<b>EGG</b>	ElectroGlottography
<b>FFT</b>	Fast Fourier Transform
<b>GCI</b>	Glottal Closing Instant
<b>GOI</b>	Glottal Opening Instant
<b>H<sub>1</sub>-H<sub>2</sub></b>	Difference of the first two harmonics on the decibel scale
<b>HRF</b>	Harmonic Richness Factor
<b>IAIF</b>	Iterative Adaptive Inverse Filtering
<b>IDFT</b>	Inverse of the Discrete Fourier Transform
<b>LF</b>	Liljencrants-Fant glottal model
<b>LF<sup>Rd</sup></b>	Transformed-LF glottal model
<b>LP</b>	Linear Prediction
<b>LPC</b>	Linear Predictive Coding
<b>MFCC</b>	Mel Frequency Cepstrum Coefficients
<b>NAQ</b>	Normalized Amplitude Quotient
<b>NRD</b>	Normalized Relative Delay
<b>Odd-DFT</b>	Odd-frequency Discrete Fourier Transform
<b>OQ</b>	Open Quotient
<b>PSIAIF</b>	Pitch Synchronous Iterative Adaptive Inverse Filtering
<b>SNR</b>	Signal to Noise Ratio
<b>SQ</b>	Speed Quotient
<b>VTF</b>	Vocal Tract Filter
<b>ZZT</b>	Zeros of the Z-Transform

# Usual Expressions

<b>Analysis/synthesis method</b>	A method that entirely models an observed signal by choosing a combination of its parameters, originating a reconstructed signal which is as close as possible to the observed signal.
<b>Formant</b>	A resonant frequency of the vocal tract.
<b>Glottal flow</b> or <b>Glottal source</b>	The airflow velocity waveform that comes out of the glottis and enters the vocal tract.
<b>Glottal model</b>	A mathematical model of the glottal pulse.
<b>Glottal pulse</b>	The shape of the glottal source in a single period, corresponding to a puff of air at the glottis. Frequently is referred to as glottal flow or glottal source.
<b>Normalized Relative Delay (NRD)</b>	Relative delay difference between a harmonic and the fundamental frequency sinusoid, divided by the period of the sinusoid.
<b>Pitch</b>	The perceptual measure of the fundamental frequency of a sound.
<b>Quasi-periodic</b>	A particular case of aperiodicity waveform where the deviation from periodicity is very small.
<b>Spectral analysis</b>	Analysis of a signal by the amplitude, frequency and phase of its component sinusoids.
<b>Source-filter theory</b>	Theory that describes the human voice production process as source signal, representing the glottal airflow, which is modulated by a transfer (filter) function determined by the shape of the vocal tract.
<b>Unvoiced sound</b>	Sound produced without the vibrations of the vocal folds (they simply remain open).
<b>Voiced sound</b>	Sound produced by the vibrations of the vocal folds.

# Chapter 1

## INTRODUCTION

*"Nothing so surely reveals the character  
of a person as his voice."  
(Benjamin Disraeli)*

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### 1.1. OVERVIEW

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Voice is one of the most important instruments of human communication and it is such a complex phenomenon that, despite being investigated over the years in different areas as engineering, medicine and singing, not all of its attributes seem to be known.

As sound identity of human beings, the voice reflects individual characteristics such as age, sex, race, social status, personal characteristics and even emotional state. It is maybe in the nuances and inflections of the voice that lies the expressive power of human language. Claudius Galen, a Greek second century physician, physiologist and philosopher, studied the voice production and believed that voice was the mirror of the soul<sup>1</sup>.

Voice is the unique signal generated by the human vocal apparatus and is perceived as the sounds originated from a flow of air from the lungs, which causes the vocal folds to vibrate, and that are subsequently modified by the vocal tract. Very briefly, voice is the result of a balance between two forces: the force of the air leaving the lungs and the muscle strength of the larynx, where the vocal folds are located. As a physical phenomenon, voice is defined as a

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<sup>1</sup> In [http://www.acsu.buffalo.edu/~duchan/new\\_history/ancient\\_history/galen.html](http://www.acsu.buffalo.edu/~duchan/new_history/ancient_history/galen.html)

complex sound, whose voiced regions, i.e., those resulting from a vibration of the vocal folds, consist of a fundamental frequency and a large number of harmonics [Sun87].

Several mathematical models have been proposed over the years both to model the voice production system or to estimate the flow of air passing through the glottis (i.e., the space between the vocal folds) (e.g. [JBM87], [BDA<sup>+</sup>05], [Alk95]), called the glottal flow or glottal source<sup>2</sup>. Most models of the voice production system presume that voice is the result of an excitation signal, consisting in the voice source, and that is modulated by a transfer (filter) function determined by the shape of the vocal tract. This model is often referred to as the "source-filter model of speech production" (e.g. [Fan60], [JBM87], [Air08b], [Mag05]).

According to Fant's source-filter theory, the glottal flow and the transfer function of the vocal tract are linearly separable from the speech signal [Fan60]. Specifically, using a technique called inverse filtering, it is possible to cancel the spectral effects of the vocal tract and lip and nostrils radiation on a speech signal and, then, to estimate the glottal source, i.e., the waveform produced at the glottis. Separation between source and filter is one of the most difficult challenges in speech processing, since neither the glottal or the vocal contributions are observable in the speech waveform.

The importance of the estimation of the glottal source is well established in speech science, providing insight into the voice signal, which is of potential benefit in many application areas such as speech coding, synthesis or re-synthesis, speaker identification, the non-invasive assessment of laryngeal aspects of voice quality and the study of pathological voices (since perturbations on the glottal flow component are considered to be one of the main sources of speech disorders), the vocal perception of emotions, and the extraction of musically relevant phonation parameters for biofeedback purposes. However, it is difficult to observe the glottal behaviour from the speech signal and the concealed location of the vocal folds makes rather difficult the direct observation and measurement of their vibration, which implies intrusive techniques. This motivates the development of computational procedures for the estimation of the glottal source directly from the speech signal.

Most approaches for estimating the glottal source are time-domain based. Nevertheless, there are several advantages on the spectral approach to voice source estimation when compared to time-domain methods, including the possibility to control spectral magnitude and phase independently, and to characterize the spectral profile of the noise so as to minimize its impact.

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<sup>2</sup> Some authors consider the glottal source as the derivative of the glottal pulse. However, as it will be assumed in this dissertation, the most common definition of the glottal source is as the sound wave propagated from the glottis into the vocal tract.

The goal of this thesis is to present a new glottal pulse prototype and a glottal source estimation algorithm that comprises frequency-domain signal analysis and synthesis, and relies on an accurate spectral magnitude modelling of the harmonics of the speech signal. In particular, a new feature is used that is based on the Normalized Relative Delays (NRDs) of the spectral harmonics.

This new approach results from accurate sinusoidal/harmonic analysis and synthesis of two concomitant acoustic signals for vowels /a/ and /i/: the glottal source signal captured near the vocal folds, and the corresponding voiced signal outside the mouth. The experimental procedure in which these signals were captured will be described and the obtained data will be studied in two main parts. Firstly, the magnitude and the group delay of the glottal source signal will be analysed and, based on the results, we propose a new glottal source model combining features of two reference glottal models - the Liljencrants-Fant and the Rosenberg models. Secondly, the same analysis is made using the signals captured outside the mouth and from the results of the two-time-aligned signals, we attempt to synthesize the glottal pulse using the estimation of the NRDs and the magnitude of the spectral peaks of the voice source. To validate the proposed approach, the results of the estimation of the glottal pulse will be critically compared and discussed with the ones obtained using representative state-of-the-art methods, highlighting the advantages of a spectral approach.

Although the estimation of the glottal source has been extensively studied over the last decades, it is very likely that it will continue to be an open topic over the next few years, which shows both its importance and complexity.

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## 1.2. OBJECTIVES

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Many inverse filtering methods and processes of estimation of the glottal pulse were developed over the last years, but a fully automatic procedure is not yet available and, as it was stated before, the estimation of the glottal source is important in many application areas which justifies the motivation of this work.

The main purpose of this thesis is to present a new frequency-domain algorithm to glottal source estimation, highlighting the advantages of a spectral approach and the potential of a new phase-related feature based on the Normalized Relative Delays (NRDs) of the harmonics.

With this work we hope to contribute to the development of non-invasive procedures of estimation of the glottal pulse and to enhance scientific knowledge about the glottal pulse and speech analysis.

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### 1.3. STRUCTURE OF THE DISSERTATION

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Chapter 2, “Human speech production system”, presents the analysis of the anatomy and physiology of the organ of voice, and the three systems that integrate the voice organ (the breathing apparatus, the vocal folds and the vocal tract) are briefly described.

Chapter 3, “Models of voice production”, gives an overview of the fundamental source-filter theory of speech production and its usual simplifications and hypothesis. Also, different methods of extraction of characteristics from speech signals and several glottal waveform models are summarized as well as their respective mathematical details.

Chapter 4, “Estimation of the glottal flow: state of the art”, describes several techniques of estimation of the glottal flow that are representative of the state of art, namely inverse filtering methods. A brief evaluation of those methods using synthetic and real speech signals is presented and the corresponding results of the estimation of the glottal pulse are discussed and compared.

Chapter 5, “Frequency-domain approach to glottal source estimation”, presents a new approach and algorithm for the estimation of the glottal source signal, which is implemented in the frequency domain and is based on the results of an experimental procedure from which the data set of our work was obtained.

This process of the estimation of the glottal pulse is applied to several speech signals (synthetic and real) and the obtained results are critically compared to the ones obtained using other procedures that are representative of the state of the art. This chapter also reviews the Normalized Relative Delay (NRD) concept and demonstrates how to accurately implement signal integration in the frequency domain.

Chapter 6, “Conclusions”, summarizes the main results obtained in the context of this dissertation, relates them to the findings of the previous research and adds remarks and possible directions for future research.

# Chapter 2

## HUMAN SPEECH PRODUCTION SYSTEM

### Contents

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## 2.1. INTRODUCTION

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An understanding of the human speech production system is essential in the context of our research.

This chapter begins with a brief anatomic and physiologic study of the voice organ and a description of the speech production process. A particular emphasis is placed on the glottal source signal and associated phases.

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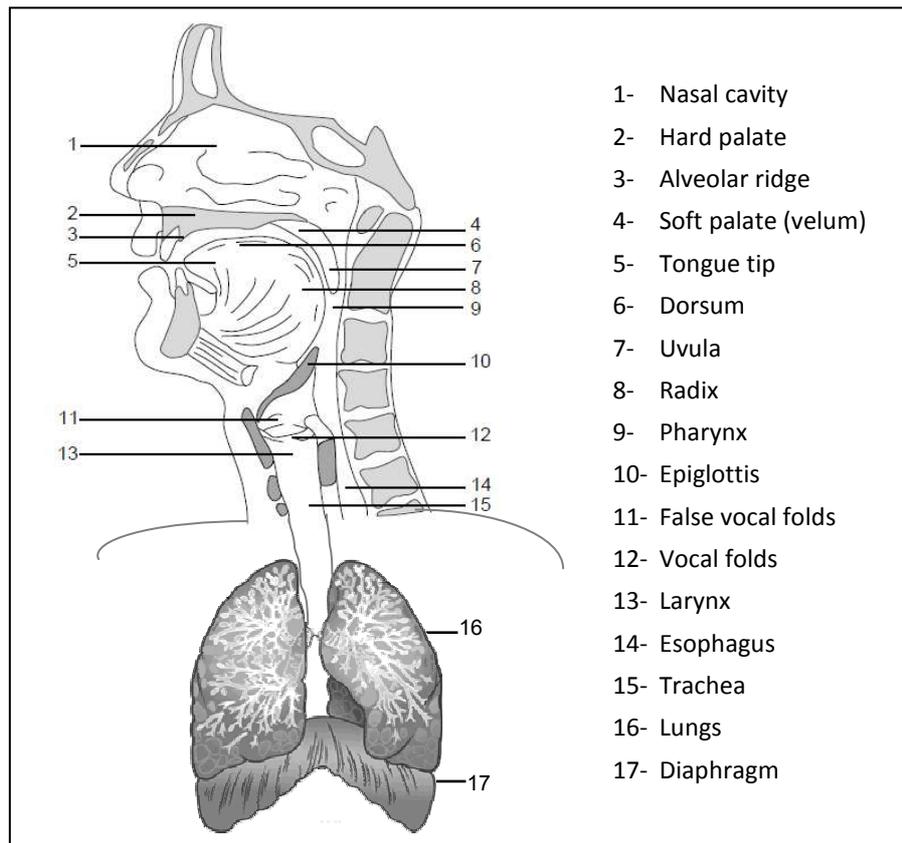
## 2.2. ANATOMY AND PHYSIOLOGY OF THE VOICE ORGAN

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The voice organ, also called phonetic system, consists of three different systems: the breathing apparatus, the vocal folds and the vocal tract. Figure 2.1 illustrates the human voice production mechanism.

The lungs or respiratory organs, are spongy structures with numerous wells that provide a large surface area for gas exchange with the blood. They are located in the chest, which is separated from the abdominal cavity by the diaphragm. The latter, together with the intercostal muscles, promote respiratory movements [KG00].

On expiration, the diaphragm and intercostal muscles relax causing a decrease in the volume of the thorax and hence the increase of pressure in the chest pushes the air out of the lungs. This causes an increase in subglottal pressure that forces the opening of the vocal folds, an end-point of which is found at the site of the Adam's Apple (i.e., at the midpoint of the larynx). As air rushes through the vocal folds, these may start to vibrate, opening and closing, in alternation, the passage of air flow. Thus, the air flow causes a series of short pulses of air, which increases the supraglottal pressure, and then, the suction phenomenon known as the Bernoulli effect is observed. This effect, due to the decrease of the pressure across the constriction aperture (i.e., the glottis), sucks the folds back together, and the subglottal pressure increases again, so that the vocal folds open giving rise to a new pulse of air [Sun87]. This phonation process has a fundamental frequency directly related to the frequency of the vibration of the vocal folds, as it will be explained below. The phonation from the larynx then enters the various chambers of the vocal tract: the pharynx, the nasal cavity and the oral cavity. The pharynx is the chamber stemming the length of the throat from the larynx to the



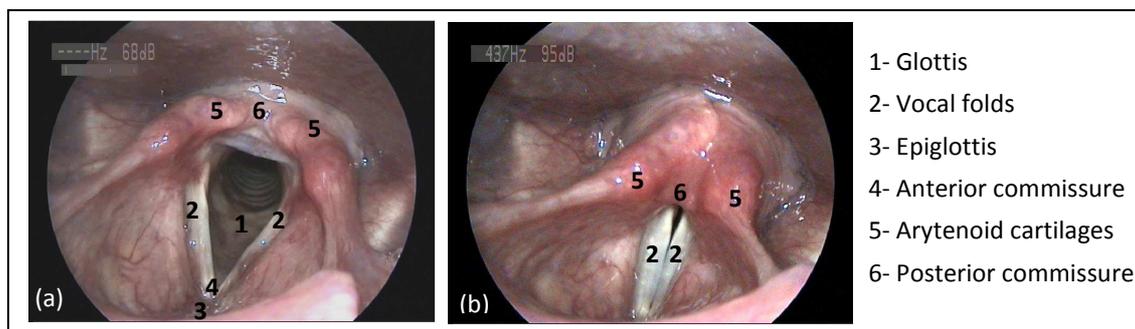
**Figure 2.1.** Human speech production mechanism (adapted from [Pul05]).

oral cavity. The position of the velum, a piece of tissue that makes up the back of the roof of the mouth, determines the access to the nasal cavity [Cin08]. For the production of certain phonemes, the velum can be raised or lowered to prevent or to allow acoustic coupling between the nasal and oral cavities. The tongue and lips, in combination with the lower jaw, are called the articulators and act to provide varying degrees of constriction at different locations, helping to change the “filter” and, therefore, the produced sound [Gol00].

Thus, according to this theory, the sustained vibration of the vocal folds is described as the balance between three aspects: the lung pressure, the Bernoulli principle and the elastic restoring force of the vocal fold tissue. However, according to recent studies, together with the Bernoulli forces, there must be also an asymmetrical driving force that is exerted on the folds and that changes with the direction of their velocity, supplying the vocal fold tissue with more energy – without which the vibrations would dissipate too readily. The Bernoulli force, along with the asymmetrical force at the glottis due to the mucosal wave as well as the closed and open phase of the folds, is now considered to be the sustaining model for vocal fold vibration [Mur08].

The vocal folds are the most important functional components of the voice organ, because they function as a generator of voiced sounds (explained below). They are covered by a

mucous membrane and the space between them is given the name of glottis, an end-point of which is found at the site of the Adam's Apple. Images of the human glottis are shown in Figure 2.2.



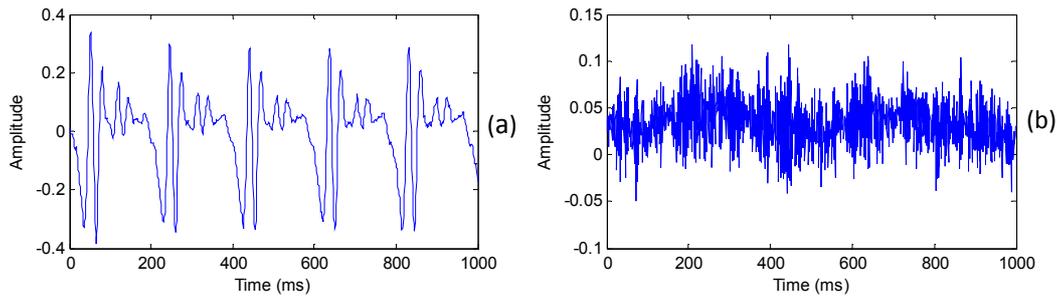
**Figure 2.2.** Top view of the larynx, showing the positions of the vocal folds.  
(a) – open vocal folds; (b) – closed vocal folds.

The length of the vocal folds varies: in a newborn it is approximately 3 mm, and increases to 9–13 mm and 15–20 mm in adult female and male, respectively [Sun87]. This length is what defines the frequency of vibration of the vocal folds, called the fundamental frequency (or pitch). Because frequency is inversely proportional to length, the values of the fundamental frequency of female voices are higher than those of male voices. For female voices, the values of the fundamental frequency are close to 220 Hz while for male voices are around 110 Hz [Per09]. So, when a tenor sings a note with a fundamental frequency of 330 Hz, this means that his vocal folds open and close 330 times per second.

Arytenoid cartilages control the movement of the vocal folds, separating them, in the case of breathing, and joining them and tightening them to produce a voiced sound emission. The action of the cartilage joining the vocal folds is known as adduction and the opposite action (i.e., separating the vocal folds) is abduction. It is the combination of adduction and abduction actions, when performed at certain frequencies, that cause the production of a sound wave and that is then propagated towards the lip opening.

The sounds produced as a result of the vibration of the vocal folds are called voiced sounds, and the sounds produced without vibration of the latter (the vocal folds remain open only and the glottal excitation is noisy) are referred to as unvoiced [Per09]. In Figure 2.3, one can see a voiced and an unvoiced segment of speech signals. These signals are better analysed in section 3.3, from the signal synthesis point of view.

The tube formed by the larynx, the pharynx, and the oral and nasal cavities, is called the vocal tract, so it can be defined as the space downstream the glottis that ends with the mouth cavity or the nostrils [Kob02]. The individual morphology determines its length but in adult males, the



**Figure 2.3.** Speech signals: (a) – voiced speech signal; (b) – unvoiced speech signal.

vocal tract length is about 17 – 20 cm and 3 cm of diameter. Children and adult females have shorter vocal tracts [Sun87].

It is known that the longer the vocal tract, the lower the formant frequencies. This knowledge is very useful to singers: if they want to sing a lower note, they have to increase the vocal tract, for example, projecting the lips or lowering the larynx.

When the vocal folds vibrate and form pressure pulses near the glottis (which, in turn, are propagated towards the vocal and nasal openings), the energy of the frequencies of the excitation is altered as these travel through the vocal tract [Gol00]. Consequently, the sound produced is shaped by the resonant cavities above the glottal source and, therefore, the vocal tract is responsible for changing acoustically the voice source.

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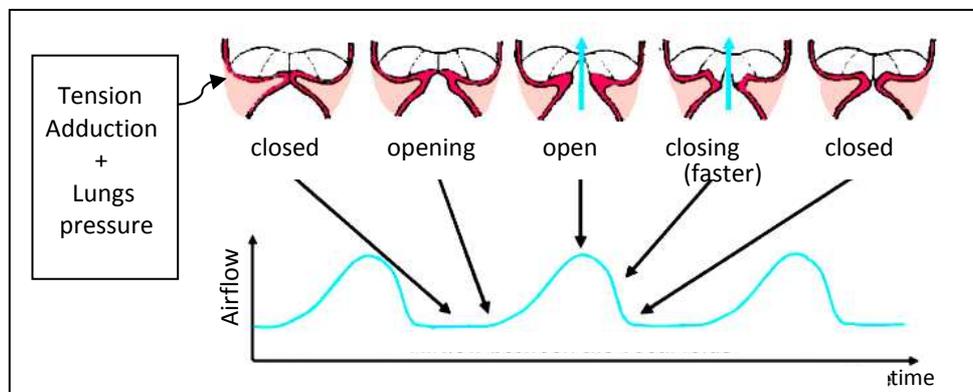
### 2.3. GLOTTAL FLOW

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According to the anatomy and physiology of speech production, the glottal flow is the airflow velocity waveform that comes out of the glottis and enters the vocal tract, also called the glottal source. The shape of the glottal source waveform in a single period is denoted by glottal pulse. It should be noted that it is very common to find in several research texts the use of the terms glottal flow, glottal source and glottal pulse interchangeably. However, Murphy [Mur08] states that the glottal flow and the glottal pulse represent the airflow that passes through the glottis and that the glottal source is the glottal pressure wave or, in some cases, the glottal aperture, i.e., the derivative of the glottal pulse.

Nevertheless, in this dissertation we will use the most common definitions, considering that they do not compromise the understanding and development of a rigorous study.

As the vocal folds open and close the glottis at identical intervals, the frequency of the sound generated is equal to the frequency of vibration of the vocal folds [Sun87]. Each cycle consists of four glottal phases, as it can be seen in Figure 2.4: closed, opening, opened and closing (or return).



**Figure 2.4.** Glottal phases (adapted from [San09]).

Typically, when the folds are in a closed position, the flow begins slowly, builds up to a maximum, and then quickly decreases to zero when the vocal folds abruptly shut [Kaf08]. However, studies have indicated that total closure of the glottis is an idealistic assumption and that the majority of the individuals exhibit some sort of glottal leakage during the assumed closed phase [Cin08]. Still, most of the glottal models (chapter 4) assume that the source has zero flow during the closed phase of the glottal cycle.

The time interval during which the vocal folds are closed and no flow occurs is referred to as the glottal closed phase. The next phase, during which there is nonzero flow and up to the maximum of the airflow velocity is called the glottal opening phase, and the time interval from the maximum to the time of glottal closure is referred to as the closing or return phase.

Many factors can influence the rate at which the vocal folds oscillate through a closed, open and return cycle, such as the vocal folds muscle tension, the vocal fold mass and the air pressure below the glottis [Kaf08].

Due to the location of the larynx, the glottal flow cannot be measured directly, but there are some medical procedures that allow the observation of the larynx and the vocal fold vibration. These techniques can be divided into two categories. First, electrical and electromagnetical glottography extract specific features of the vocal fold vibration related to the changing electrical properties of the human tissue. Second, imaging techniques are based on visual analysis of larynx by observing the vocal folds using a mirror [Air08b].

Glottal inverse filtering, which will be explored in chapter 4, is also a technique used to estimate the airflow through the glottis without requiring any medical procedure and using only computational procedures.

### 2.3.1. ELECTROGLOTTOGRAPHY

Electroglottography (EGG), a very common technique used both in voice research and clinical work, is a non-invasive method for examination of the vocal fold vibration [Air08b]. However, EGG involves contact with the skin and even physical pressure, and some specialists consider this to be an invasive technique.

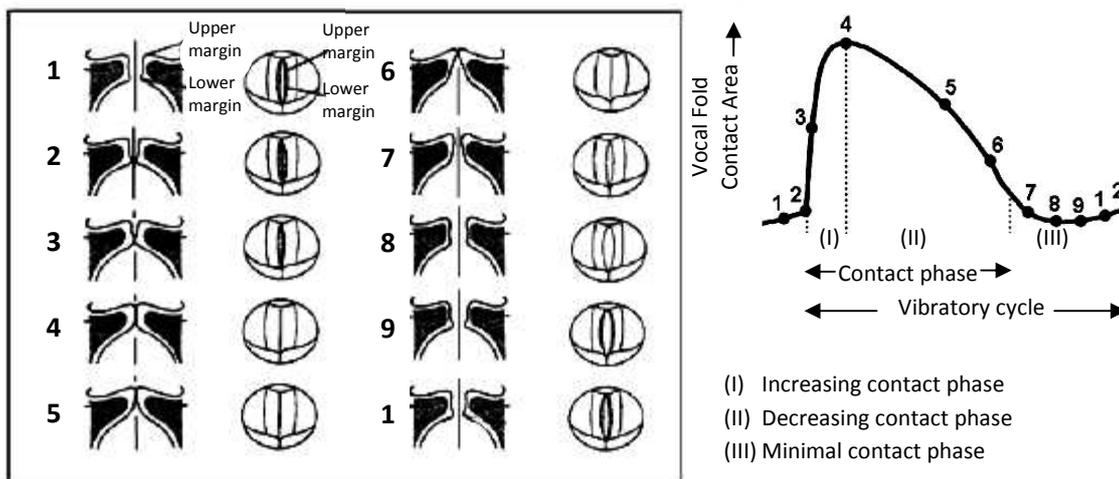
EGG is based on the fact that human tissues are conductors of electric current [Hen09], giving a variable resistance to electric current, whereas air is a particularly poor conductor. It measures the contact area of the vocal folds by placing one electrode on each side of the thyroid cartilage, as it can be seen in Figure 2.5.



**Figure 2.5.** *EGG measurement setting. Electrodes have been placed on the subject's skin and a band has been adjusted around the neck to hold the electrodes in place. The electroglottograph (Glottal Enterprises MC2-1) is on the right on top of the oscilloscope [Pul05].*

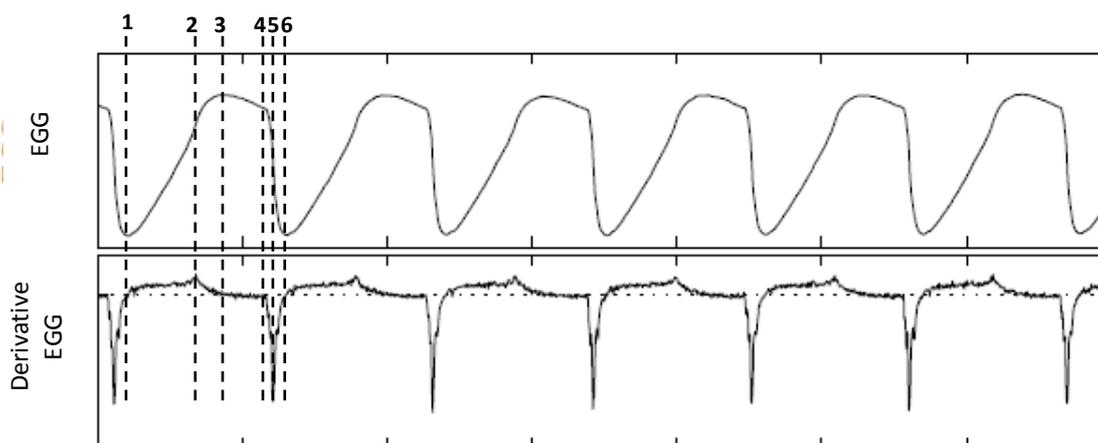
The conductivity of the vocal fold tissue is larger than that of the air within the laryngeal cavity and the glottis, which makes that the impedance between the electrodes varies in step with the vocal fold vibration [Air08b]. A high-pass filter (with cut-off frequency between 5 and 40 Hz) removes the low frequency noise components, mainly due to the movement of the larynx during phonation, the blood flow in arteries and veins of the neck, and the contractions of laryngeal muscles [Hen01].

The resulting electroglottographic signal, the electroglottogram, allows to analyse the vocal folds movement and to identify the glottal phases (see Figure 2.6).



**Figure 2.6.** Schematic representation of a single cycle of vocal fold vibration (left figure) viewed coronally (left) and superiorly (right), and an EGG of a normal phonation (right figure). The numbered points on the trace correspond approximately to the points of the cycle depicted on the right (adapted from [Ken04]).

Figure 2.7 shows an example of an electroglottogram from a male subject during normal phonation, where the glottal phases can be observed.



**Figure 2.7.** Electroglottogram of a normal phonation of a male subject. The upper panel shows the EGG signal and the lower panel its first derivative. Upward change in the signal represents increasing impedance and thus reduced contact between the vocal folds (adapted from [Pul05]).  
 Glottal phases:  
 1 – 3: opening phase; 3 – 4: open phase; 4 – 6: closing phase; 6 – 1: closed phase

In the opening phase (1-3), the vocal folds are separating from lower margins towards upper margins and then upper margins start opening. Then the open phase (3-4) begins, where the vocal folds are maximally opened. The closing phase (4-6) follows, where the vocal folds are closing from lower margins towards upper margins. Finally, the closed phase (6-1) takes place, where the vocal folds are fully closed.

Despite its relative simplicity, the EGG allows the investigation of the vocal fold vibration during phonation and a measurement of the glottal activity, independently of the supraglottic system. However, many authors argue that the EGG signal does not allow an exact determination of the instants of closure and glottal opening, and some prefer to analyse the derivative of the signal EGG [Pul05]. This signal is often studied because it allows to visualize the changes in the tilt of the signal: if the derivative is negative in a given instant, it means that the EGG signal is decreasing at that instant, which corresponds to the closing phase; if the derivative is positive, then the EGG signal is increasing, which denotes the opening phase; otherwise, the derivative is equal to zero, meaning either the open phase (maximum) or the closed phase.

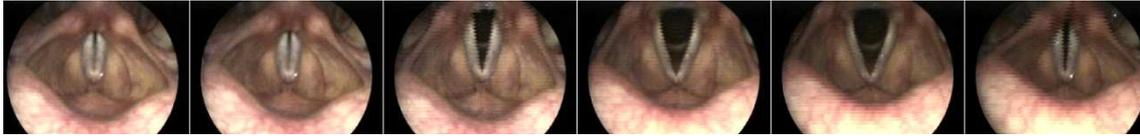
Nathalie Henrich [Hen01] regarded the peaks of the derivative of the EGG signal as reliable indicators of glottal opening and closing instants defined by reference to the glottal air flow. But this kind of approach is unreliable because often such peaks are imprecise or absent, or double peaks may occur [Pul05]. Also, the EGG signals denote the area of contact of the vocal folds and thus do not represent directly the glottal airflow pulse shape.

### 2.3.2. IMAGING TECHNIQUES

Video laryngoscopy (Figure 2.8) consists of a video camera attached to a laryngoscope so that images (Figure 2.9) and sounds of the larynx and vocal folds can be simultaneously recorded and later analysed [Gui08].



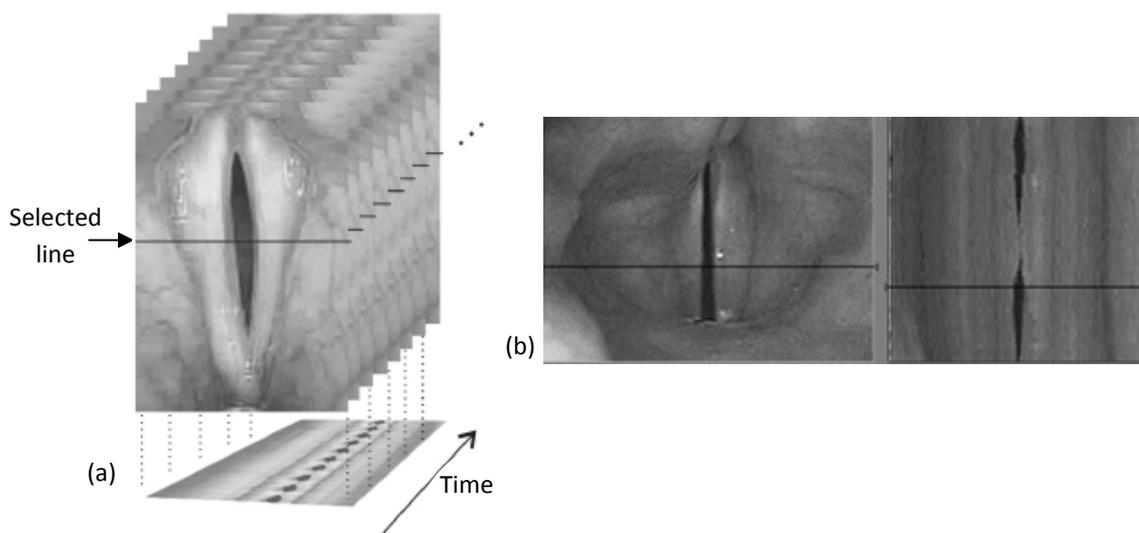
**Figure 2.8.** *Video laryngoscopy.*



**Figure 2.9.** Sequence of vocal folds images captured during a video laryngoscopy examination.

From this technique a test, called kimography, can be performed that makes a quantitative analysis of the vocal fold vibration, by joining a sequence of lines obtained from the captured video frames. This is illustrated in Figure 2.10.

The examination of the kimography allows to measure the duration of each phase of the glottal cycle and the opening amplitude of the glottis.



**Figure 2.10.** kimography.

- (a) The image from video laryngoscopy, the selected line for analysis and its projected kimography [Gui08].
- (b) A video fragment and its image on the kimography.  
(Image from <http://www.diagnova.pl/en/index.php/offer/products/video-recording/>)

Videostroboscopy (Figure 2.11) is other procedure used to assess the structure and movement of the vocal folds. It uses a video camera attached to a stroboscopic light source, which illuminates the vocal folds quasi-synchronized with vocal fold vibration to provide what appears to be a slow-motion view of vocal fold movement and vibration [Gui08].

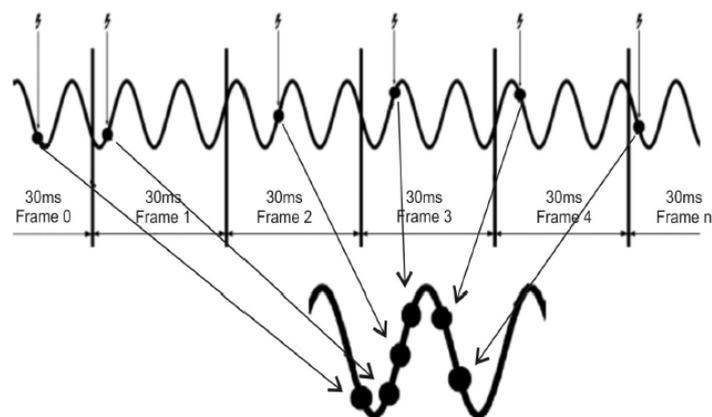


**Figure 2.11.** Videostroboscopy

(Image from <http://www.uwec.edu/Maps/bldgtour/hss/index.htm>)

Illustration of the fundamental principle of videostroboscopy is shown in Figure 2.12.

By enabling the vocal folds to be viewed both in slow motion and at standstill, assessment of amplitude and glottic closure is enhanced using the videostroboscopy procedure [WB87].



**Figure 2.12.** Fundamental principle of videostroboscopy.

Flashes of light are fired one time each frame of video at a given moment (above). The images captured from each frame are combined to create an artificial cycle (below) [Gui08].

Despite the fact that these techniques allow the analysis of the glottal source, they can interfere with normal phonation behaviour. Also, the logistic requirements of these techniques (equipment and health professionals for video laryngoscopy and videostroboscopy), the invasive nature of the procedures and the time required make these techniques not practical and, therefore, unattractive for the estimation of the glottal source.

The estimation of the glottal pulse directly from the speech signal seems to be much more attractive, due to the relative simplicity and non-invasiveness of the process, which explains, somehow, the numerous studies done in this area in recent decades.

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## **2.4. SUMMARY**

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In this chapter an overview is given of the anatomy and physiology of the voice organ, and the human speech production process.

Also, the four phases of the glottal cycle are presented as well as different medical procedures that allow the observation of the larynx and the vocal fold vibration. In general, these procedures are uncomfortable for the speaker and interfere with normal phonation behaviour, which makes more attractive and motivates the development of techniques that estimate the glottal pulse directly from the speech signal.

# Chapter 3

## MODELS OF VOICE PRODUCTION

### Contents

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### 3.1. INTRODUCTION

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Any sound, given the physical nature of sound waves, requires an energy source, an oscillator and a medium to travel through. In the human body system, these are represented by the lungs, the vocal folds and the vocal tract, respectively. From the action of the lungs, the vocal folds vibrate as an oscillating force and, together with the resonant cavities of the vocal tract, mouth and nose, this force creates the sound waves required for voice [Mur08]. Thus, this is the basis of any model of voice production, as the source-filter model, that will be presented and analysed in this chapter. Also, different methods of extraction of characteristics from speech signals and glottal waveform models are described and their respective mathematical details are presented.

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### 3.2. SOURCE-FILTER MODEL

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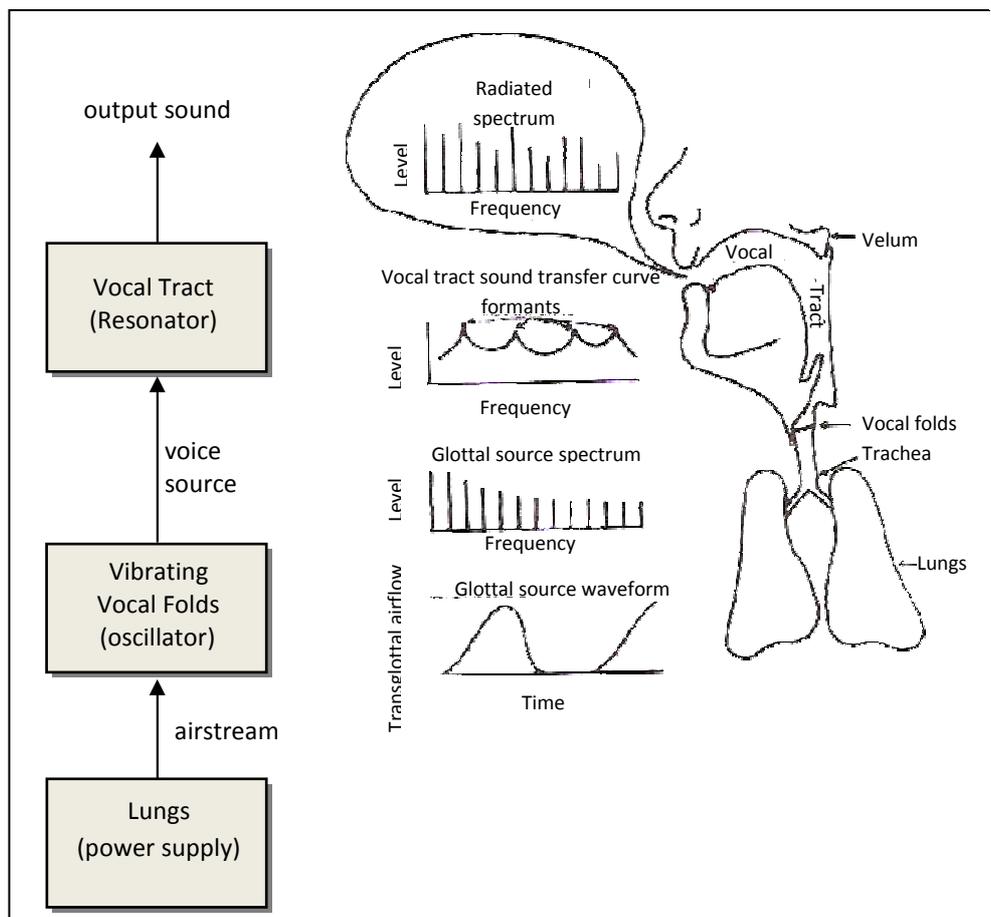
The voice organ, as a generator of sounds, has three major units: a power supply (the lungs), an oscillator (the vocal folds) and a resonator (the vocal tract) [Sun77].

As it was explained in the previous chapter, when the vocal folds are closed and an airstream arises from the lungs, the pressure below the glottis forces the vocal folds apart: the air passing between the folds generates a Bernoulli force that, along with the mechanical properties of the folds (and the asymmetrical force), almost immediately closes the glottis. The pressure differential builds up again, forcing the vocal folds apart again. This cycle of opening and closing the glottis feeds a train of air pulses into the vocal tract and produces a rapidly oscillating air pressure in the vocal tract: in other words, a sound [Sun77]. During this process, an entire family of *spectrum* tones is generated, called partials, where the lowest tone is known as the fundamental and the others as overtones.

The vocal tract has four or five important resonances, called formants, that shape the initial sound wave, setting frequency amplitudes and formant features, which define the quality and vowel type when the wave is perceived audibly [Mur08].

The glottal source spectrum is filtered by the vocal tract and since the partials have different frequencies, the vocal tract treats them in different ways: the partials closest to a formant

frequency reach higher amplitudes than neighbouring partials [Sun87]. This is illustrated in Figure 3.1.



**Figure 3.1.** Schematic illustration of the generation of voice sounds (adapted from [Sun77], [Sun87]).

Many models for voice production system are based on Fant's source-filter theory: the voice is the result of the convolution between the excitation source and the filter system, i.e., the source represents the air flow at the vocal folds and the filter represents the resonances of the vocal tract which change over time [Fan60]. For voiced speech, the excitation is a periodic series of pulses, whereas for unvoiced speech, the excitation has the properties for random noise [Kaf10]. Thus, the source is the creation of the puffs of air at the glottis (glottal pulses) generating the sound wave (glottal source), which propagates through the vocal tract, and that is then filtered by varying shapes and cavities encountered therein and radiated by the lips [Mur08]. This model is, then, a simplification of the intricate relationship between the glottal source, the vocal tract and the lip/nostrils radiation, usually simply referred as lip radiation. Figure 3.2 illustrates this simple model.



**Figure 3.2.** Block diagram of the source-filter model.

This model has two strong assumptions:

1. the source and the filter are separated and independent systems ;
2. in time domain, voice production can be represented by means of a convolution of its elements (i.e., the glottal source, the vocal tract filter and lip radiation) [Deg10].

The first assumption implies that the glottal source is equal to the glottal flow, which in reality, is not perfectly valid, because a source-tract interaction exists and the glottal flow is actually dependent in some degree of the variations of the vocal tract impedance. Yet, the source-filter model has been used in this dissertation, since the underlying assumptions can be considered sufficient for most cases of interest which explains for example that it is widely used in speech processing systems [Pul05].

This model is a simplification of the physiology and acoustic model of voice production and the scheme in Figure 3.3 emphasizes the links between these elements. According to Gilles Degottex ([Deg10]), the author of the scheme, the articulators are in blue, the passive structures are in grey and the glottis, which is acoustically active, is in orange like the vocal folds.

On the left of Figure 3.3 is a synthesis of the physiology of the voice production system, described in the previous chapter.

In the center, an acoustical model is presented, in which the impedance of the vocal apparatus is represented by area sections and their physical properties all along the structures. The impedance of the larynx is mainly defined by the glottal area, which is an implicit variable influenced by the imposed mechanical properties of the vocal folds [Deg10].

On the right of Figure 3.3, the source-filter model is depicted: the speech signal is the result of a glottal flow filtered by the vocal tract cavities and radiated by the lips and nostrils.

The source-filter model is, as it was explained, a simplification of the discrete-time model of speech production, represented in Figure 3.4.

The mathematical framework of the classic source-filter model of speech production model can be expressed as follows:

$$s[n] = g[n] * v[n] * l[n] \quad (1)$$

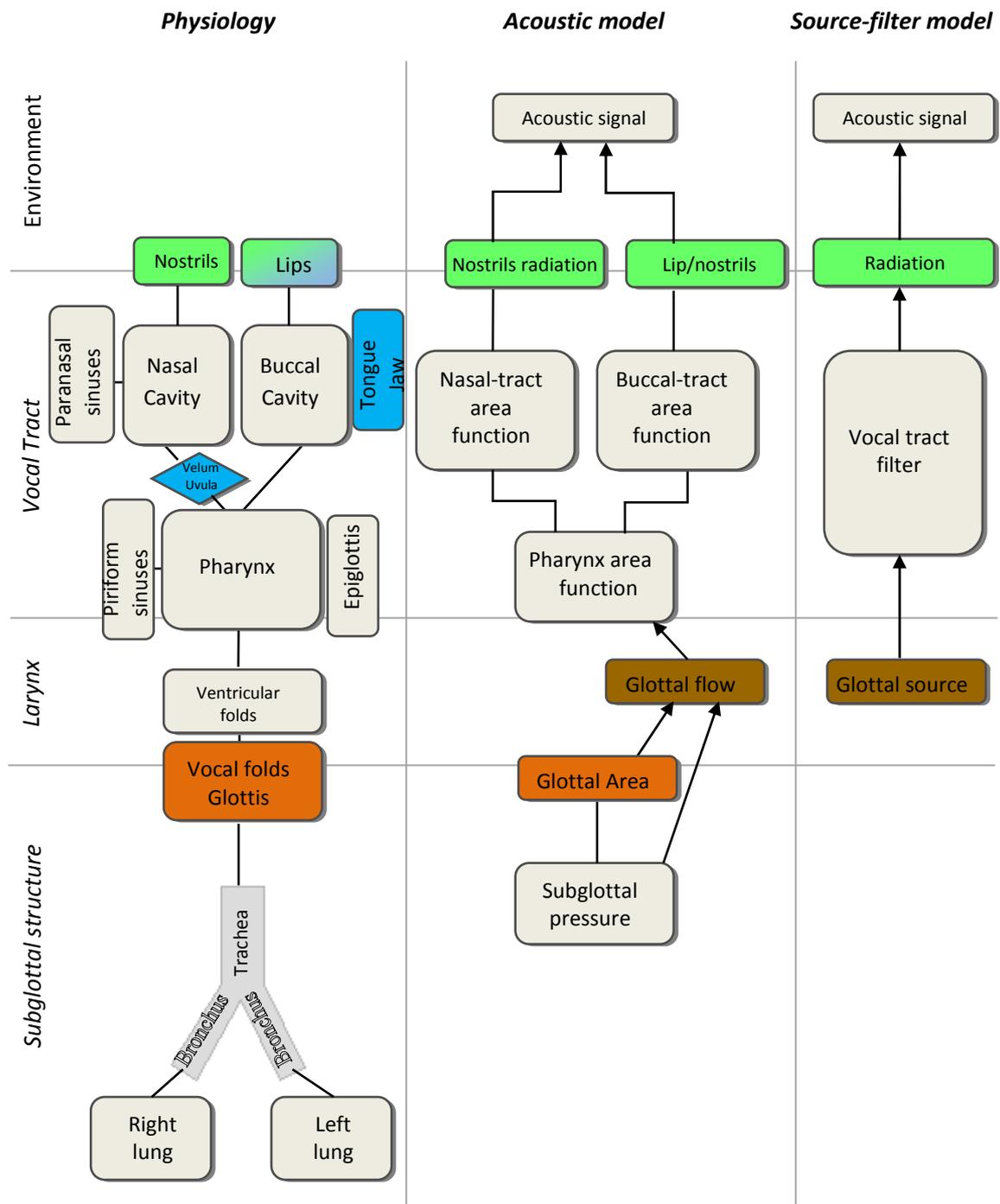
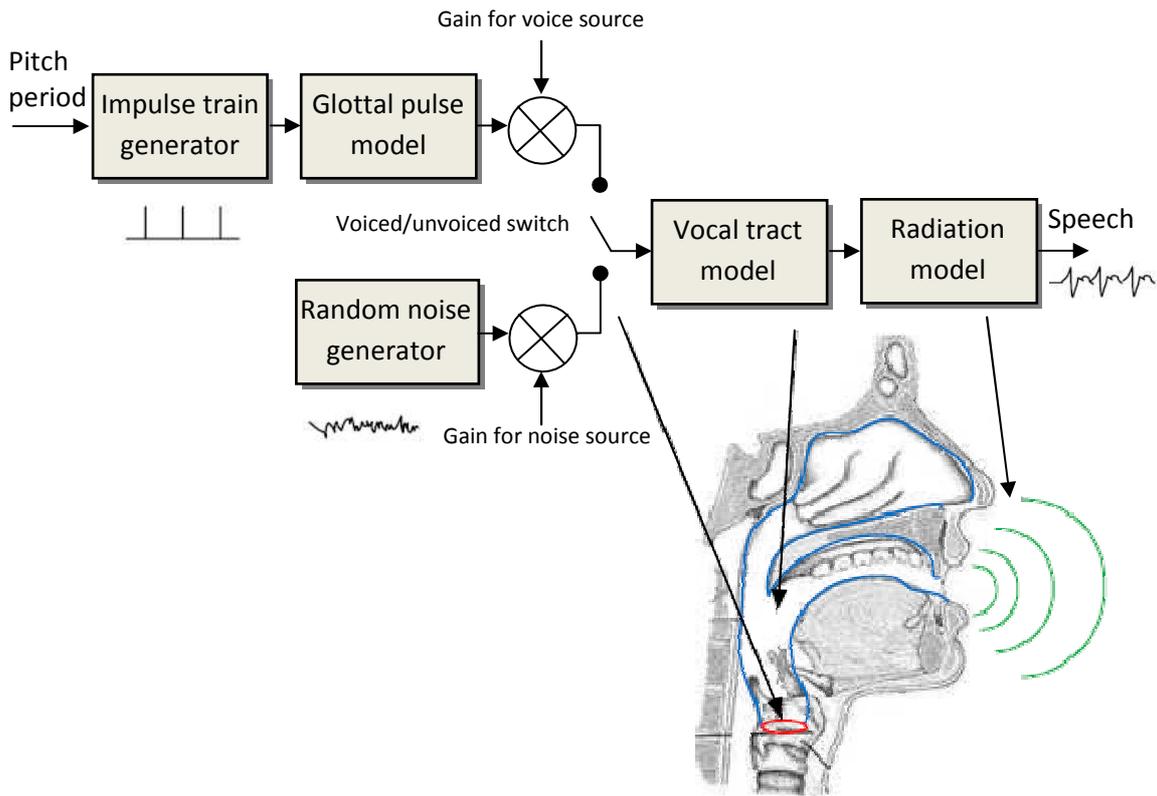
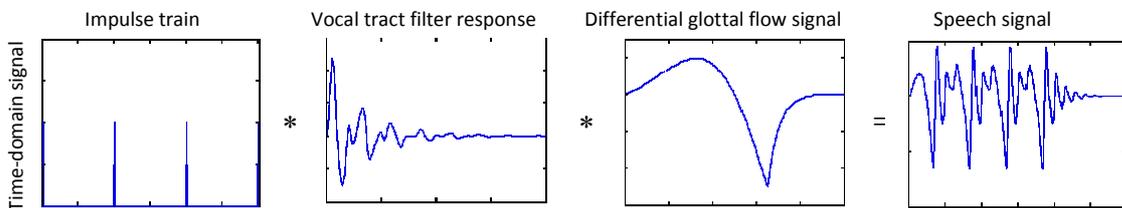


Figure 3.3. Schematic view of voice production models [Deg10].

where  $s[n]$  is the output signal, i.e., the speech signal,  $g[n]$  is the excitation source signal,  $v[n]$  is the impulse response of the vocal tract and  $l[n]$  is the lip/nostrils radiation. This is illustrated in Figure 3.5.



**Figure 3.4.** General discrete-time model of speech production and its physiologic correspondence (adapted from [HAH01] and [Gol00]).



**Figure 3.5.** Source-filter model: the speech signal as a result of the convolution between the excitation source signal, the impulse response of the vocal tract and the lip/nostrils radiation.

In Z-domain, equation (1) can be written as:

$$S(z) = G(z)V(z)L(z) \tag{2}$$

where  $G(z)$  is the Z transform of the acoustic excitation at the glottis level. The resonances and anti-resonances of the vocal tract are combined into a single filter  $V(z)$ , termed Vocal Tract Filter (VTF) and the lip and nostrils radiation are combined into a single filter  $L(z)$ , termed radiation. Therefore, the glottal inverse filtering requires solving the equation:

$$G(z) = \frac{S(z)}{V(z)L(z)} \tag{3}$$

that is, to determine the glottal waveform, the influence of the vocal tract and the lip/nostrils radiation must be removed. In the case of a voiced speech signal, the glottal waveform presents a typical periodic shape as previously shown in Figure 2.4.

Usually, the VTF is modelled as an  $p$ -order all-pole filter:

$$V(z) = \frac{1}{1 - \sum_{i=1}^p b_i z^{-i}} \quad (4)$$

where the poles correspond to resonances of the vocal tract filter and, therefore, to the formant frequencies of the vocal tract [Mur08].

The lip/nostrils radiation imposes a high pass filter approximated by a first order time-domain derivative [Mur08], meaning that the derivative of the glottal flow is the effective excitation of the vocal tract. Therefore:

$$L(z) = 1 - \alpha z^{-1} \quad (5)$$

where  $\alpha$  is the lip/nostrils radiation coefficient, which value is close to (but less than) 1 [JBM87]. Usually,  $\alpha$  is a value between 0.95 and 0.99 in order that the zero lies inside the unit circle in the  $z$  plane.

This equation can be written as [JBM87]:

$$L(z) \approx \frac{1}{\sum_{k=0}^N \alpha^k \cdot z^{-k}} \quad (6)$$

where  $N$  is theoretically infinite but in practice finite because  $\alpha < 1$ . This result suggests that the effect of a zero may be approximated by a sufficiently large number of poles.

Although in the literature, most often, these three processing stages are implemented in the discrete-time domain, the spectral approach to voice source modelling has a number of advantages, as it will be discussed in this dissertation.

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### 3.3. EXTRACTION OF CHARACTERISTICS FROM A SPEECH SIGNAL

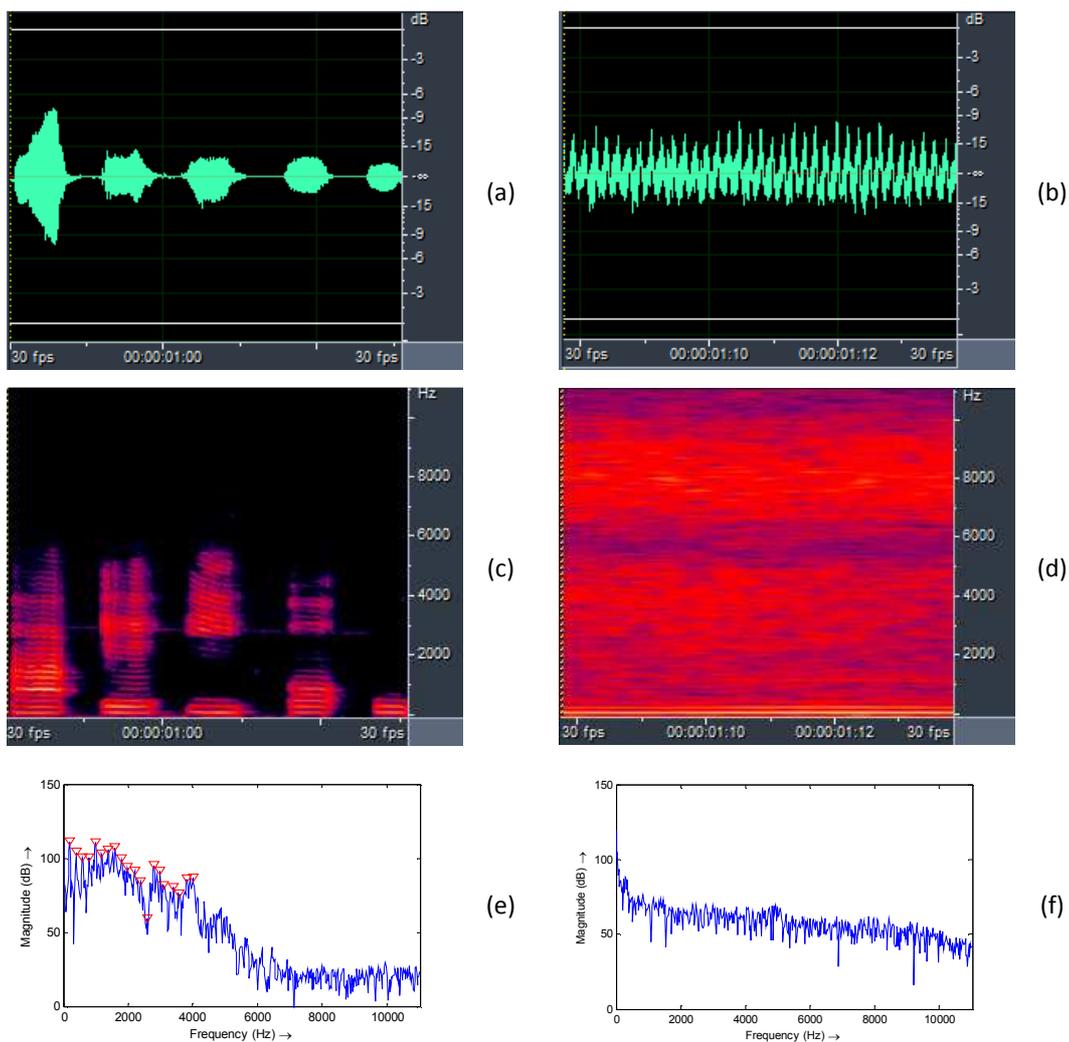
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Speech signals can be classified into voiced and unvoiced. This classification is fundamental in signal analysis, since each type has a different kind of excitation in the synthesis of the signal.

Voiced speech signals are those that are generated as a result of the vibration of vocal folds, for example, all the vowels that we pronounce. These signals have an important feature: a well defined periodicity.

Unvoiced speech signals, such as “s”, “p”, “z” or “ch”, are generated by the passage of air at high speed through the vocal tract while the glottis is partially open. These kind of signals have almost no periodicity.

Figure 3.6 shows the speech analysis of voiced and unvoiced speech signals. Plots (a) and (b) illustrate the corresponding speech waveforms, the plots below, (c) and (d), illustrate the corresponding spectrograms, i.e., a time-varying spectral representation of the energy distribution reflecting to the resonances of the vocal tract, and plots (e) and (f), the corresponding magnitude spectra.



**Figure 3.6.** Illustrations of speech sounds.

(a): the speech waveform of the voiced sound of the vowels “a e i o u”, uttered by a female subject; (c): the corresponding spectrogram; (e): the magnitude spectrum pertaining to a segment of vowel /a/ where the harmonics are depicted;  
 (b): the speech waveform of the unvoiced sound “z”; (d): the corresponding spectrogram; (f): the magnitude spectrum pertaining to a short segment of that unvoiced sound.

From these illustrations it is possible to observe that the unvoiced speech signal (plot (b)) is characterized by a non-periodic nature and its spectrum (plot (d)) has more energy in the high frequency region. On the other hand, the spectrum of the voiced speech signal (plot(c)) has more energy in low frequency region.

Speech signals are non stationary signals, i.e., over time their main attributes and, in particular, their waveform, are constantly being changed. The mathematical tools used in signal processing typically require that these signals remain time invariant so that its characteristics can be conveniently analysed. If a speech signal is divided into short enough segments (approximately between 10 and 30 ms), these "new" signals of short duration can be considered almost stationary since, throughout this duration, the phonatory articulators movements are sufficiently reduced and slow. Thus, the transfer function associated to the vocal tract shape remains fixed (or nearly fixed) and the acoustic characteristics of the "new" signal can be considered virtually time invariant.

Therefore, in order to extract features from a voice signal it is first necessary to perform a segmentation of the signal into segments of sufficiently short duration. This segmentation is achieved by applying a sliding window (e.g., Hanning, Hamming, Sine or Blackman<sup>3</sup>) to the complete voice signal, i.e., the segmentation of the speech signal is made by multiplying the window with the voice segment. Each one of these segments is called a frame and can be expressed as:

$$x_m[n] = x[n]w_m[n] \quad (7)$$

where  $x[n]$  is the speech signal and  $w_m[n]$  is the window function, which is zero everywhere except in a small region.

The short-time Fourier (DTFT) representation for frame  $m$  is defined as:

$$X_m(e^{j\omega}) = \sum_{n=-\infty}^{+\infty} x_m[n]e^{-j\omega n} = \sum_{n=-\infty}^{+\infty} w_m[n]x[n]e^{-j\omega n}. \quad (8)$$

There are several methods to extract features from a voice signal, and some will be analysed: Linear Predictive Coding (LPC), Mel-Frequency Cepstral Coefficients (MFCC) and Discrete All-Pole Modelling (DAP).

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<sup>3</sup> See mathematical details in the Appendix A.

### 3.3.1. LINEAR PREDICTIVE CODING (LPC) METHOD

Linear Predictive Coding (LPC) is a mathematical technique introduced in the sixties that may be applied to time series data and was used, primarily, as a direct proposal to modelling the voice spectral envelope in digital form [Mur08]. Given a speech signal, LPC assumes that a current sample can be determined by a weighted linear combination of a certain number of past previous samples. This method is widely used because it is fast and simple, and effective ways exist of estimating the main parameters, or coefficients, of the prediction filter [HAH01].

The most common representation of linear prediction (LP) is:

$$y[n] = \sum_{i=1}^N a_i x[n-i] \quad (9)$$

where  $y[n]$  is the linear prediction of a signal  $x[n]$ , and  $a_i$ , for  $i=1$  to  $N$ , are the prediction coefficients.  $N$  is the predictor order, which is usually in the range of 8 to 14, with 10 being the most common for coding applications. The choice of the prediction order determines the number of poles that result in the designed filter and is essentially determined by the sampling rate. Equation (9) is sometimes referred to as an autoregressive (AR) model. The difference between the actual sample and the predicted sample is called the residual error or the prediction error, and is given as:

$$e[n] = x[n] - y[n] \quad (10)$$

and from equation (9), one obtains:

$$e[n] = x[n] - y[n] = x[n] - \sum_{i=1}^N a_i x[n-i]. \quad (11)$$

The aim of LPC analysis is getting the most suited coefficients such that the residue is as small as possible. Their estimation is termed linear predictive analysis, and the most common choice for the optimization of these coefficients is the criterion of minimizing the square error function given by:

$$E = \sum_{n=0}^{L-1} [e[n]]^2 = \sum_{n=0}^{L-1} \left[ x[n] - \sum_{i=1}^N a_i x[n-i] \right]^2. \quad (12)$$

This function can be minimized by imposing:

$$\frac{\partial E}{\partial a_i} = 0, \quad i=1, \dots, N. \quad (13)$$

From this equation, one obtains:

$$2 \sum_{n=0}^{L-1} \left[ e[n] \cdot \frac{\partial e[n]}{\partial a_i} \right] = 0 \Leftrightarrow \quad (14)$$

$$\Leftrightarrow 2 \sum_{n=0}^{L-1} \left[ e[n] \cdot (-x[n-i]) \right] = 0 \quad (15)$$

$$\Leftrightarrow -2 \sum_{n=0}^{L-1} \left[ x[n] - \sum_{k=1}^N a_k x[n-k] \right] x[n-i] = 0 \quad (16)$$

$$\Leftrightarrow -2 \left( \sum_{n=0}^{L-1} [x[n] \cdot x[n-i]] - \sum_{n=0}^{L-1} \sum_{k=1}^N a_k x[n-k] \cdot x[n-i] \right) = 0 \quad (17)$$

$$\Leftrightarrow \sum_{k=1}^N a_k \sum_{n=0}^{L-1} x[n-k] \cdot x[n-i] = \sum_{n=0}^{L-1} x[n] \cdot x[n-i]. \quad (18)$$

This last equation leads to the normal equations for linear prediction [Cin08].

Thus, the result of LPC analysis is a set of coefficients  $a_i$ , for  $i=1$  to  $N$ , that can be computed using the autocorrelation or covariance methods [Cin08], and the error signal  $e[n]$ , which is as small as possible in the least squares sense, represents the difference between the predicted signal and the original signal.

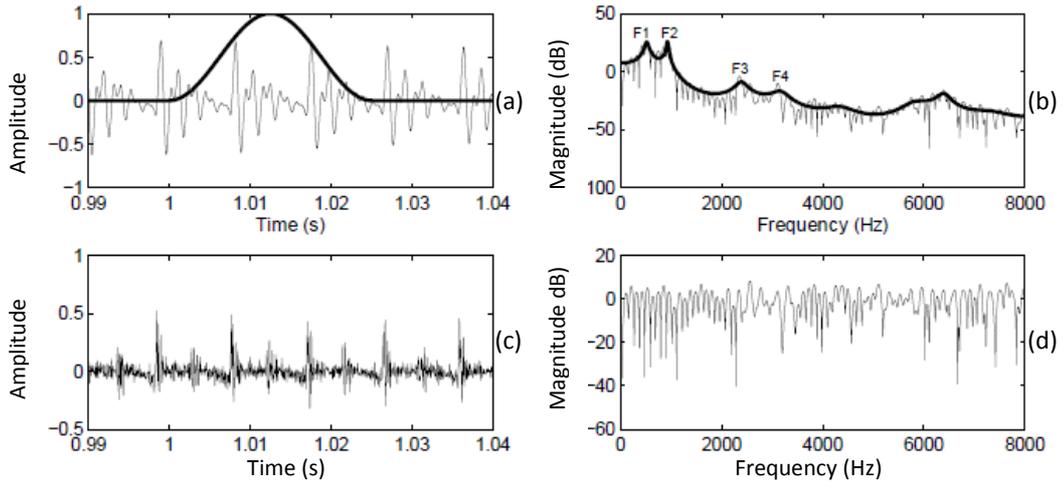
Figure 3.7 illustrates the LPC method: after windowing the segment of the speech signal, shown in plot (a), from a spectral standpoint, linear prediction attempts to match the power spectrum of the signal  $x[n]$  to the predicted filter given by the coefficients  $a_i$ , as it is observed in plot (b), where it is also possible to identify some vocal tract resonances, i.e., the formants, denoted F1 to F4. By inverse filtering, the LPC residual is obtained, displayed in plot (c), and then the amplitude spectrum of the residual signal, represented in plot (d). In this last plot, it is possible to observe that the amplitude spectrum is almost flat, which denotes that the effects of the vocal tract resonances have been removed [Dru11].

In Z-Transform domain, equation (11) is equivalent to:

$$E(z) = X(z) \left[ 1 - \sum_{i=1}^N a_i z^{-i} \right] = X(z) A(z) \quad (19)$$

where  $A(z)$  is the Z-Transform model of the 'whitening' filter,  $E(z)$  is the Z-Transform of the prediction error and  $X(z)$  is the Z-Transform of the speech signal.

Usually,  $A(z)$  is referred to as the LPC analysis filter and  $\frac{1}{A(z)}$ , an all-pole filter, as the synthesis filter.



**Figure 3.7.** Illustration of the LPC method. (a): the speech signal (thin line) and the applied window (solid line); (b): the magnitude spectrum (thin line) and the corresponding LPC spectral envelope (solid line), where the four first formants (F1 to F4) are depicted; (c): the LPC residual obtained by inverse filtering; (d): the magnitude spectrum of the residual signal [Dru11].

Defining the power spectrum  $P(\omega)$  of the signal  $x[n]$  as

$$P(\omega) = |X(e^{j\omega})|^2 \quad (20)$$

then, from equation (19), one has:

$$P(\omega) = \frac{|E(e^{j\omega})|^2}{|A(e^{j\omega})|^2}. \quad (21)$$

If the prediction filter is effective, the prediction error is white noise, which means its power spectral density is flat. As a consequence, the signal spectrum  $P(\omega)$  is approximated by the all-pole model spectrum  $\tilde{P}(\omega)$  of the estimated filter. Assuming that the noise is white, then  $|E(z)|^2 = \sigma^2$  and

$$\tilde{P}(\omega) = \frac{\sigma^2}{|A(e^{j\omega})|^2} \quad (22)$$

where  $\sigma^2$  is the error energy. From equations (21) and (22), one can conclude that the more “flat” the residual power spectrum is, the better approximation is obtained ( $|E(e^{j\omega})|^2 \approx \sigma^2$ ).

Defining the total error as the infinite sum

$$\varepsilon(a) = \sum_{n=-\infty}^{+\infty} e_n(a)^2 = \frac{1}{2\pi} \int_{-\pi}^{\pi} |E(e^{j\omega})|^2 d\omega \quad (23)$$

where  $e_n$  is the prediction error, given by equation (10), and combining equations (21) and (22), equation (23) reduces to:

$$\varepsilon(a) = \frac{1}{2\pi} \int_{-\pi}^{\pi} |E(e^{j\omega})|^2 d\omega = \frac{1}{2\pi} \int_{-\pi}^{\pi} P(\omega) |A(e^{j\omega})|^2 d\omega = \frac{\sigma^2}{2\pi} \int_{-\pi}^{\pi} \frac{P(\omega)}{\hat{P}(\omega)} d\omega. \quad (24)$$

Analysing equation (24), one can conclude that, if a small region of the spectrum is considered, the error can be minimized and a better fit is obtained when  $\hat{P}(\omega) > P(\omega)$ , because  $P(\omega) / \hat{P}(\omega)$  is small [Mag05].

One disadvantage of this method is that for discrete spectrum, the LPC error measure possesses an error cancelation property, which means that the contributions to the error when  $\hat{P}(\omega) > P(\omega)$  cancel those when  $\hat{P}(\omega) < P(\omega)$ . Thus, an envelope can be selected rather the only one which passes through all the spectral points [JM91]. Also, the optimal order is difficult to determine and the iterative procedure is rather slow [Dru11].

The LPC model has other limitations as: it assumes an all-pole spectrum, it is naturally adapted to accurately model resonances (or pole effects) rather than anti-resonances (or zero effects). However nasalized vowels, involving the lowering of the velum within the vocal tract and the radiation of speech sounds through the nose, can create zeros in the spectrum [Mur08]. On the other hand, consonants produced with a continuous airflow through a vocal tract constriction, called fricative sounds, also introduce anti-resonances into the spectrum. Another disadvantage of this procedure is that LPC is especially problematic for high pitched harmonic sounds [Dru11]. In this case, the 'harmonic locking effect' effect is typically observed because pole locations are tied to the frequency of the harmonics of voiced speech signal.

### 3.3.2. DISCRETE ALL-POLE MODELLING (DAP)

In 1991, El-Jaroudi and Makhoul [JM91] proposed a new method for parametric modelling of spectral envelopes, called the Discrete All-Pole (DAP) modelling. The main purpose of the DAP method is to fit the all-pole model using only the finite set of spectral locations that are related to the harmonic positions of the fundamental. Figure 3.8 shows an example of a spectral envelope given by DAP and LP.

This method uses the discrete Itakura-Saito error measure and the optimization criterion is derived in the frequency domain.

The Itakura-Saito error measure is given by [JM91]:

$$E_{IS} = \frac{1}{N} \sum_{m=1}^N \left[ \frac{P(\omega_m)}{\hat{P}(\omega_m)} - \ln \frac{P(\omega_m)}{\hat{P}(\omega_m)} - 1 \right] \quad (25)$$

where  $P(\omega_m)$  and  $\hat{P}(\omega_m)$  are the given discrete spectrum and the all-pole spectrum, respectively, defined at  $N$  frequency points. This error reaches the minimum only when model spectrum coincide on all discrete points.

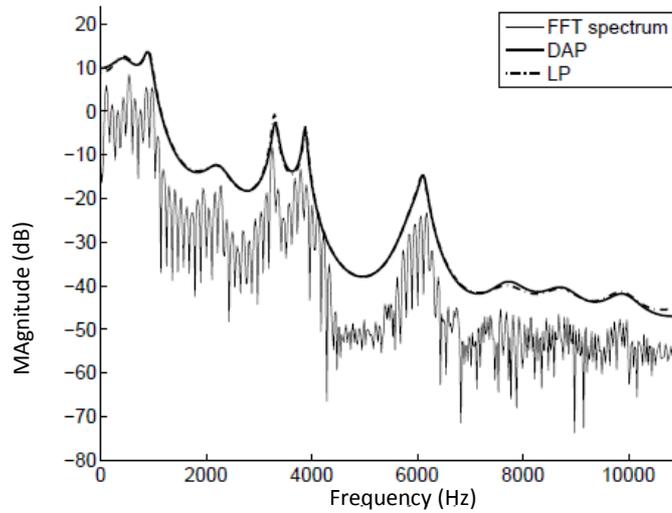
According to El-Jaroudi and Makhoul [JM91], the minimum error is obtained when

$$\frac{1}{N} \sum_{m=1}^N \frac{P(\omega_m)}{\hat{P}(\omega_m)} = 1. \quad (26)$$

Thus, from equation (25):

$$E_{IS\min} = \frac{1}{N} \sum_{m=1}^N \left[ -\ln \frac{P(\omega_m)}{\hat{P}(\omega_m)} \right] = \ln \frac{\left[ \prod_{m=1}^N \hat{P}(\omega_m) \right]^{1/N}}{\left[ \prod_{m=1}^N P(\omega_m) \right]^{1/N}} \quad (27)$$

and one can conclude that the minimum error is equal to the logarithm of the ratio of the geometric means of the model spectrum and the original spectrum.



**Figure 3.8.** FFT magnitude spectrum of a male vowel /a/ (thin line) and the all-pole spectrum of the DAP method (thick line) together with the LP method (dashed line). For the sake of clarity, the magnitude levels of the prediction model have been lifted 10 dB [Mag05].

Alku *et al.* [AVV02] stated that the DAP allows a better estimation of the formants of the vocal tract, particularly the  $F_1$ , and decreases the amount of formant ripple in the estimated glottal flows. Also, it seems to be more accurate for high-pitched voices than the LPC method.

### 3.3.3. MEL-FREQUENCY CEPSTRAL COEFFICIENTS (MFCC) METHOD

Mel-Frequency Cepstral Coefficients (MFCC) method is based on feature extraction of speech signal from its cepstrum, changed according to the Mel scale, a scale that seeks to replicate the human auditory perception.

#### 3.3.3.1. Cepstral Analysis

In the frequency domain, the convolution between the two components of the signal, the excitation source signal  $g[n]$ , and the impulse response of the vocal tract  $v[n]$ , is transformed into a product:

$$g[n] * v[n] \Leftrightarrow G(\omega)V(\omega). \quad (28)$$

Applying the logarithm operator to the signal, it yields:

$$\log(G(\omega)V(\omega)) = \log(G(\omega)) + \log(V(\omega)). \quad (29)$$

Thus, the resulting signal is a linear combination between the two components.

Applying the inverse of the Fourier transform to the resulting signal from equation (29), the signal will be represented in a new domain, called the cepstral domain. In this domain, it is possible that the two components of the signal, the excitation and the impulse response of the vocal tract, are linearly combined and separated from each other. Thus, representing the speech signal in the cepstrum, it is possible to select specific components of the latter, applying a linear filter to remove unwanted parts. Applying a reverse Fourier transform to the preserved components of the cepstrum, allows to reconstruct the desired components in the spectral domain.

The cepstral domain can be divided into real cepstrum and complex cepstrum. The difference between them is that, in the former case, the phase information of the speech signal is lost, i.e., any signal is minimum phase. In the latter, the cepstral coefficients have real part and imaginary part and, thus, the phase information is preserved.

The real cepstrum and the complex cepstrum of a signal  $x[n]$  are given, respectively, by [Gol00]:

$$c[n] = \frac{1}{2\pi} \int_{-\pi}^{\pi} \ln |X(e^{j\omega})| e^{j\omega n} d\omega \quad (30)$$

and

$$\hat{x}[n] = \frac{1}{2\pi} \int_{-\pi}^{\pi} \ln X(e^{j\omega}) e^{j\omega n} d\omega. \quad (31)$$

In this equation, the complex logarithm is used and can be written as:

$$\hat{X}(e^{j\omega}) = \ln X(e^{j\omega}) = \ln |X(e^{j\omega})| + j\theta(\omega) \quad (32)$$

and the phase  $\theta(\omega)$  is given by:

$$\theta(\omega) = \arg[X(e^{j\omega})]. \quad (33)$$

From equations (30) and (31) it is simple to conclude that if the signal  $x[n]$  is real, both the real cepstrum and the complex cepstrum are real signals and homomorphic transformations, i.e., they convert a convolution into a sum. Thus, if  $x[n]$  is a speech signal, then the real cepstrum and the complex cepstrum can be written as the sum of the excitation and the vocal tract filter.

### 3.3.3.2. Mel scale

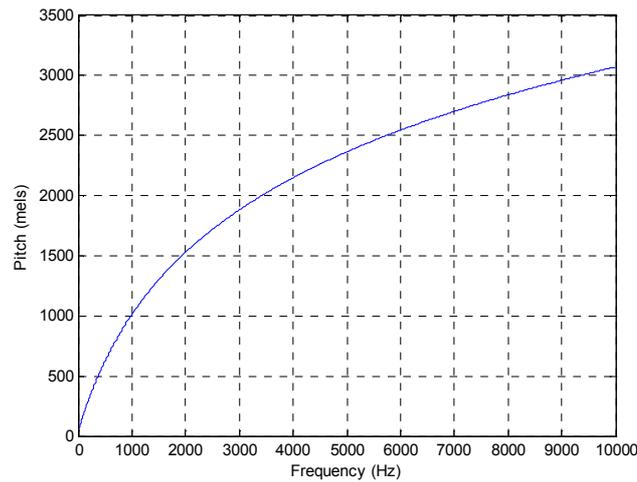
Several studies state that the correlation between the human perception of the fundamental frequency of a sound and its real value is not linear (e.g. [CL09; Cua07]). The perceived frequency by human people is known as pitch. In 1940, Stevens and Volkman developed a scale, called the Mel scale, that seeks to approach the characteristics of sensitivity of human hearing [Gol00].

“Mel” is a unit of measure of perceived pitch or frequency of a tone, defined as:

$$f_{mel} = 1127 \ln \left( 1 + \frac{f}{700} \right) \quad (34)$$

where  $f$  is the actual frequency in Hz.

Figure 3.9 shows the Mel scale. As it can be seen, this scale has almost a linear frequency behaviour below 1000 Hz and a logarithmic behaviour above 1000 Hz.



**Figure 3.9.** *The Mel scale.*

Some experiments in human perception have shown that frequencies of a complex sound within a certain bandwidth of some nominal frequency cannot be individually identified unless one of the components of this sound falls outside the bandwidth [Cua07]. This bandwidth is known as critical bandwidth and its width varies with the frequency.

### 3.3.3.3. MFCC calculation process

In the MFCC analysis, the first steps are the pre-emphasis and the segmentation of the speech signal, typically using the Hamming window with 50% overlapping. The next processing step is the Fast Fourier Transform (FFT), which converts each frame of  $N$  samples from the time domain into the frequency domain. Then, the amplitude of the FFT is obtained and is filtered through triangular windows to approximate the Mel frequency scale. A cepstral analysis follows from a minimum frequency of 0 Hz to the maximum frequency of half of the sampling frequency. In the final step, the cepstral coefficients are extracted, applying the logarithm function to the different frames of the spectrum and then using the Discrete Cosine Transform (DCT)<sup>4</sup>.

A block diagram of the MFCC calculation process is represented in Figure 3.10.

According to Jankowski *et al.* [JVL95], the MFCC analysis provides superior noise robustness in comparison with linear prediction-based feature extraction techniques.

<sup>4</sup> See Appendix A for mathematical details.

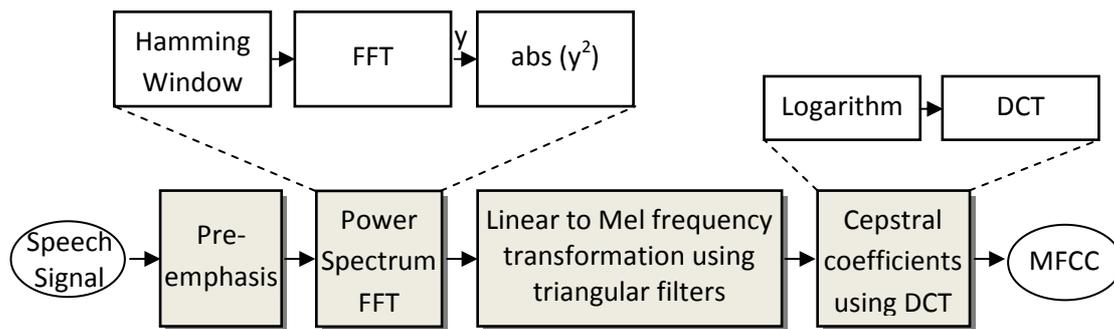


Figure 3.10. Block diagram of the MFCC calculation process.

### 3.4. GLOTTAL PULSE MODELS

The importance of the analysis of the glottal flow is very well established in different areas but it was stated before that the medical procedures that allow the observation of the vocal fold vibration are uncomfortable for the speaker and interfere with normal phonation behaviour. The estimation of the glottal flow from a speech signal (called inverse filtering) has been a challenge over the last decades and, as a consequence, several glottal models have been proposed to define one period of the glottal flow analytically. In this section, some of these models will be described.

Although the glottal models do not use the same number of parameters or the same name for similar parameters, which makes it rather difficult to understand the differences and similarities among models, all share some common features, as stated by Doval and d'Alessandro [DA99], because:

- the glottal flow is always positive or null;
- the glottal flow is quasi-periodic;
- the glottal flow is a continuous function of time;
- on a single period, the glottal flow is bell-shaped: it starts increasing, then decreasing and finally null;
- the glottal flow is a differentiable function of time, except in some instants as the glottal closing instant (GCI) and the glottal opening instant (GOI);
- the glottal opening phase is longer than the glottal closure phase.

Despite the fact that most of the glottal models consider these assumptions, as it was previously mentioned, studies have shown that the majority of the individuals reveal a glottal



In the following list, some of the most known and used glottal models are briefly described.

- **Rosenberg Glottal Model**

Rosenberg proposed six different models to model a glottal pulse [Deg10]. One of the most known models is:

$$g_{R_1}(t) = \begin{cases} \frac{A_v}{2} \left[ 1 - \cos\left(\frac{\pi t}{t_e}\right) \right] & , \quad 0 \leq t < t_e \\ A_v \cos\frac{\pi(t-t_e)}{2t_c} & , \quad t_e \leq t < t_c \\ 0 & , \quad t_c \leq t < T_0 \end{cases} \quad (36)$$

It is clear that in this model the three phases of the glottal cycle (opening phase, closing phase and closed phase) are represented, as illustrated in Figure 3.12 (a), and the corresponding derivative has a discontinuity for  $t = t_e$ .

According to Degottex [Deg10], in 1971, Rosenberg made a test to select the model which sounds as the best source and selected one model that shapes the glottal volume velocity with two polynomial parts:

$$g_{R_2}(t) = \begin{cases} At^2(t_e - t) & , \quad 0 < t < t_c \\ 0 & , \quad t_c < t < T_0 \end{cases} \quad (37)$$

This latter model has only one shape parameter,  $t_e$ , the instant of closure and it is simple to determine the instant of maximum flow:  $t_p = \frac{2}{3}t_e$ .

- **Fant Glottal Model**

In 1979, Fant [Fan79] proposed a glottal model which is described by:

$$g_F(t) = \begin{cases} \frac{1}{2}(1 - \cos(\omega_g t)) & , \quad 0 \leq t \leq t_p \\ K \cos(\omega_g(t - t_p)) - K + 1 & , \quad t_p < t \leq t_c = t_p + \frac{1}{\omega_g} \arccos \frac{K-1}{K} \\ 0 & , \quad t_c < t \leq T_0 \end{cases} \quad (38)$$

where  $\omega_g = \pi / t_p$  and  $K$  is a parameter that controls the slope of the descending branch.

According to this model, if  $K = 0.5$  the pulse is symmetric.

This model of glottal flow is illustrated in Figure 3.12 (b).

- **Liljencrants-Fant Glottal Model (LF Model)**

Liljencrants and Fant [FLL85] suggested a model for the derivative of the glottal flow, called the LF model. This is a five parameter model that, together with the length of the glottal cycle, determines uniquely the pulse shape.

The LF model is described by the following equations:

$$g'_{LF}(t) = \begin{cases} E_0 e^{\alpha t} \sin(\omega_g t) & , \quad 0 \leq t \leq t_e \\ -\frac{E_e}{\beta t_a} (e^{-\beta(t-t_e)} - e^{-\beta(t_c-t_e)}) & , \quad t_e < t \leq t_c = T_0 \end{cases} \quad (39)$$

where,

- $E_0$  is a scale factor necessary to achieve area balance;
- $E_e$  is the amplitude of the negative maximum;
- $\alpha = C\pi$ , where  $C$  controls the exponentially growing sinusoid;
- $\omega_g = 2\pi F_g$  is the frequency of the sinusoid, where  $F_g = \frac{1}{2t_p}$ ;
- $\beta$  is a decay constant for the recovery phase of the exponential.

The parameters  $\alpha$  and  $\beta$  can be calculated from equation (39) by imposing:

$$g'_{LF}(t_e) = E_e \quad (40)$$

and the energy balance,

$$\int_0^{T_0} g'_{LF}(t) dt = 0. \quad (41)$$

The LF model is, thus, a piecewise function, consisting of two parts. The first part models the glottal flow derivative from the instant of glottal opening to the instant of the maximum negative extreme and corresponds to the opening phase. The second segment characterizes the closure phase. In addition to these two equations, the model is governed by the principle of area balance, meaning that the integral of the function over the entire period must be equal to zero [Cin08]. In Figure 3.12 (c) the LF-model is represented as well as the derivative of the

glottal flow, where it is apparent that the timing instants of the LF model have a correspondence with the behaviour of the vocal folds.

This model seems to be the preferred glottal model by many researchers (e.g. [Boz05], [Hen01], [CRR<sup>+</sup>07]), because of its ability to accommodate a wide range of natural variation. Also, several studies have shown that the LF model is superior to other models when the objective is to model natural speech [Cin08]. However, its use in speech synthesizers is limited because of its computational complexity, since it involves solving a nonlinear equation (41) [Vel98].

- **Transformed-LF (LF<sup>Rd</sup>): a particular parameterization of the LF model**

In 1995, Fant proposed an alternative model, called the LF<sup>Rd</sup> model, which is a particular parameterization of the LF model. In this model, the curve is parameterized by only one shape parameter  $Rd$ . The author has shown that this parameter allows to better describing voice qualities using a single value.

The  $t$  parameters can be expressed in a normalized form, known as  $R$  parameters:

- $R_0 = t_e / T_0$ ;
- $R_g = T_0 / (2t_p)$ ;
- $R_k = (t_e - t_p) / t_p$ ;
- $R_a = t_a / T_0$ .

From several measurements of the  $R$  parameters on various speakers having different types of phonation, the following statistical regression has been proposed:

$$Rd = (1 / 0.11)(0.5 + 1.2R_k)(R_k / 4R_g + R_a). \quad (42)$$

Figure 3.12 (e) illustrates some examples of the LF<sup>Rd</sup> model for different  $Rd$  values.

From this parameter, the parameters can be predicted as follows [Deg10]:

$$\begin{aligned} R_{ap} &= (-1 + 4.8Rd) / 100 \\ R_{kp} &= (22.4 + 11.8Rd) / 100 \\ R_{gp} &= 1 / \left[ 4 \left( \left( 0.11Rd / (0.5 + 1.2R_{kp}) \right) - R_{ap} \right) / R_{kp} \right]. \end{aligned} \quad (43)$$

According to Fant [Fan95],  $Rd$  takes a value between 0.3 and 2.7.

- **Rosenberg++ Glottal Model**

Veldhuis [Vel98] proposed a glottal source model which has two extensions of the Rosenberg model (thus the name R++) described by the expression in (37). However, according to this author, the Rosenberg model of the glottal source has always the same instant of maximum flow, which limits its flexibility and does not have a return phase.

The R++ model is given by [Vel98]:

$$g_{R++}(t) = \begin{cases} f(t) & , 0 < t < t_e \\ f(t_e) + t_a \cdot K \cdot \left( 1 - e^{-\frac{t-t_e}{t_a}} - \frac{t-t_e}{t_a} e^{-\frac{t-t_e}{t_a}} \right) \cdot \frac{1}{1 - e^{-\frac{t_c-t_e}{t_a}}} & , t_c < t < T_0 \end{cases} \quad (44)$$

with

$$f(t) = At^2 \left( t^2 - \frac{4}{3}t(t_p + t_x) + 2t_p t_x \right) \quad (45)$$

$$K = 4A_v t_e (t_p - t_e)(t_x - t_e). \quad (46)$$

The parameter  $t_x$  can be found solving equation:

$$t_x = t_e \left( 1 - \frac{\frac{t_e^2}{2} - t_e t_p}{2t_e^2 - 3t_e t_p + 6t_a(t_e - t_p)D(t_c, t_e, t_a)} \right) \quad (47)$$

with

$$D(t_c, t_e, t_a) = 1 - \frac{t_c - t_e}{t_a} \cdot \frac{1}{e^{\frac{t_c-t_e}{t_a}} - 1}. \quad (48)$$

Figure 3.12 (d) illustrates LF and R++ glottal-pulse time derivatives for two sets of parameters. The top panel shows glottal-pulse time derivatives for a modal voice with a distinct closed phase and the bottom panel for an abducted voice without a distinct closed phase.

According to the author of the model [Vel98], R++ model is computationally more efficient than LF model and requires less processing time.

- **Klatt Glottal Model**

Klatt and Klatt [KK90] proposed two models of the glottal source, in which the characteristics of the waveform are described by conventional parameters as the fundamental frequency of voicing ( $F_0$ ), the peak amplitude of the glottal pulse ( $A_v$ ), the open quotient (OQ) and the

spectral tilt or the spectral change associated with “corner rounding” in which closure is nonsimultaneous along the length of the vocal folds. The open quotient corresponds to the ratio of the open phase duration to the total duration (i.e, the period) of the glottal cycle.

One of the models is a slightly modified version of the LF model allowing to consider turbulence noise generation at the glottis. Thus, a cutoff frequency is specified below which the source consists of harmonics, and above which the source is flat-spectrum noise.

The other proposed model, known as the KLGLOTT88 model, or the Klatt model, synthesizes the glottal pulse in the same way as the Rosenberg model described by the analytical expression (37).

Figure 3.12 (f) illustrates the derivative glottal wave of the Klatt model.

The derivative of the glottal flow model is given by:

$$g'_k(t) = \begin{cases} 2a \frac{t}{f_s} - 3b \left( \frac{t}{f_s} \right)^2, & 0 \leq t \leq T_0 \cdot OQ \cdot f_s \\ 0, & T_0 \cdot OQ \cdot f_s < t \leq T_0 \cdot f_s \end{cases} \quad (49)$$

where

$$a = \frac{27A_v}{4OQ^2 \cdot T_0} \quad (50)$$

$$b = \frac{27A_v}{4OQ^3 \cdot T_0^2} \quad (51)$$

In this model the closed phase of the glottal cycle (i.e., the derivative is zero) is clearly visible, as it can be seen in Figure 3.12 (f).

- **Causal-Anticausal Linear Model (CALM)**

This model, proposed by Doval, d’Alessandro and Henrich [DAH03] and referred to as CALM model, is totally described in the spectral domain, based on the assumption that the glottal flow can be considered as the impulse response of a linear filter.

The authors showed that glottal flow characteristics contribute to the speech signal spectrum with two components: the glottal formant (frequency of the maximum on the spectrum of the time-derivative of the glottal pulse) and spectral tilt [Boz05]. The latter is linked, in this model, to the causal part of the model glottal closure and it is related, in terms of spectra, to the position of the single causal pole of the model. The glottal formant corresponds to the anticausal part of the glottal model and to the pair of poles outside the unit circle.

This model is defined by two filters. The first anti-causal filter is given by:

$$H_A(z) = \frac{b_1 z}{1 + a_1 z + a_2 z^2} \quad (52)$$

with

$$a_1 = -2e^{-a_p / f_s} \cos(b_p / f_s) \quad (53)$$

$$a_2 = e^{-2a_p / f_s} \quad (54)$$

$$b_1 = E \frac{\pi^2}{b_p^3} e^{-a_p / f_s} \sin(b_p / f_s) \quad (55)$$

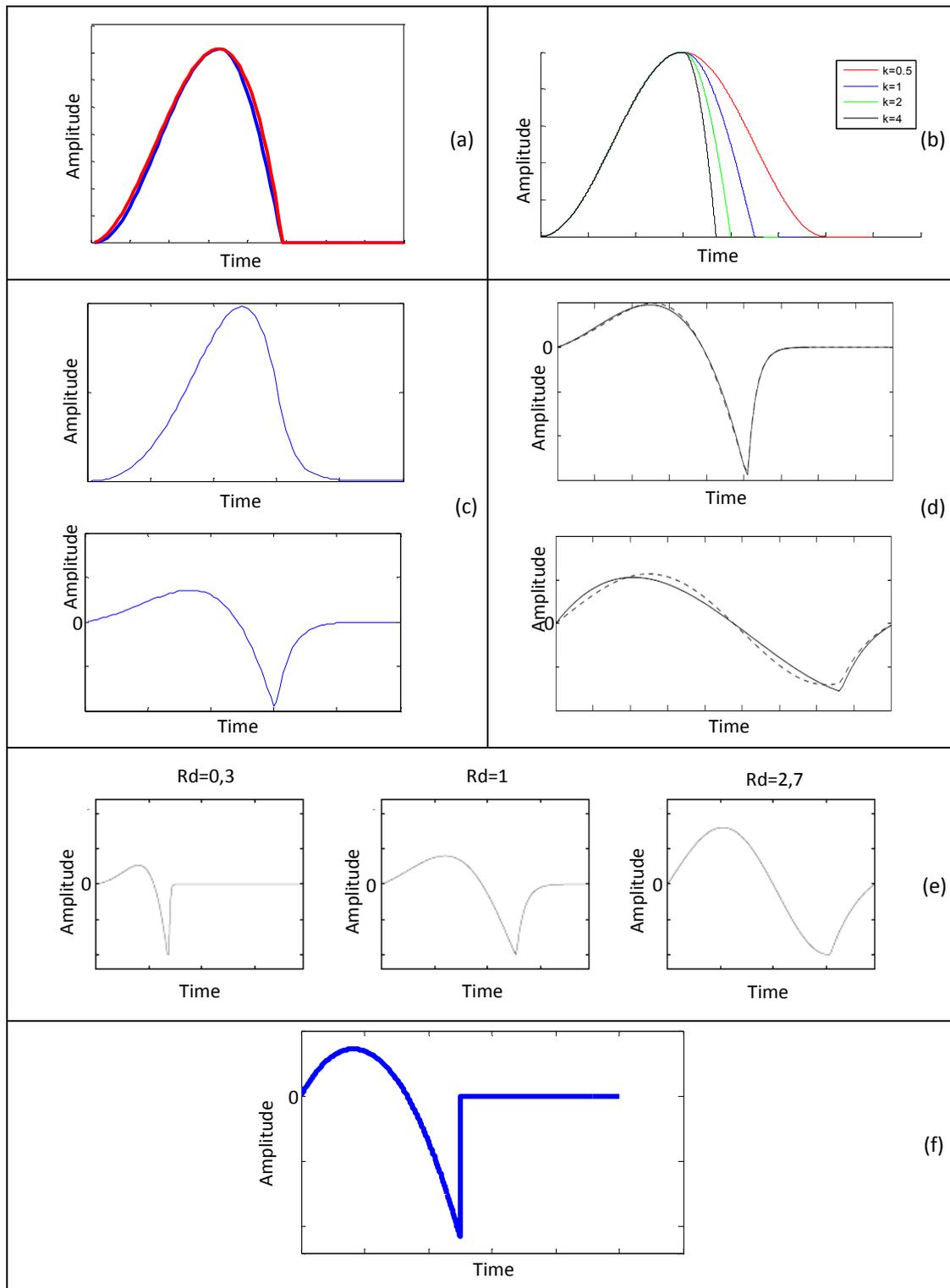
$$a_p = -\frac{\pi}{OQ.T_0 \tan(\pi\alpha_m)} \quad (56)$$

$$b_p = \frac{\pi}{OQ.T_0} \quad (57)$$

The second causal filter is equivalent to the low-pass filter of the KLGLOTT88 model, used to control the spectral tilt at high frequencies [Deg10].

The anti-causal pole pair, as it can be concluded from the equations above, does not depend on the time-parameters and the causal real pole is independent of the parameters  $OQ$  and  $\alpha_m$ .

This approach, that will be explored in the next chapter, implies that it is possible to obtain an estimation of the voice source parameters without any inverse filtering procedure, only requiring a process to separate the causal and the anticausal parts of the speech signal.



**Figure 3.12.** *Glottal pulse models:*

- (a) *The Rosenberg model. In blue is represented the glottal pulse defined by the model (36) and in red glottal pulse defined by the model (37).*
- (b) *Fant model, proposed in 1979.*
- (c) *The LF model (upper panel) and the corresponding derivative (lower panel).*
- (d) *R++ (solid lines) and LF (dashed lines) glottal pulse time derivatives [Vel98].*
- (e) *LF<sup>Rd</sup> model for different Rd values [Deg10].*
- (f) *Klatt derivative glottal pulse model.*

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### 3.5. SUMMARY

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This chapter has focused on Fant's source-filter theory of speech production, according to which the human voice is the result of the convolution between the excitation source signal, that represents the glottal flow, the impulse response of the vocal tract filter and the lip radiation. The mathematical details of this process and some methods to extract features from a voice signal, specifically the LPC, DAP and MFCC methods, were presented and analysed. It was concluded that despite the fact that the LPC method is widely used because it is fast and simple, it has some limitations, namely the difficulty in the determination of the optimal order, the iterative procedure is rather slow and it is especially problematic for high pitched harmonic sounds. This last limitation turns the DAP method more attractive than LPC, since it is more accurate for high-pitched voices and also in the estimation of the formants of the vocal tract, particularly the  $F_1$ . The MFCC method provides superior noise robustness in comparison with linear prediction-based feature extraction techniques.

Also, within this chapter different glottal flow models were presented that are representative of the state of the art, as well as their respective mathematic details. Most of these glottal flow models are implemented in the time domain and although they do not use the same number or the same parameters, all have in common some features, namely the signal of the glottal flow (always positive or null) and the glottal flow derivative, for one single period, starts positive, then negative and finally null, which means that the glottal flow starts increasing, then decreasing and, in the last, it is null.

# Chapter 4

## GLOTTAL PULSE ESTIMATION - STATE OF THE ART

### Contents

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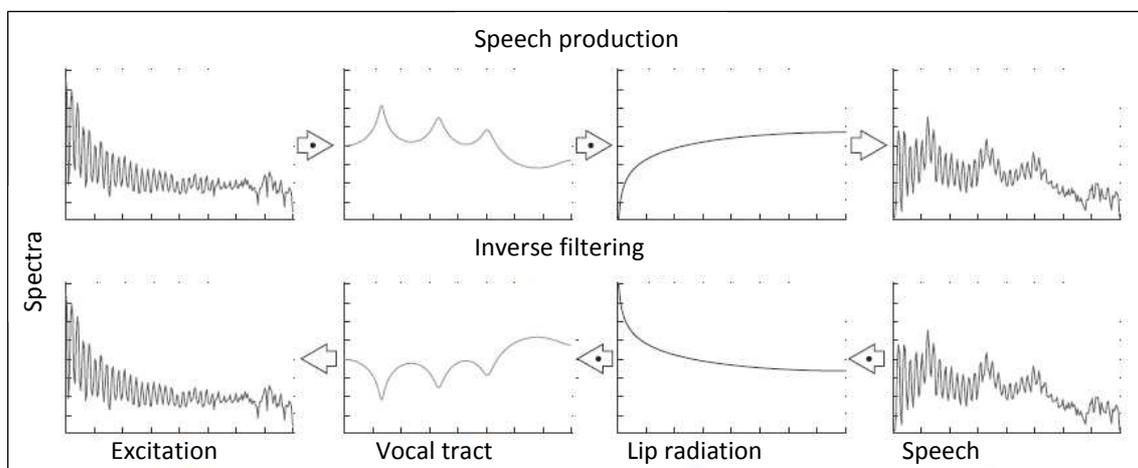
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## 4.1. INTRODUCTION

In the last decades, several methods and techniques have been developed for the estimation of the glottal waveform during voiced speech and it continues to be a currently active research field. Many of these approaches are based on Fant's source-filter theory: the glottal flow and the transfer function of the vocal tract are independent and thus linearly separable from the speech signal [Air08].

The source-filter theory of speech production states that speech can be described as a sound source being modulated by a dynamically changing filter. This is a simplification of the relationship between the glottal source and the vocal tract and implies that speech signals are produced by a source signal, representing the glottal airflow, that is modulated by a transfer (filter) function determined by the shape of the vocal tract. If the transfer function of the vocal tract filter is known, an inverse filter can be constructed in order to estimate the voice source. Inverse filtering is a procedure that tries to estimate the glottal pulse by cancelling the spectral effects of the vocal tract and lip/nostrils radiation (Figure 4.1).



**Figure 4.1.** Schematic spectra of the represented signals and filters.

The upper row represents the separated speech production model. The lower row represents the corresponding inverse filtering process, in which the lip/nostrils radiation and vocal tract are inverted to produce an estimate of the glottal flow waveform [Air08].

This procedure has, generally, three different stages: first, modelling the vocal tract filter (usually, as an all-pole model), i.e., the transfer function of the vocal tract is estimated; second, filtering the voice signal through the inverse filter of the vocal tract in order to cancel the effects of formants; and finally, filtering the resulting signal with a first-order integrator to eliminate the effects of the lip radiation, achieving the estimation of the glottal pulse.

Basically, the procedure involves extracting two signals, the volume velocity waveform at the glottis, and the effect of the vocal tract filter, from a single source signal [Pul05]. If voice production is described as a convolution between the glottal excitation and the vocal tract filter, than inverse filtering can be understood as a deconvolution operation.

In the last years other glottal flow estimation techniques have been developed that are not based on inverse filtering procedures.

In this chapter different glottal flow estimation processes, including inverse filtering techniques, are reviewed. Also, some of these procedures will be implemented using speech signals (real and synthetic) in order to analyse, compare and evaluate the corresponding estimations of the glottal pulse.

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## **4.2. GLOTTAL PULSE PARAMETERIZATION**

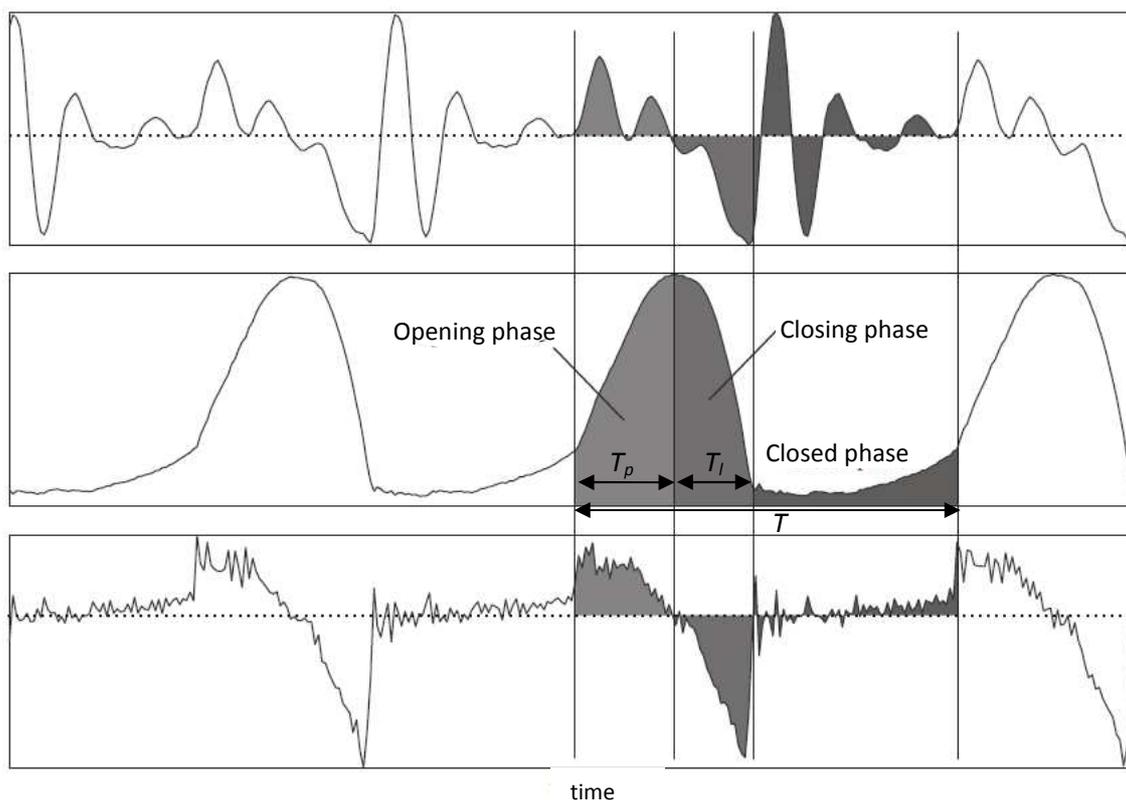
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The estimation of the glottal pulse has usually a final step consisting in the parameterization, whose purpose is to determine quantitative features of the signal that characterize the glottal wave and may quantify a perception parameter [Sou11]. The parameterization of the estimated glottal pulse might be helpful to the interpretation of the data within the signal [Cin08].

There are three main categories of parameterization methods of the glottal flow: time-domain, frequency-domain and model-based methods [Air08a].

### **4.2.1. TIME-DOMAIN METHODS**

The glottal cycle, as it was referred, can be divided to a few phases. Usually, in time-domain methods, the critical time instants, as the instant of the glottal opening and the glottal closure, are marked in the glottal flow pulse and the durations of the phases are measured. This is illustrated in Figure 4.2. From these values some time-domain parameters can be obtained, as the open quotient (OQ), the closing quotient (CIQ) and the speed quotient (SQ).



**Figure 4.2.** Three periods of a sound-pressure waveform and the respective glottal flow and its derivative. The opening, closing and closed phases of the glottal flow waveform are highlighted for clarity. The length of the glottal cycle is denoted by  $T$ , the length of the opening phase by  $T_p$  and the length of the closing phase by  $T_l$  (adapted from [Air08a]).

As mentioned in section 3.4, the open quotient, also sometimes referred to in the literature as the glottal pulse width [Cin08], is defined as the ratio of the open phase duration to the total duration of the glottal cycle. According to this definition, the open quotient is null for a sealed larynx, and when turbulent air is travelling unhindered through the glottis, the open quotient is 1. According to some authors, the open quotient of a normal phonation is a value between 0.4 and 0.8 [Cin08].

The closing quotient is the ratio of the closing phase duration to the glottal cycle duration and due to abrupt closure of the vocal folds during phonation, usually this value is less than half of the open quotient.

The speed quotient, also called the glottal pulse skewness, is the ratio of the opening phase duration to the closing phase duration. This last value indicates the speed of glottal opening to glottal closing and, if it is equal to 1, it means that the opening phase has the same duration as the closing phase.

Denoting  $T$  the duration of the glottal cycle,  $T_p$  the duration of the opening phase and  $T_l$  the duration of the closing phase, OQ, CIQ and SQ result as:

$$OQ = \frac{T_p + T_l}{T}, \quad (58)$$

$$CIQ = \frac{T_l}{T}, \quad (59)$$

$$SQ = \frac{T_p}{T_l}. \quad (60)$$

Despite the simplicity of these definitions, it is problematic to determine their exact values because it is difficult to find the exact locations of the glottal opening and closing instants. This reduces the precision and robustness of these parameters [Air08b].

Some other time-based parameters can be defined, combining the amplitude-based time instants to express properties related to the time domain of the signals, such as the amplitude quotient (AQ), defined as:

$$AQ = \frac{A_{ac}}{d_{\min}}. \quad (61)$$

where  $A_{ac}$  is the difference between the maximum and the minimum value within one period and  $d_{\min}$  is the minimum value of the flow derivative. This parameter has been shown to correlate with the phonation type [Air08b].

Normalized amplitude quotient (NAQ) is other time-based parameter, defined as the ratio of the amplitude quotient to the total period duration:

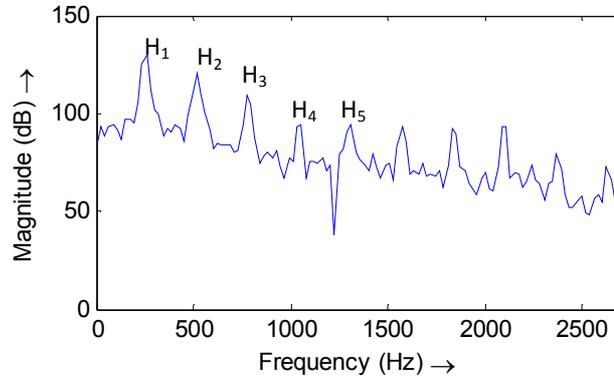
$$NAQ = \frac{AQ}{T}. \quad (62)$$

This parameter seems to correlate with the expression of the phonation type in intensity changes [Air08b].

The measurements of amplitude levels are straightforward to obtain and the absolute scale of the glottal pulses is not required to be known, which makes the AQ and NAQ more robust than their time-based counterpart, CIQ [Air08a]. However, time-domain methods are not very robust to noisy data since the time-domain waveforms and landmarks vary a lot with noise [Boz05].

### 4.2.2. FREQUENCY-DOMAIN METHODS

Glottal flow parameterization is achieved in the frequency domain by taking measurements from the power spectrum of the flow signal, as shown in Figure 4.3.



**Figure 4.3.** Flow magnitude spectrum. The levels of the first five harmonics are depicted as  $H_1$  to  $H_5$ .

Some parameters have been proposed to facilitate parameterization of the spectra of the glottal flow pulses, as the difference of the first and second harmonics decibels, denoted by  $H_1 - H_2$ , or  $\Delta H_{12}$ , and the harmonic richness factor (HRF):

$$HRF = \frac{\sum_{k \geq 2} H_k}{H_1} \quad (63)$$

where  $H_k$  is the  $k$ th harmonic. This parameter is related to  $H_1 - H_2$  but tries to approximate the spectral energy distribution from more than one higher harmonic [Air08b].

A trivial observation on these parameters is that they co-vary with the fundamental frequency. When the fundamental frequency increases, the distance between the harmonics grows and, thus, the value of  $H_1 - H_2$  increases while the value of HRF decreases.

Parabolic spectrum parameter (PSP) is another frequency-domain parameter used to improve spectral parameterization, which fits a second-order polynomial to the flow spectrum to gain an estimate of the spectral slope [Air08a].

There are several advantages on the spectral approach to voice source modelling, such as the better description of the voice quality spectral parameters, the more efficient voice quality modification and voice source parameter estimation [DAH03]. Frequency-domain methods seem to be also more robust in handling both noisy and phase distorted data [Boz05]. However, there are few frequency-domain glottal source models discussed in the literature.

### 4.2.3. MODEL-BASED METHODS

The model-based parameterization methods attempt to capture the general flow shape of the glottal source with the finer subtleties of the vocal fold motion, using some mathematical formula (as the glottal pulse models) that yields artificial waveforms similar to glottal flow pulses and usually implemented in the time domain [Cin08].

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## 4.3. INVERSE FILTERING TECHNIQUES

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Inverse filtering has many applications in both research and clinical examination of voice production, as it was stated above, but few voice inverse filtering software packages exist and it is still a challenge to develop a complete and automatic inverse filtering method. Some of the existing tools implement manual inverse filtering techniques, as DeCap, developed by Svante Granqvist, and Waveview, developed by Glottal Enterprises. This latter software allows to analyse both CV-mask (airflow) and microphone (radiated pressure) waveforms during speech and singing. Also, Paul Milenkovich [Mil01] developed a time-frequency analysis software, TF32, that is able of linear predictive inverse filtering, and Kreiman *et al.* [KGB06], based on the inverse filtering method proposed by Javkin *et al.* [JBM87], developed an open-source inverse filtering and analysis software, Inverse Filter and Sky. Another open-source licence software package that implements glottal inverse filtering and several time-based parameters of the voice source in a graphical user interface is HUT Voice Source Analysis and Parametrization Toolkit (Aparat), developed by Airas *et al.* [APB<sup>+</sup>05]. This software is used in Matlab environment and implements the inverse filtering algorithms Iterative Adaptive Inverse Filtering (IAIF) and Pitch Synchronous Iterative Adaptive Inverse Filtering (PSIAIF). Also, in Matlab, there is Voicebox<sup>5</sup>, a speech processing toolbox maintained and mostly written by Mike Brookes, which includes inverse filtering routines but with no graphical user interface.

In this section some of the above mentioned techniques of inverse filtering and others will be presented and analysed and some of the inverse filtering software applications will be used to estimate the glottal pulse from speech signals.

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<sup>5</sup> Available at <http://www.ee.ic.ac.uk/hp/staff/dmb/voicebox/voicebox.html>

### 4.3.1. ITERATIVE ADAPTIVE INVERSE FILTERING (IAIF/PSIAIF)

The Iterative Adaptive Inverse Filtering (IAIF) is a semi-automatic inverse filtering method proposed by Alku [Alk92]. The method uses a speech pressure signal as input and generates an estimate of the corresponding glottal flow signal. This procedure has three fundamental parts: analysis, inverse filtering and integration. The glottal contribution to the speech spectrum is initially estimated using an iterative structure. This contribution is cancelled and, then, the transfer function of the vocal tract is modelled. Finally, the glottal excitation is estimated by cancelling the effects of the vocal tract (using inverse filtering) and lip radiation (by integration). A scheme of speech production model used in this approach is presented in Figure 4.4.

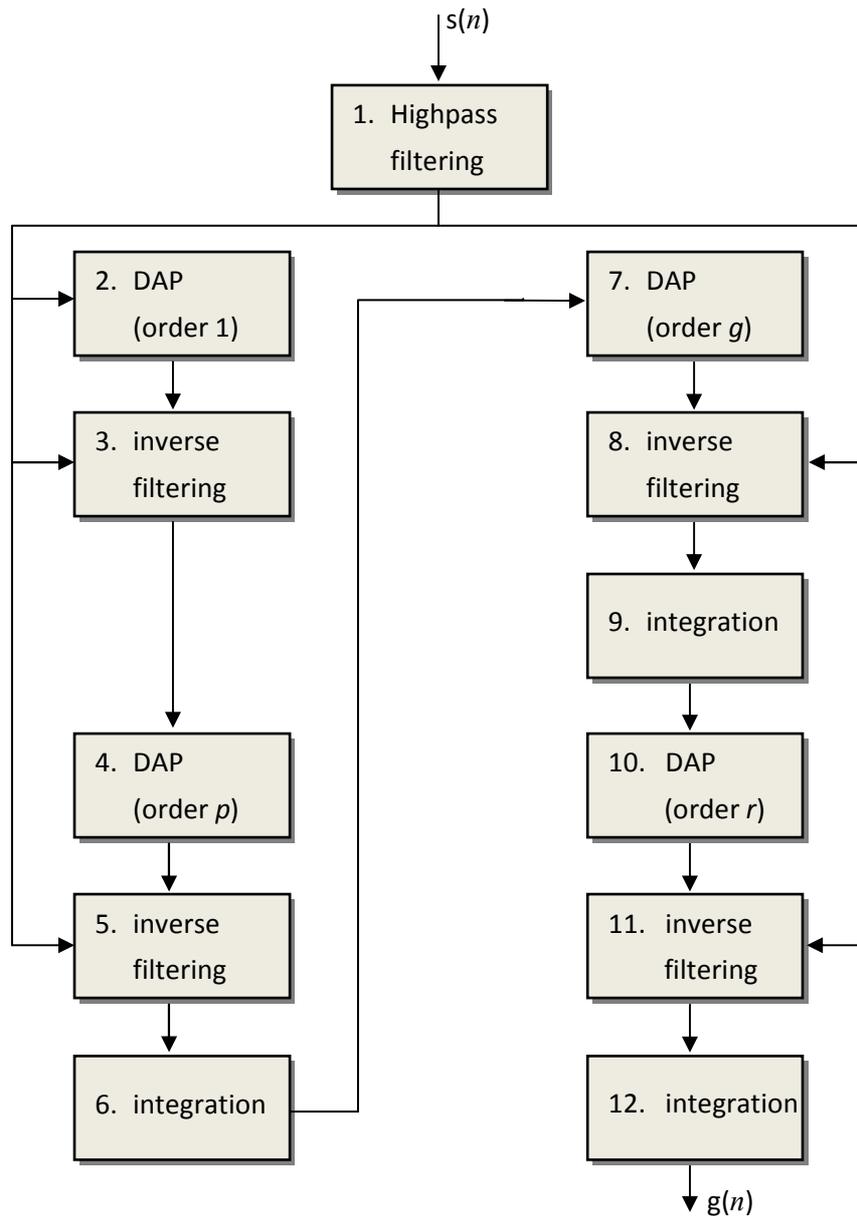


Figure 4.4. Speech production model used in IAIF.

The algorithm has been changed from that described by Alku [Alk92] by replacing the conventional linear predictive analysis (LPC) with the discrete all-pole modelling (DAP) method. These modifications, by Alku *et al.* [APB<sup>+</sup>05], allow to reduce the bias due to the harmonic structure of the speech spectrum in the formant frequency estimates. The block diagram of the IAIF procedure is shown in Figure 4.5.

The method operates in two iterations: the first phase, which consists on the stages 1 to 6, makes an estimation of the vocal tract function and applies inverse filtering to the signal with that estimate, and generates an estimate of the glottal source which is used as input of the second phase (stages 7 to 12) to achieve a more accurate estimate. A more detailed description of each step is provided below [Pul05].

1. The input signal (speech signal) is first high-pass filtered using a linear-phase finite impulse response (FIR) filter to remove disturbing low-frequency fluctuations. To avoid filtering out relevant information, the cut-off frequency should be lower than the fundamental frequency of the speech signal. The high-pass filtered signal is used as the input of the next stages.
2. The output of the previous step is analysed by a first-order DAP and there is a first estimate of the combined effect of the glottal flow and the lip radiation effect on the speech spectrum.



**Figure 4.5.** The block diagram of the IAIF method for estimation of the glottal excitation  $g(n)$  from the speech signal  $s(n)$  [APB<sup>+</sup>05].

3. The input signal is inverse filtered using the filter obtained in step 2. The spectral tilt caused by the spectrum of the excitation signal and the lip radiation effect is removed.
4. A new analysis by DAP is calculated to obtain a model of the vocal tract transfer function. The order  $p$  of the DAP analysis can be adjusted by the operator of the IAIF method and it is related to the number of formants modelled in the relevant frequency band.
5. The input signal is inverse filtered using the inverse of the  $p$ th-order model from the previous step.
6. Lip radiation is cancelled by integrating the output of the previous step. Then, a first estimation of the glottal flow is obtained and completes the first phase of the procedure.

7. A  $g$ th-order analysis of the obtained glottal flow estimate is calculated and then the second phase of the IAIF method. This gives a spectral model of the effect of glottal excitation on the speech spectrum. The value of  $g$  is usually between 2 and 4.
8. The input signal is inverse filtered using the model of the excitation signal to eliminate the glottal contribution.
9. The output of the previous step is integrated in order to cancel the lip radiation effect.
10. A new model of the vocal tract filter is formed by an  $r$ th order DAP analysis. The value of  $r$  can be adjusted and it is usually set equal to the value of  $p$  in step 4.
11. The input signal is inverse filtered with the vocal tract model obtained in the step 10, in order to remove the effect of the vocal tract.
12. The final estimate of the glottal flow is obtained, removing the lip radiation effect by integrating the signal. This yields, finally, to the output of the IAIF method.

A toolkit for voice inverse filtering, Aparat, which is a Matlab implementation of the IAIF method, was developed at the Laboratory of Acoustics and Audio Signal Processing at Helsinki University of Technology. This software (Figure 4.6), available as open-source<sup>6</sup>, is an interface for the semi-automatic IAIF inverse filtering algorithm. Also, allows to determine the time and amplitude based parameters and to visualize the spectra of the speech signal, the estimated glottal flow and the used vocal tract filter (Figure 4.7).

According to the authors, Aparat has been used successfully in several research projects. However, the application of automatic inverse filtering has been problematic in high pitched signals [APB<sup>+</sup>05].

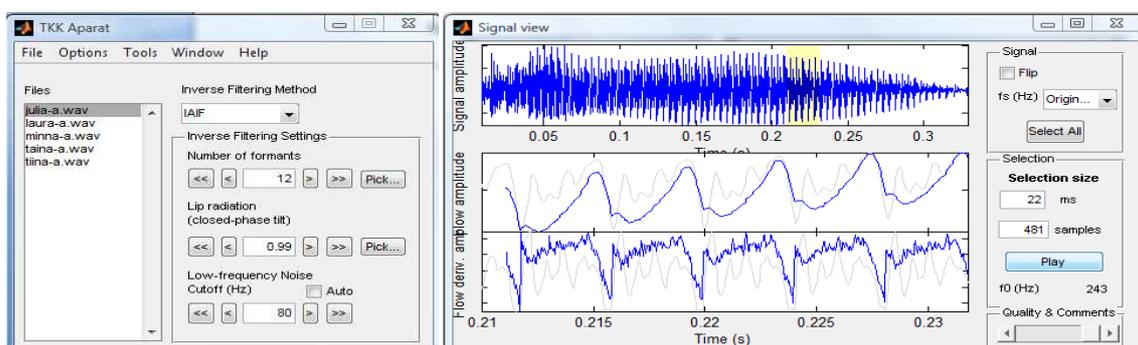
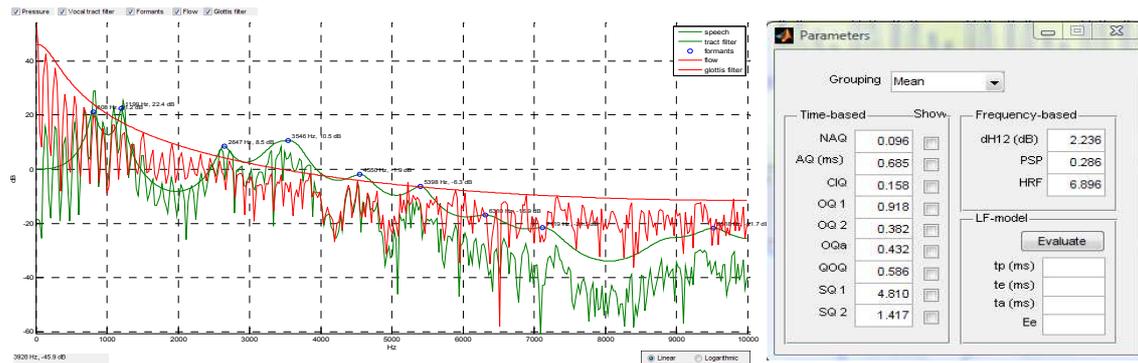


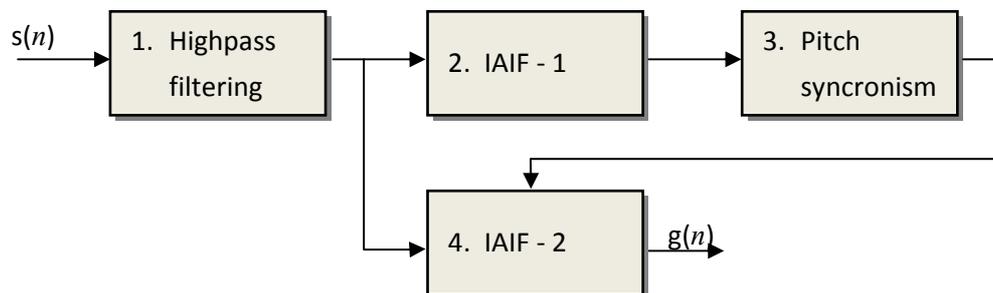
Figure 4.6. The graphical user interface and the signal view of Aparat.

<sup>6</sup> Available at <http://www.acoustics.hut.fi/software/aparat/>



**Figure 4.7.** The spectra view in Aparat of a speech signal, the calculated glottal flow and the used vocal tract filter (left), and parameters computed from the estimated glottal flow.

Pitch Synchronous Iterative Adaptive Inverse Filtering (PSIAIF) is an inverse filtering method based on IAIF. The glottal pulse is obtained by applying the IAIF method twice to the speech signal. The output of the first IAIF procedure is used to calculate the fundamental period which is important to calculate the new windowing, before applying IAIF again. The block diagram of PSIAF procedure is shown in Figure 4.8.

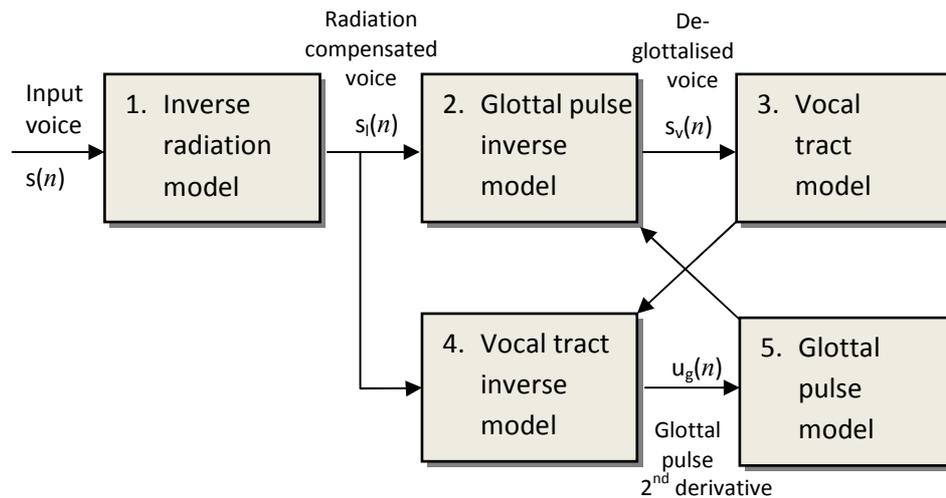


**Figure 4.8.** Block diagram of the main steps of the PSIAIF method.

Also based on IAIF is the method used by Murphy [Mur08], represented in Figure 4.9. The process uses repeated paired lattices to eliminate the effects of the vocal tract and lip radiation effects on the sound wave produced at the glottis.

The model operates as follows.

1. The input voice,  $s(n)$ , is filtered using an inverse radiation model filter to eliminate the effect of the lip radiation and produces a signal for the radiation compensated voice,  $s_r(n)$ .
2. A first estimation of the simple glottal pulse inverse function is obtained, which is used to eliminate the behaviour of the glottal pulse on the radiation compensated voice. Then, a trace for the deglottalised voice,  $s_v(n)$ , is produced.



**Figure 4.9.** Inverse filtering model by Murphy [Mur08].

3. A model for the vocal tract is derived by inverse filtering  $s_v(n)$  with lattice filters and extracting the model of the vocal tract.
4. The vocal tract inverse model is applied to the radiation compensated voice,  $s_i(n)$ , and generates a residual trace that contains information on the glottal pulse second derivative,  $u_g(n)$ , which is related to the relative speed between each fold's centre of mass.
5. The glottal pulse is extracted and, by repeating step 2 and, then, steps 3 to 5, reliable estimations for the glottal pulse second derivative and vocal tract function are made.

The author advocates that this method generates robust estimates for the voice signal decompositions, which have been used for determining any unusual vibration patterns that may be caused by pathological masses on the vocal folds or in their immediate environment.

This inverse filtering model is not free available and, therefore, it could not be tested for glottal source estimations.

#### 4.3.2. JAVKIN ET AL. METHOD

The first assumption of Javkin *et al.* [JBM87] is that speech waveforms are the product of both the phonatory setting and the shape of the vocal tract, and if the effect of the vocal tract can be subtracted from the speech waveform, then the glottal waveform can be examined without requiring any invasive procedure.

The algorithm proposed was developed in the frequency domain because, according to the authors, the formants introduced by the vocal tract, as well the effect of the lip radiation, are best understood in this domain rather than time domain. Since the estimated glottal flow is a function of time, the Z-Transform is used converting between these two domains.

Because of interactions between the vocal tract and the source, formant frequencies and bandwidths modulate during the open phase of the glottal cycle. Then, reliable estimate of the vocal tract parameters should be obtained during the glottal closed phase, which can be detected from the LPC residual signal.

To remove the formants and the effects of the lip radiation, it is necessary to construct a filter that has the inverse response. A digital filter that models the vocal tract is proposed and a model for each formant is obtained.

$$VT(z) = \prod_{k=1}^{k=M} F_k(z) \quad (64)$$

and

$$F_k(z) = \frac{1 - e^{-b_k T} \cdot 2 \cos(f_k T) + e^{-2b_k T}}{1 - e^{-b_k T} \cdot 2 \cos(f_k T) \cdot z^{-1} + e^{-2b_k T} \cdot z^{-2}} \quad (65)$$

where,

- $M$  is the number of formants,
- $b_k$  is the (one-sided) bandwidth in radians of formant  $F_k$ ,
- $f_k$  is the formant frequency in radians of formant  $F_k$ ,
- $T$  is the sampling period.

To invert the effect of the vocal tract it is necessary to invert the effect of all the formants, and to invert a formant, the numerator and denominator of equation (65) are simply reversed, yielding:

$$IF_k(z) = \frac{1 - e^{-b_k T} \cdot 2 \cos(f_k T) \cdot z^{-1} + e^{-2b_k T} \cdot z^{-2}}{1 - e^{-b_k T} \cdot 2 \cos(f_k T) + e^{-2b_k T}} \quad (66)$$

The lip radiation is modelled by:

$$L(z) = 1 - z^{-1} \quad (67)$$

Inverting the effect of lip radiation is less straightforward, because that effect amounts to a differentiation. However, at zero frequency,  $z$  will be equal 1, and the value of the inverse of the expression (67) would be infinity, which means that low frequencies would be greatly amplified, giving rise to an unstable response. To avoid this,  $z$  is multiplied by a constant ( $k$ )

that is less than 1 and multiplying the resulting expression by  $1 - k$  will make the amplification (or gain) equal to 1 at zero frequency. Then, the expression that will invert lip radiation is:

$$IL(z) = \frac{1 - k}{1 - kz^{-1}}. \tag{68}$$

Finally, inverting the effects of both vocal tract and lip radiation yields to the glottal pulse.

The proposed inverse filtering method implements the inversion of the nine formants in cascade.

Based on this inverse filtering method, Kreiman *et al.* [KGB06] developed interactive software<sup>7</sup> for inverse filtering, Inverse Filter, voice synthesis, Synthesizer, and voice analysis, Sky. Although the latter allows estimating the glottal pulse, in an automatic process, the inverse filter version is a simplified version of Inverse Filter.

The interfaces of each one of these computer programs are shown, respectively, in Figures 4.10, 4.11 and 4.12.



Figure 4.10. Inverse Filter interface.

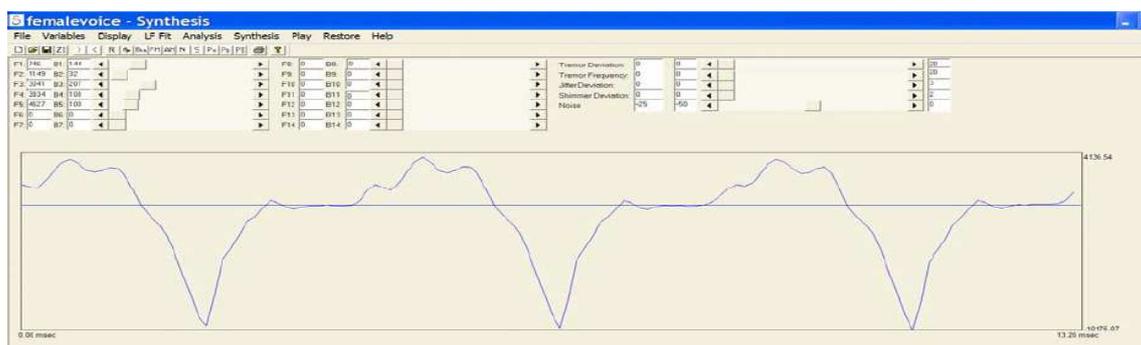


Figure 4.11. Synthesizer interface.

<sup>7</sup> Available at <http://www.surgery.medsch.ucla.edu/glottalaffairs/download.htm>.

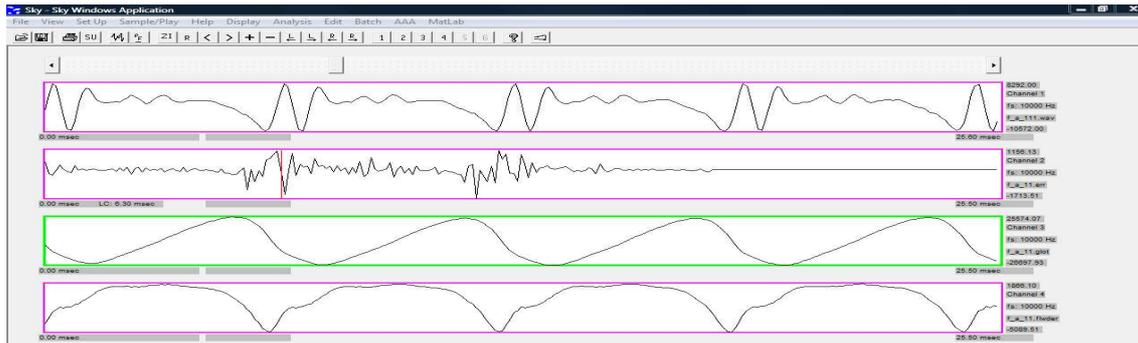
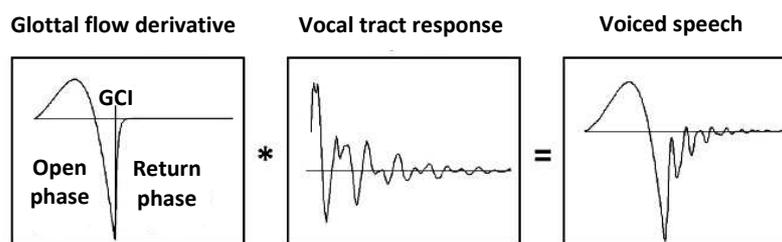


Figure 4.12. Sky interface.

#### 4.4. ZEROS OF THE Z-TRANSFORM (ZZT) AND COMPLEX CEPSTRUM (CC)

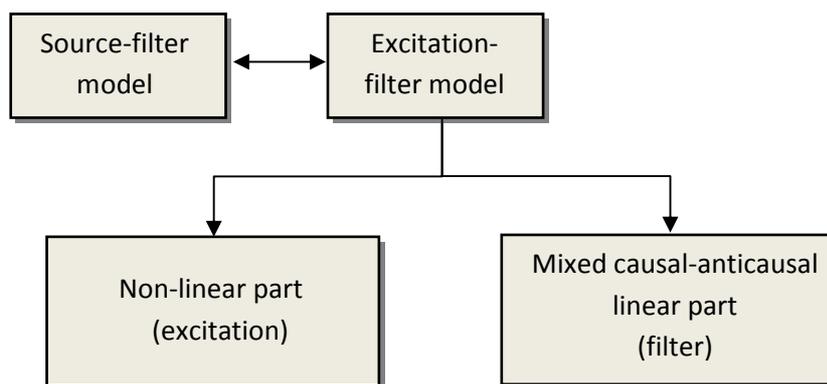
Zeros of the Z-Transform (ZZT) is a spectral decomposition method that considers the source-filter model as an “excitation-filter model” [SAD07]. This approach, proposed by Bozkurt *et al.* [BDA<sup>+</sup>05], relies on the observation that speech is a mixed-phase signal, where the anticausal component corresponds to the glottal source open phase and the causal component comprises both the glottis closure and the vocal tract contributions. Thus, the Glottal Closing Instant (CGI), also known as Glottal Closure Instant, allows the separation of glottal open and closed phases, corresponding, respectively, to the anticausal and causal signals, as it is illustrated in Figure 4.13.



**Figure 4.13.** Illustration of the source-filter modelling for one period. The Glottal Closing Instant (GCI) allows the separation of glottal open and glottal closed phases, corresponding to the anticausal and causal signals [adapted from DDM<sup>+</sup>08].

The authors stated that, while the contribution of the glottal flow in the vocal tract dominated spectrum is hardly observed, the vocal tract contribution in the glottal flow dominated spectrum is observed as ripples of low amplitude ([Boz05], [BDA<sup>+</sup>05]).

The block diagram of the model of speech production used on ZZT is shown in Figure 4.14.



**Figure 4.14.** The model of speech production used on ZT.

ZT it is a representation of the z-transform polynomial through its zeros (roots)<sup>8</sup> and, according to Bozkurt [Boz05], the set of ZT of a speech signal is just the union of ZT sets of the three components: the impulse, the glottal flow and the vocal tract filter.

The ZT pattern for the impulse train is a set of zeros on the unit circle (i.e., with modulus 1), with a gap at each multiple of the fundamental frequency. For the differential glottal flow, the ZT pattern is an union of two sets of zeros: one inside the unit circle (i.e., with modulus lower than 1), in which a gap can be seen, corresponding to the spectral tilt; other outside the unit circle (i.e., with modulus greater than 1), showing a gap between the zero on the real axis and the others, which corresponds to the glottal formant. Also, the glottal formant and the spectral tilt can be seen on the spectrum representation, respectively, as a local maximum in the low-frequency region and a global slope. The ZT pattern for the vocal tract is a line of zeros inside the unit circle, in which can be seen zero gaps, each one corresponding to a formant [BDA<sup>+</sup>04]. This is illustrated in Figure 4.15.

Before beginning the ZT process, the glottal closure instants (GCI) of the speech signal have to be detected and for each GCI synchronously windowed speech frame, the roots of the z-transform are computed and separated in two subsets based on their modulus: the roots with modulus greater than 1 (i.e., outside the unit circle) and the roots with modulus lower than 1 (i.e., inside the unit circle). According to this representation, the first subset of roots corresponds to the anticausal part of the voice source and the other to the causal part of source and vocal tract. Then, computing DFT for each of these groups, the corresponding spectrum is obtained. Finally, using IDFT, the estimation of the glottal source and the vocal tract filter are obtained. An example of this decomposition is shown in Figure 4.16.

A block diagram of the ZT decomposition algorithm is shown in Figure 4.17.

<sup>8</sup> See Appendix A for mathematical details.

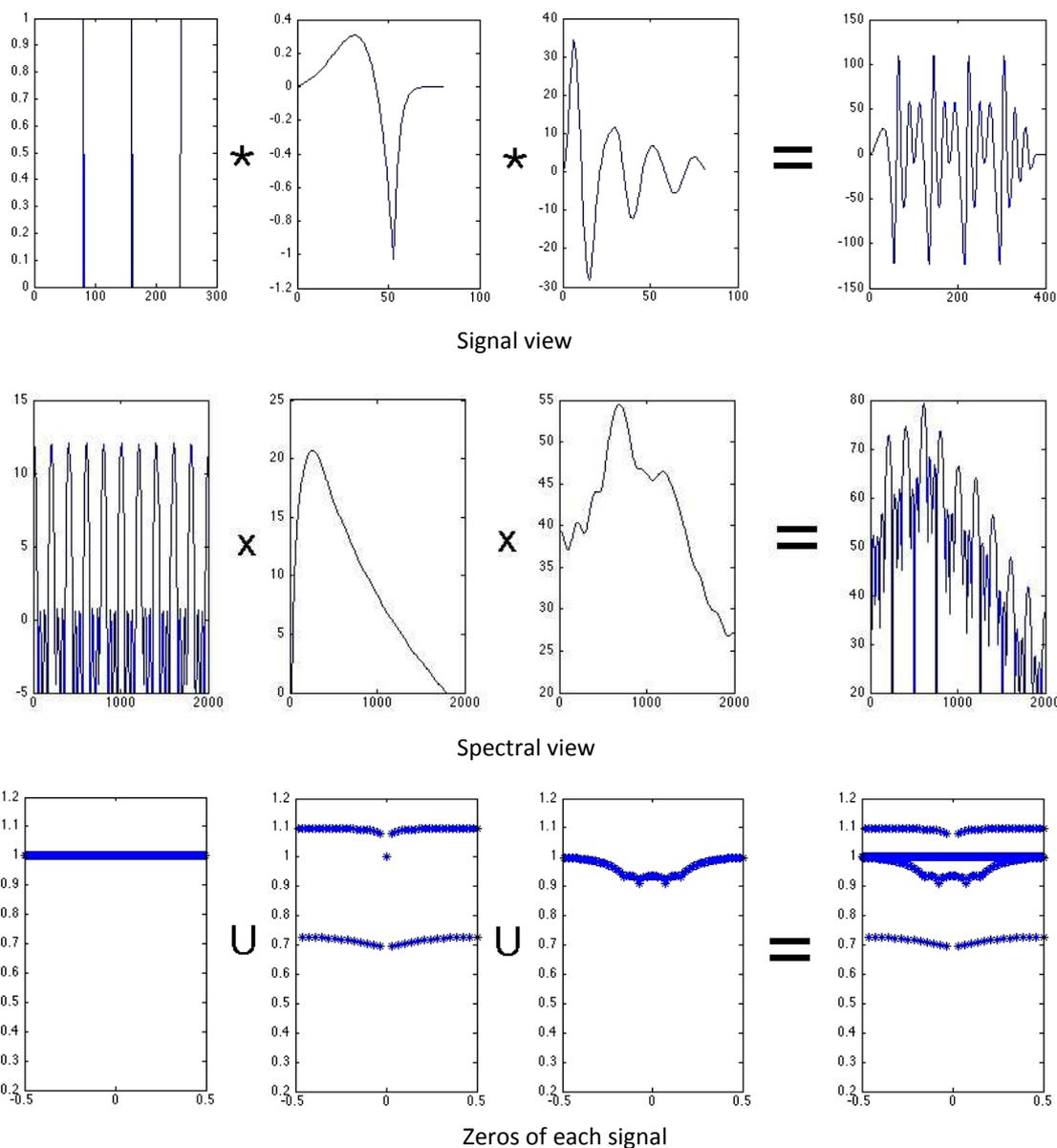


Figure 4.15. The ZTZ of a speech signal [SAD07].

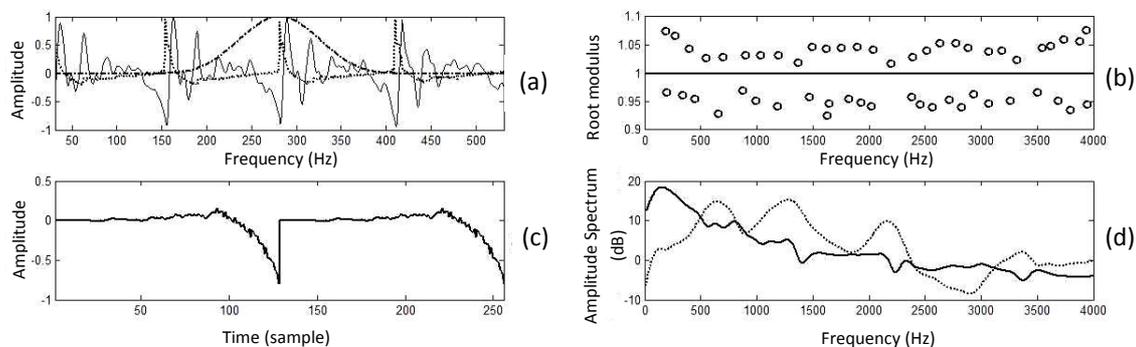
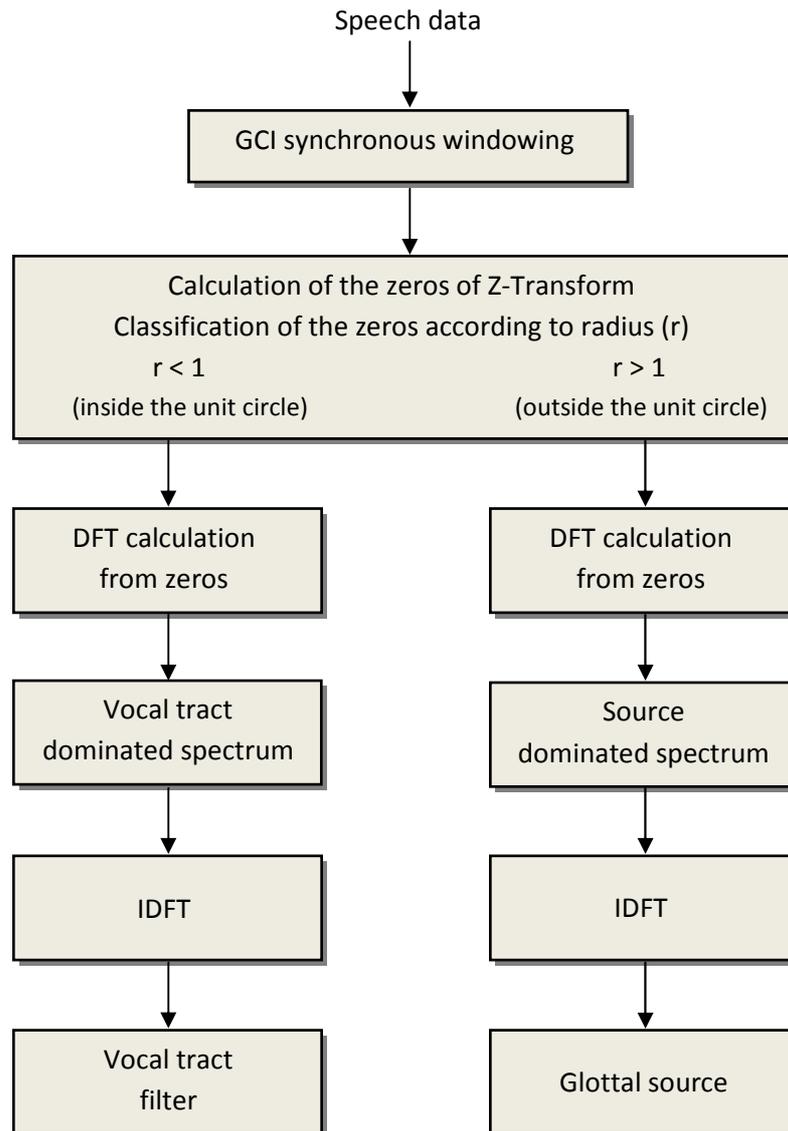


Figure 4.16. Example of decomposition on a real speech segment using Causal-Anticausal decomposition. (a): the speech signal (solid line) with the synchronized dEGG (dotted line) and the applied window (dash-dotted line); (b): the zero distribution in polar coordinates; (c): two cycles of the maximum-phase component; (d): amplitude spectra of the minimum (dotted line) and maximum-phase (solid line) components of the speech signal [Dru11].



**Figure 4.17.** Block diagram of the ZT decomposition algorithm.

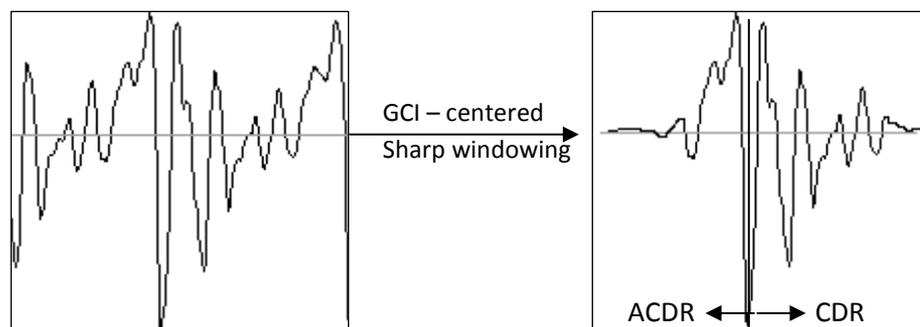
Despite the simplicity of the ZT decomposition algorithm, the need of finding roots of high degree polynomials makes it computationally heavy [BDA<sup>+</sup>05]. Also, windowing the speech signal is very critical, because the exact determination of the GCI instants of a speech signal is still an open problem and this seems to influence quite strongly the zeros computation.

In 2009, Drugman *et al.* [DBD09] proposed a method, called Complex Cepstrum-based Decomposition (CC) based on the same principles of the ZT decomposition, i.e., the speech signal is a mixed-phase signal where the maximum-phase contribution is related to the glottal open phase and the minimum-phase is related to the glottis closure and the vocal tract component (Figure 4.16). This approach has a clear advantage: computationally it is much faster than the ZT.

This decomposition is based on the fact that the complex cepstrum of an anticausal signal and causal signal is zero for, respectively, all  $n$  positive and negative. Thus, if one considers only the negative part of the CC, it is possible to estimate the glottal contribution.

According to the authors, a difficulty of CC implementation is the estimation of the phase because requires an efficient phase unwrapping algorithm and the windowing is still a critical issue in this approach.

In 2008, Thomas Drugman *et al.* [DDM<sup>+</sup>08] proposed a new approach for glottal source estimation directly from the speech signal. This method uses the knowledge mentioned above, that GCI marks the separation between the glottal open and closed phases, which correspond, respectively, to the anticausal and causal signals. Thus, the causality and anticausality dominated regions are delimited by GCI and, according to the authors, the Anticausality Dominated Region makes a good approximation of the glottal open phase, since the causal contribution, i.e., the glottal source return phase and the vocal tract filter have almost no contribution before GCI. This approach requires a GCI-centered and sharp window (typically a Hanning-Poisson or Blackman window<sup>9</sup>), as it is illustrated in Figure 4.18.



**Figure 4.18.** Effect of a sharp CGI-centered windowing on a two-period long speech frame. The Anticausality Dominated Region (ACDR) approximates the glottal source open phase and the Causality Dominated Region (CDR) the source return phase and the vocal tract filter ([DDM08]).

<sup>9</sup> See Appendix A for mathematic details.

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## 4.5. EVALUATION OF THE ESTIMATION OF THE GLOTTAL FLOW

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Even though the estimation of the glottal flow is not a trivial process, the validation of the method and the evaluation of the quality of the estimations, namely in real speech signals, is other difficult problem since it is uncertain how the real shape of the glottal flow of real speech signals looks like without using special equipment and invasive procedures [WM07].

In current literature, there are some researchers that make a qualitative evaluation of the glottal flow waveform estimations based on some demonstrative pictures and compare them with the original glottal flow when is known, as in synthetic signals (e.g., [Boz05], [Deg10]) or with the ones obtained using other techniques and, thus, evaluate the quality of each procedure. However, in this last case, for real speech signals, it is difficult to determine which one is a better estimation. Also, it is difficult to know if the selected examples represent the general behaviour of those methods.

In this evaluation process, some researchers analyse the quality of the estimated glottal flow waveform using some parameters, as the glottal formant (e.g. [Dru11]), time-based parameters, as NAQ and CIQ, (e.g., [Air08a], [Dru11]) and the harmonic richness factor (e.g., [DDM<sup>+</sup>08], [Kaf10], [Dru11]), or evaluate the quality of the algorithm used calculating the error between the estimated glottal flow waveform and the input glottal waveform, when this latter is known (e.g., [Sou11], [Dru11], [Deg10]). In this case, it is common to determine the Signal to Noise Ratio (SNR), given by [Sou11]:

$$SNR = 10 \log \left( \frac{\sum_{n=1}^N \hat{g}^2(n)}{\sum_{n=1}^N (\hat{g}(n) - g(n))^2} \right) \quad (69)$$

where  $g(n)$  represents the ideal glottal pulse and  $\hat{g}(n)$  represents the glottal pulse estimation, or the spectral distortion defined as [Dru11]:

$$SD = \sqrt{\int_{-\pi}^{\pi} 20 \log \left| \frac{G(\omega)}{\hat{G}(\omega)} \right|^2 \frac{d\omega}{2\pi}} \quad (70)$$

where  $G(\omega)$  and  $\hat{G}(\omega)$  correspond to the DTFT of the original glottal pulse and to the DTFT of the estimated glottal pulse, respectively.

---

## 4.6. BRIEF RELATIVE PERFORMANCE COMPARISON

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This section reports and discusses the results obtained using some of the previously described methods in order to estimate the glottal pulse of selected speech signals, namely: the IAIF method, which is built in the Aparat software; the Javkin *et al.* method, using Inverse Filter; LPC inverse filtering, using TF32 software, and the ZTT and CC decompositions, using Matlab. Concerning the latter two methods, the GCI-centered Blackman window was used and the GCI instants were calculated using the Matlab function *dypsa* included in the Voicebox toolbox.

In this section, the evaluation of the estimations of the glottal pulse will be qualitative. The determination of a quantitative parameter (such as the SNR) to better analyse the quality of the estimated glottal flow waveforms, will be presented in the next chapter.

For this evaluation, four signals samples were selected, with normal phonation, in which one is a synthetic signal:

- a signal of a male synthetic vowel /a/ with  $F_0=110$  Hz, generated using the Voicebox Matlab toolbox and having the LF model as glottal impulse (Figure 4.19);
- a real signal of a female vowel /a/ with  $F_0=161$  Hz (Figure 4.20);
- a real signal of a male vowel /a/ with  $F_0=102$  Hz (Figure 4.21);
- a real signal of a female vowel /i/ with  $F_0=186$  Hz (Figure 4.22).

All speech signals were down-converted to 22050 Hz.

In each figure (from left to right) we show first the glottal flow waveform, for the synthetic signal, or the speech waveform, for the real speech signals. Then estimates follow using IAIF, LPC inverse filtering, Javkin *et al.* method and finally ZTT and CC decompositions, in which, as it was mentioned above, the maximum-phase component corresponds to the glottal open phase and the minimum-phase component corresponds both to the glottis closure and the vocal tract influence.

Analysing Figure 4.19, since the glottal pulse reference is available, one can conclude that the better estimations are the ones obtained using IAIF and the CC decomposition. However, only in the estimations obtained using IAIF, the Javkin *et al.* method and LPC inverse filtering, it is possible to denote the abrupt closure of the glottal pulse, often referred to in the literature. In ZTT and CC decompositions, the glottal flow derivative waveforms do not denote what corresponds to that, i.e., there is no abrupt decreasing on the negative amplitudes. Also, the estimation performed by the ZTT decomposition, has almost no positive amplitudes and,

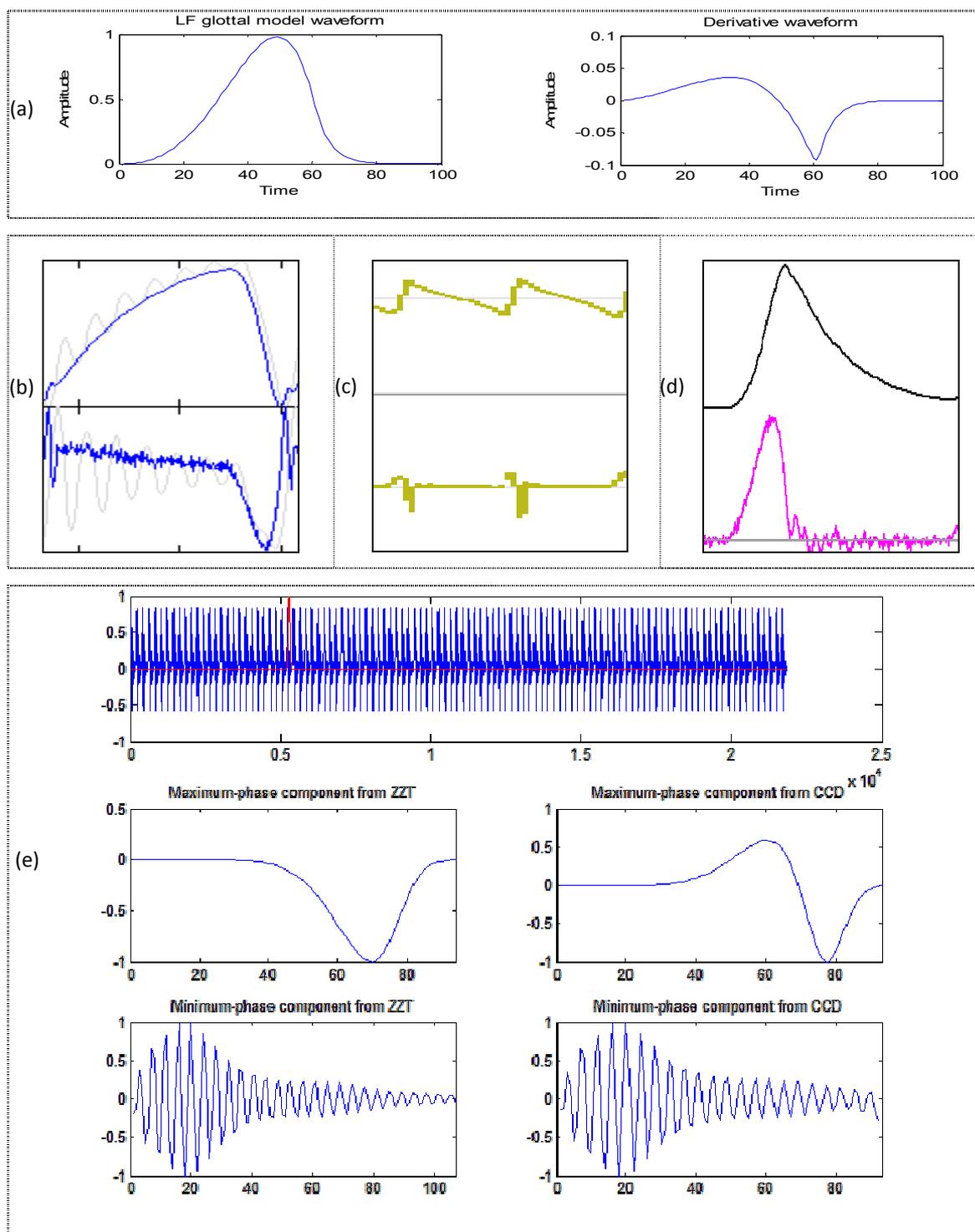
therefore, no opening glottal phase. These features may be caused by the GCI windowing issue or, simply, by the computational procedures underlying the decompositions.

It is also possible to visualize in the estimation by IAIF that the glottal impulse has almost no closed phase, contrarily to the real input glottal flow waveform.

Analysing the estimations of the glottal flow waveforms from real speech signals (Figures 4.20 to 4.22), as it was mentioned above, it is difficult to evaluate the quality of each estimation since the real glottal pulse waveform is not known. Although, what seems to be common in the approaches using IAIF, the Javkin *et al.* method and LPC inverse filtering, is the abrupt closure as well as the asymmetric and bell-shape of the glottal pulses. Also, a ripple is visible in the closed phase of the glottal flow using these methods. This is often assumed to illustrate the non-zero air flow in the closed phase or the effect of the noise when the signal was captured. Still, maybe it highlights that some part of the vocal tract filter contribution was not removed and, therefore, the estimation of the glottal flow is not correctly achieved.

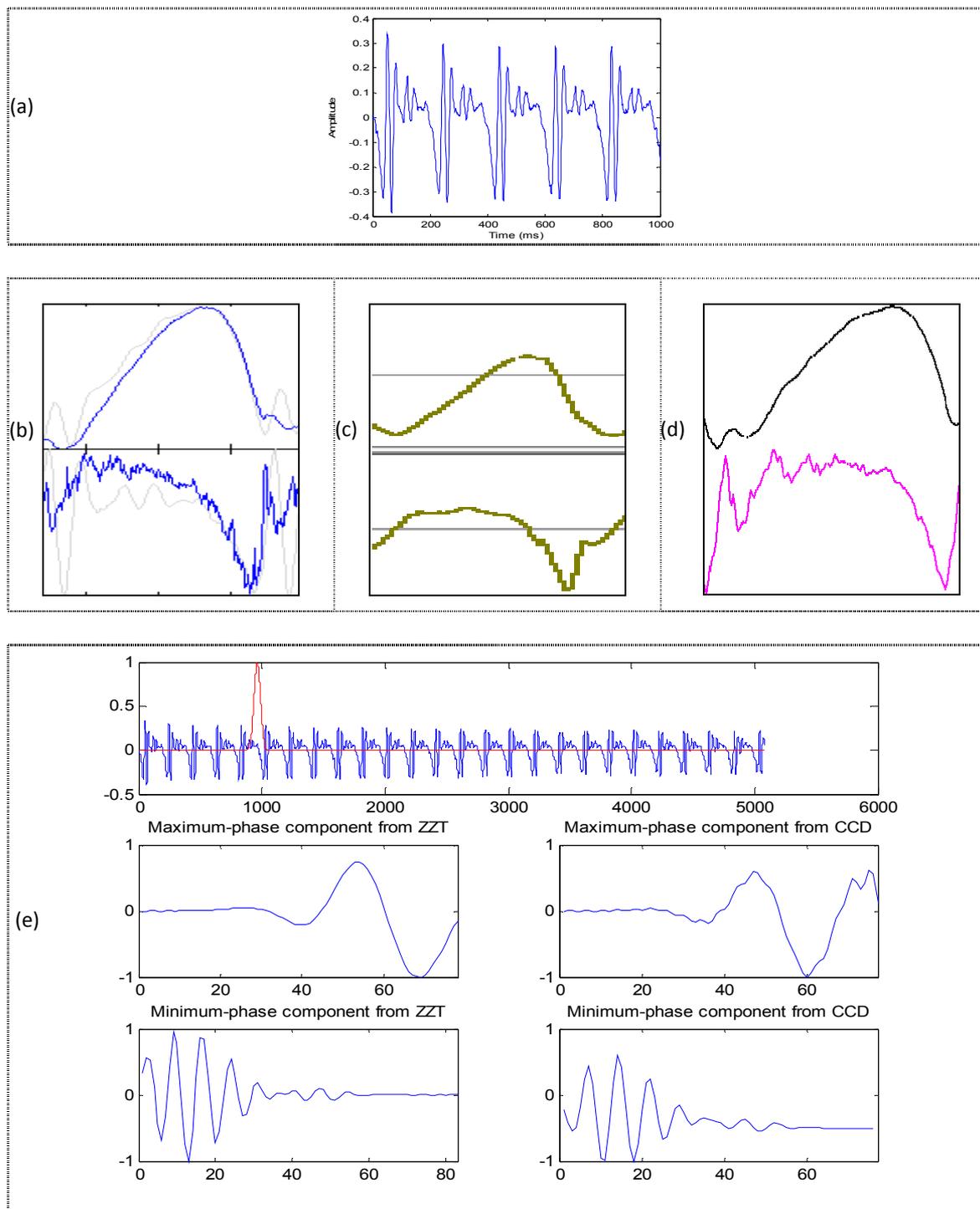
However, this closed phase is clearly visible on the estimations using the ZZT and CC decompositions, because the derivative is approximate or equal to zero in some intervals.

Our results also show that the effectiveness of the ZZT and CC decompositions appears to be similar, with a slight improvement in the latter in the case of the synthetic signal.



**Figure 4.19.** Glottal flow estimations of a male synthetic vowel /a/ using the LF model ( $F_0 = 110$  Hz).

- (a) Glottal flow waveform (left) and glottal flow derivative (right);
- (b) The glottal flow (top row) and derivative (bottom row) waveforms estimated by IAIF;
- (c) The glottal flow (top row) and derivative (bottom row) waveforms estimated by LPC inverse filtering;
- (d) The glottal flow (top row) and derivative (bottom row) waveforms estimated by Javkin et al method;
- (e) The estimation of the derivative of the glottal flow (maximum-phase component) and vocal tract contribution (minimum-phase component) using the ZT and CC decompositions. The top panel represents the speech waveform and the applied window.



**Figure 4.20.** Glottal flow estimations of a female vowel /a/.

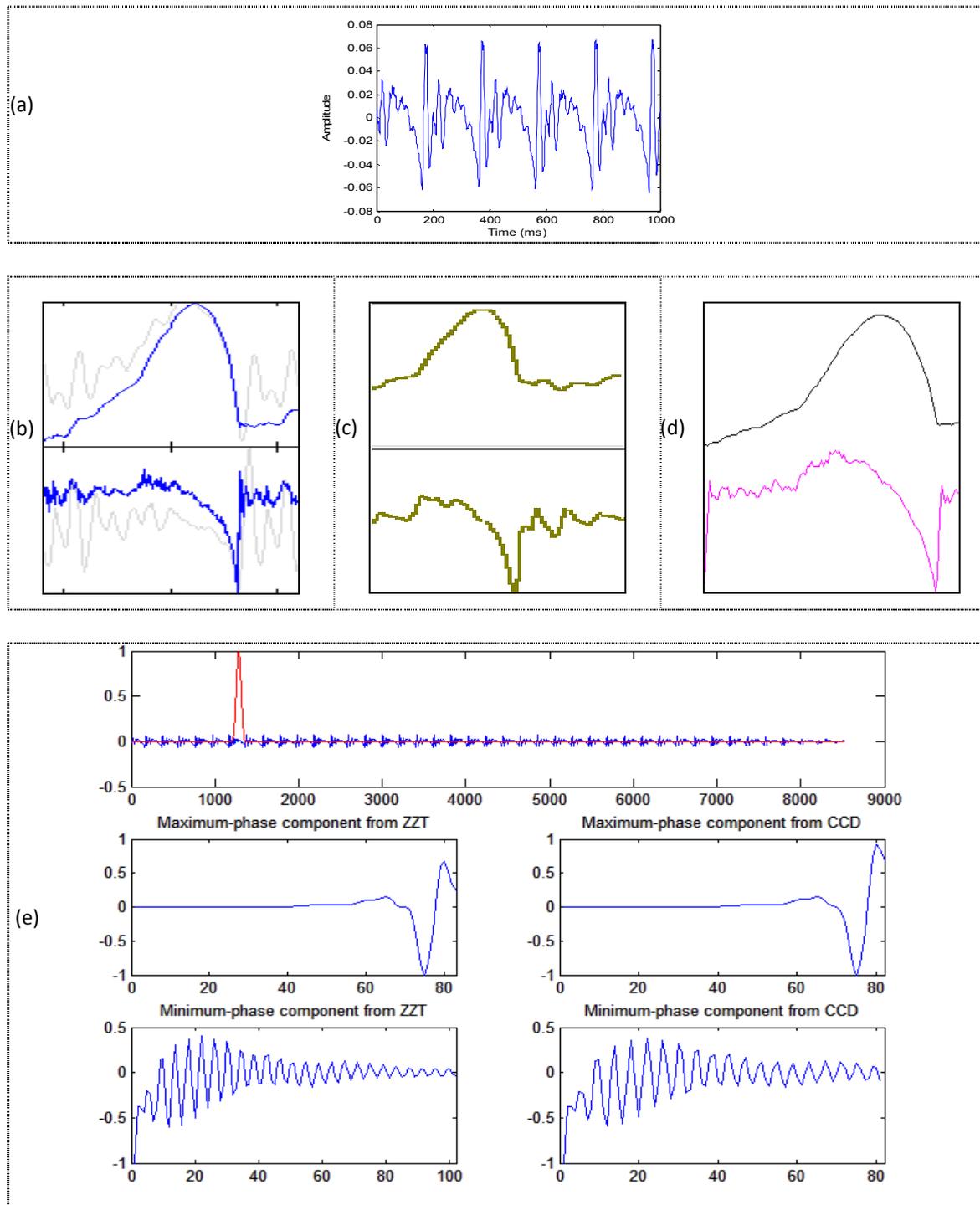
(a) Waveform;

(b) The glottal flow (top row) and derivative (bottom row) waveforms estimated by IAIF;

(c) The glottal flow (top row) and derivative (bottom row) waveforms estimated by LPC inverse filtering;

(d) The glottal flow (top row) and derivative (bottom row) waveforms estimated by Javkin et al method;

(e) The estimation of the derivative of the glottal flow (maximum-phase component) and vocal tract contribution (minimum-phase component) using the ZT and CC decompositions. The top panel represents the speech waveform and the applied window.



**Figure 4.21.** Glottal flow estimations of a male vowel /a/.

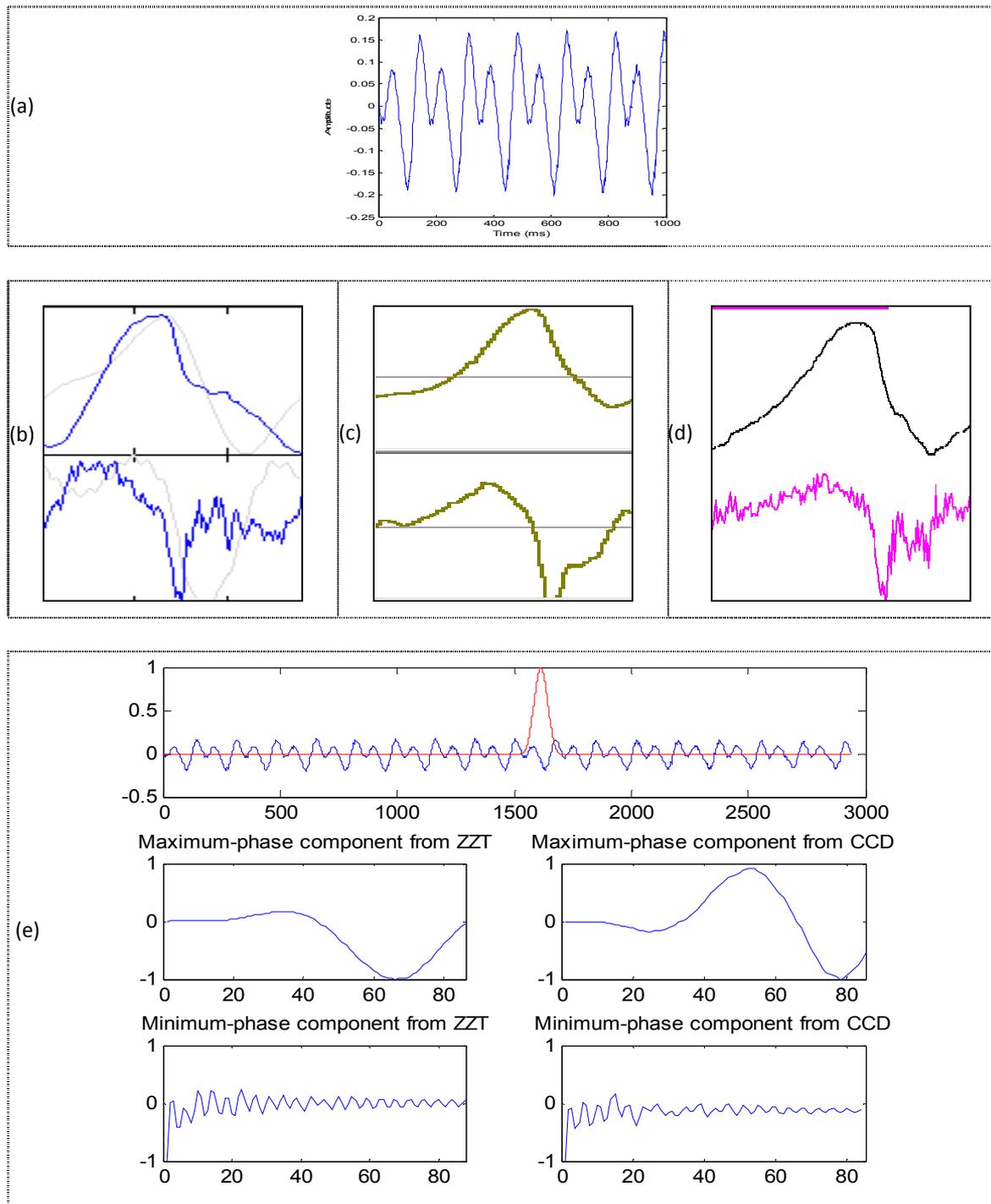
(a) Waveform;

(b) The glottal flow (top row) and derivative (bottom row) waveforms estimated by IAIF;

(c) The glottal flow (top row) and derivative (bottom row) waveforms estimated by LPC inverse filtering;

(d) The glottal flow (top row) and derivative (bottom row) waveforms estimated by Javkin et al method;

(e) The estimation of the derivative of the glottal flow (maximum-phase component) and vocal tract contribution (minimum-phase component) using the ZT and CC decompositions. The top panel represents the speech waveform and the applied window.



**Figure 4.22.** Glottal flow estimations of a female vowel /i/.

- (a) Waveform;
- (b) The glottal flow (top row) and derivative (bottom row) waveforms estimated by IAIF;
- (c) The glottal flow (top row) and derivative (bottom row) waveforms estimated by LPC inverse filtering;
- (d) The glottal flow (top row) and derivative (bottom row) waveforms estimated by Javkin et al method;
- (e) The estimation of the derivative of the glottal flow (maximum-phase component) and vocal tract contribution (minimum-phase component) using the ZZT and CC decompositions. The top panel represents the speech waveform and the applied window.

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## 4.7. SUMMARY

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The focus of this chapter was laid on the mathematical description of different procedures of estimation of the glottal pulse which included different inverse filtering techniques. Also, the glottal pulse parameterization was reviewed as well as the evaluation of glottal flow estimations.

Some of the analysed procedures and inverse filtering techniques were applied into four signals (one synthetic and three real signals) in order to estimate the glottal flow and to compare the results. The selected methods were: IAIF using the Aparat software, the Javkin *et al.* method using Inverse Filter, LCP inverse filtering using TF32, and the ZZT and CC decompositions. The IAIF and the ZZT and CC decompositions are automatic processes, although these two latter are computationally very heavy, with a slight improvement in the case of the CC decomposition. The problematic issue of windowing in these two processes (ZZT and CC decompositions) was also clear: if the window applied to the segment of the voiced speech signal is not appropriate, the correct estimation of the glottal source derivative (maximum phase component) is compromised.

The estimations by ZZT and CC methods are very close to each other, but the latter outperforms in the synthetic signal.

The results have shown that neither of these approaches is completely robust since the estimations of the glottal flow for the synthetic signal were not very close to the original waveform. However, for this signal, the IAIF and the CC decomposition seem to give the most accurate estimations.

Regarding the real signals, some features of the glottal flow were mostly common: the asymmetric and bell-shape of the glottal impulse, the abrupt closure and the quasi no-existing glottal closed phase. Only in the ZZT and CC decompositions this last feature is clearly visible, but the abrupt closure is not denoted.

As previously mentioned, the evaluation of these procedures will be complemented in the next chapter.

# Chapter 5

## FREQUENCY-DOMAIN APPROACH TO GLOTTAL SOURCE ESTIMATION

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## 5.1. INTRODUCTION

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Over the last decades several procedures were developed in order to estimate the excitation of voiced speech and most of them were implemented in the time domain. However, frequency-domain methods seem to be more robust in handling both noisy and phase distorted data [Boz05] and they also have a potential to provide a better description of the voice quality spectral parameters, to implement more efficient voice quality modification, and to perform voice source parameter estimation [DAH03].

In this chapter we present a new glottal source estimation approach that comprises frequency-domain signal analysis and synthesis, and that relies on both accurate spectral magnitude modelling and determination of the Normalized Relative Delays (NRDs) of the harmonics of the speech signal. Therefore, the NRD concept is also reviewed here. Moreover, a new frequency-domain model of the glottal excitation combining features of the LF and Rosenberg models is devised.

Our approach also results from a set of experiments conducted with the collaboration of an otorhinolaryngologist. A tiny and high-quality microphone was attached at the tip of a rigid video laryngoscope, and was used as in a conventional laryngoscopy exam. An identical microphone was put outside the mouth in order to record two time-aligned acoustic signals: a glottal source signal captured as close as possible to the vocal folds, and the corresponding voiced signal captured outside the mouth. The aim of capturing these signals was to model the spectral magnitude and the group delay of the glottal source and the voiced signals, corresponding to each one of the vowels /a/ and /i/. This clarification was essential to the complete design of a new approach to glottal source estimation.

The proposed approach to glottal source estimation will be validated using several speech signals (synthetic and real) and the results will be critically compared with the ones obtained using others estimation processes representative of the state of the art: IAIF and CC decomposition.

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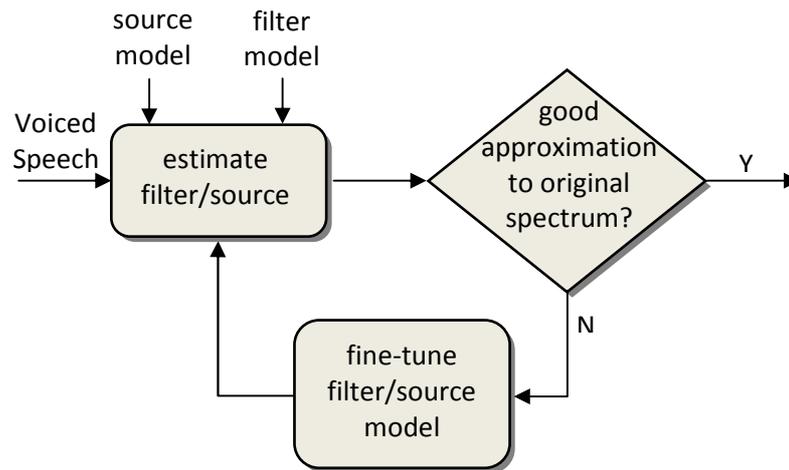
## 5.2. GENERAL OVERVIEW AND APPROACH

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Most of the techniques of estimation of the glottal source are based on the source-filter model and, thus, have a model for the vocal tract transfer function in order to eliminate the effect of the vocal tract filter and to cancel the lip/nostrials radiation from the speech signal. In the literature, most often, as it was discussed in chapter 3, the vocal tract filter is modelled as an all-pole filter that shapes the spectrum of the source according to the resonances of the vocal tract, and the lip/nostrials radiation is typically modelled as a first-order discrete-time derivative operator of the pressure wave at the output of vocal tract. This operation converts volume velocity of the air flow into sound pressure variation, the physical quantity captured by a microphone. Thus, the glottal pulse inverse filtering requires a first-order integration operation in order to eliminate the lip/nostrials radiation from the speech signal. Most of the inverse filtering techniques implement this operation in time domain (e.g., IAIF, PSIAIF, inverse filtering method proposed by Murphy [Mur08]), but as we stated in [DSF11], it motivates two sources or approximation errors: a first error is due to the first-order differentiator, since the frequency response clearly differs from the frequency response of an ideal differentiator, especially at high frequencies; a second error is due to the inverse transfer function of the first-order differentiator, in order to avoid the pole at  $z=1$  and to insure stability. In fact, as described in section 3.2, a typical difference equation used in the integration procedure is  $y[n] = (1 - \alpha)x[n] + \alpha y[n-1]$  [JBM87], however this solution introduces signal distortions and it is sensitive to noise.

In our research, we first idealized a frequency-domain approach to glottal source estimation which would implement the signal integration in the frequency domain, in order to eliminate the lips/nostrials radiation from the speech signal, and then start with some default source or filter models or even with a first filter estimate from the harmonic-noise decomposition of the voice signal. Then, iteratively and using analysis-by-synthesis, the best combination of source and filter spectra matching the spectrum would be found. This is illustrated in Figure 5.1.

The main steps in this procedure are the analysis and resynthesis. The first is responsible for the estimation of the sinusoidal components in the signal and their parameterization (frequency, magnitude and phase), and then for removing these from the magnitude spectrum, giving rise to the noise residual. The second is responsible for selectively synthesizing the residual only, the sinusoidal components only, or any magnitude/phase modification affecting a specific sinusoidal or noise component.



**Figure 5.1.** Initial idea for analysis by synthesis approach to filter/source fine-tuning.

However, with the development of our research, this glottal source estimation model was reformulated and, in particular, does not implement the speech signal integration step, since it is implicit in the procedure, as it will be explained in the following sections.

Nevertheless, since the signal integration is common in most glottal source estimation procedures and usually implemented in the time domain, we will review in the next section that it is possible and advantageous to implement this operation in the frequency domain [DSF11].

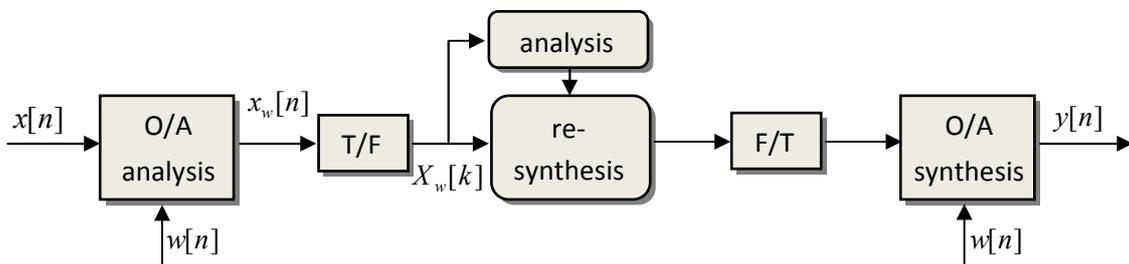
Despite speech signals are strongly studied over the years, most often the phase information is ignored. However, recent studies (e.g. [SF10], [BNG06], [Boz05], [Dru11], [MY11]) have shown the importance and the pertinence of using this information in order, for example, to identify the perceptual signature of a periodic sound, or to obtain a higher quality speech synthesis or even to extract other speech features, as the Normalized Relative Delay (NRD). This feature expresses the delay between the harmonics relative to the fundamental of a periodic signal and denotes the phase contribution to the shape invariance of a periodic signal. The NRD concept and its computation will be thoroughly described in section 5.2.2.

According to Sousa and Ferreira [SF10], the NRD feature can be used in identifying the phonation type (pressed, normal and breathy), and also allows the analysis and synthesis of a desired harmonic synchronization, independently of the overall time shift of the signal and of its fundamental frequency. Therefore, NRDs, in addition to magnitude information, are also powerful features because they allow to characterize completely the time waveform of a speech signal, which is essential in the analysis-synthesis of our glottal source estimation process. In fact, one of the main results of our research was that, for sustained vowels /a/ and /i/, it is possible to estimate the NRDs corresponding to the glottal source signal using simply a

compensation of the NRDs of the speech signal. Thus, having a default model of the glottal pulse and also estimating the magnitude of the spectral peaks of the glottal pulse from a smooth spectral envelope model of the voice signal, it is possible to synthesize the estimated glottal pulse. This is the main idea of our glottal source estimation.

### 5.2.1. SIGNAL INTEGRATION IN THE FREQUENCY DOMAIN

As highlighted in [DSF11], the signal integration can be accurately implemented in the frequency domain. Our processing framework is represented in Figure 5.2.



**Figure 5.2.** Analysis-synthesis processing framework. O/A denotes Overlap-and-Add, T/F denotes Odd-DFT transformation and F/T denotes Inverse Odd-DFT.

According to this figure, in our framework:

1. the processing is frame-based using a segmentation based on a window  $w[n]$  whose length is  $N$  samples, and using 50% overlap between adjacent frames at the analysis, and 50% overlap-and-add between adjacent frames at the synthesis;
2. the time-frequency transformation is based on the Odd-frequency discrete Fourier transform (Odd-DFT)<sup>10</sup>;
3. using an appropriate window  $w[n]$  and without any spectral modification, the system is perfect reconstructing, i.e.,  $y[n] = x[n - n_d]$  where  $n_d$  is a constant system delay. In

particular, if  $w[n] = \sin\left[\left(n + \frac{1}{2}\right)\frac{\pi}{N}\right]$ , then  $n_d = N - 1$ .

The Odd-DFT has several advantages over the plain DFT, including the fact that when its length  $N$  is even and the signal is real,  $N/2$  coefficients are unique instead of  $N/2 + 1$ , and that when it is used with other windows than the rectangular window, several interesting properties can be taken advantage of, including DC power concentration and accurate sinusoidal analysis ([Fer01], [FS05]).

<sup>10</sup> See Appendix A for mathematical details.

Let us consider a continuous signal  $x_c(t)$  and  $x[n]$  the signal obtained by sampling  $x_c(t)$  in the time domain, i.e.,  $x[n] = x_c(nT_s)$ , where  $T_s = 1/F_s$  represents the sampling period, the reciprocal of the sampling frequency  $F_s$ .

In order to have the signal segmentation, as illustrated in Figure 5.2, a windowing step is implemented. Therefore,

$$x_w[n] = x[n] \cdot w[n] \xleftrightarrow{F} \frac{1}{2\pi} X(e^{j\omega}) * W(e^{j\omega}) \quad (71)$$

Taking the Odd-DFT of  $x_w[n]$ , the time-frequency transformation is obtained:

$$X_w[k] = \sum_{n=0}^{N-1} x_w[n] e^{-j\frac{2\pi}{N}(k+\frac{1}{2})n} \quad (72)$$

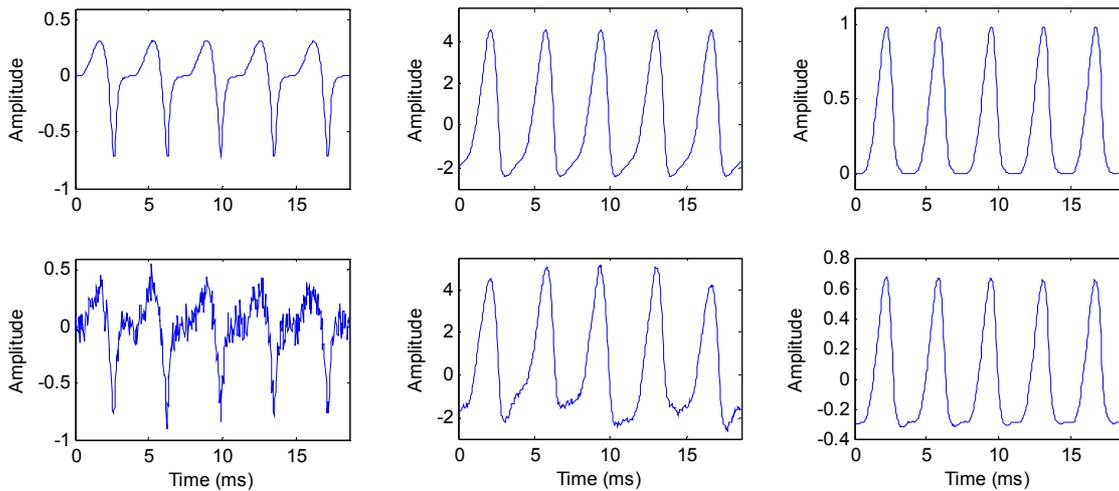
where  $N$  is the length of the transform. This implies that, for analysis and synthesis purposes, the spectral information that we have access is discrete, i.e., for  $k = 0, 1, \dots, N-1$ :

$$X_w[k] = X_w(e^{j\omega}) \Big|_{\omega = \frac{2\pi}{N}(k+\frac{1}{2})} \quad (73)$$

Following the accurate estimation of the frequency, magnitude and phase of all the identifiable sinusoids in the  $X_w[k]$  spectrum [Fer01], resynthesis of these sinusoids can take place with any desired modification, generating a new spectrum vector  $X_w[k]$ . For example, signal integration in the time domain is achieved by modifying  $X_w[k]$  as:

$$Y_w[k] = \frac{X_w(k)}{jF_s 2\pi(k+0.5)/N}, \quad k = 0, 1, \dots, N-1. \quad (74)$$

In order to illustrate some of the pitfalls of the integration in time domain, we present in Figure 5.3 a comparison between the integration in the time domain and in the frequency domain of the LF derivative glottal pulse without noise and with white noise at 9 dB SNR. It is clear that the output results of the integration implemented in the frequency domain (according to the algorithm of Figure 5.2 and the modification defined by equation (74)) are faithful reconstructions of the LF waveform. Furthermore, even when the input signal is a noisy derivative of the LF glottal pulse, the output is still a correct reconstruction of that model. In this last case, during the resynthesis, the high-frequency components of the derivative of the glottal model disappear due to the noise, generating the artifacts that are visible on the closed phase of the glottal model. Nevertheless, the noise has markedly less impact in this output than in the one obtained using the time-domain integration according to  $y[n] = (1-\alpha)x[n] + \alpha y[n-1]$ .



**Figure 5.3.** Time representation of the derivative of the LF glottal waveforms without noise (top left figure) and with white noise at 9 dB SNR (bottom left figure), and the corresponding output results of a first-order time-domain integrator (center) and of a frequency-domain integrator (right figure).

As discussed in detail in [DSF11], for both cases, the signal integrations implemented in the frequency domain are significantly superior to the ones implemented in the time domain, which highlight its advantages.

### 5.2.2. NORMALIZED RELATIVE DELAY CONCEPT

According to Bozkurt [Boz05], research developed during the last years showed that phase plays an important role in speech perception, contrarily to early research which stated that the human ear is insensible to phase. Also, recent studies (e.g., [SF10], [SF11], [MY11]) have shown that phase information from the speech signal has important applications in speech analysis and synthesis. However, the phase spectrum is frequently ignored and there are few studies that use this feature for parameter estimation purpose, when compared to amplitude based parameter estimation methods.

As previously mentioned, in our framework phase-related features are used that are based on the NRDs of the spectral harmonics of the glottal source. Therefore, the NRD concept is explained here.

Let us admit a periodic signal  $x[n]$  consisting of  $L$  sinusoids harmonically related according to a fundamental frequency  $\omega_0$ .

Therefore [SF10],

$$\begin{aligned}
x[n] &= A_0 \sin(n\omega_0 + \phi_0) + \sum_{l=1}^{L-1} A_l \sin(n\omega_l + \phi_l) \\
&= A_0 \omega_0 \sin(n + n_0) + \sum_{l=1}^{L-1} A_l \omega_l \sin(n + n_l)
\end{aligned} \tag{75}$$

where  $A_l$ ,  $\omega_l$ ,  $\phi_l$  and  $n_l$  denote, respectively, the magnitude, the frequency, the phase and the time delay of the  $l^{\text{th}}$  sinusoid to a reference point in  $n$ . When  $x[n]$  is multiplied by a time window before using the Odd-DFT time to frequency-domain transformation, the time reference point depends on the time window used. Usually the window is even symmetric and the reference point corresponds to the center of the window, i.e., it corresponds to the group delay of the filter whose impulse response is the time window. If  $X[k]$  denotes the complex Odd-DFT transform, of length  $N$ , of  $x[n]$  after windowing, then the phase of  $X[k]$  represents the time delay  $n_k$  relative to the center of the window [SF10]. This implies that the independent variable  $n$  can be ignored in equation (75), which is equivalent to making  $n = 0$ , and [SF10]:

$$\begin{aligned}
x &= A_0 \sin(\omega_0 n_0) + \sum_{l=1}^{L-1} A_l \sin(\omega_l n_l) \\
&= A_0 \sin\left(2\pi \frac{n_0}{P_0}\right) + \sum_{l=1}^{L-1} A_l \sin\left(2\pi \frac{n_l}{P_l}\right) \\
&= A_0 \sin\left(2\pi \frac{n_0}{P_0}\right) + \sum_{l=1}^{L-1} A_l \sin\left(2\pi \frac{n_0 + n_l - n_0}{P_l}\right) \\
&= A_0 \sin\left(2\pi \frac{n_0}{P_0}\right) + \sum_{l=1}^{L-1} A_l \sin\left(2\pi \left(\frac{n_0}{P_l} + \frac{n_l - n_0}{P_l}\right)\right) \\
&= A_0 \sin\left(2\pi \frac{n_0}{P_0}\right) + \sum_{l=1}^{L-1} A_l \sin\left(2\pi \left(\frac{n_0}{P_l} + NRD_l\right)\right)
\end{aligned} \tag{76}$$

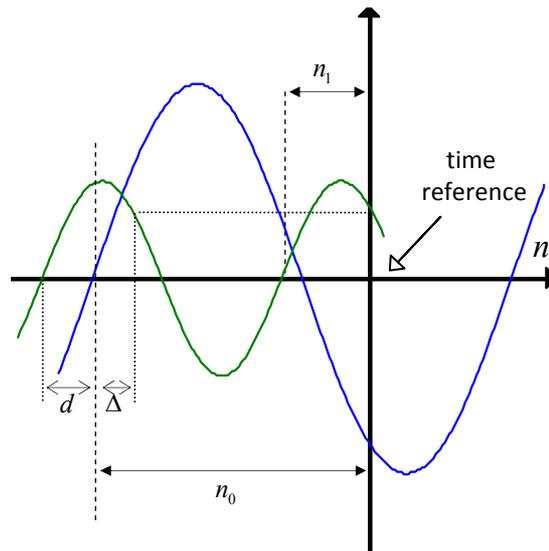
where  $n_l$ ,  $P_l$  and  $NRD_l$  are given as

$$n_l = \frac{\phi_l}{\omega_l} \tag{77}$$

$$P_l = \frac{2\pi}{\omega_l} \tag{78}$$

$$NRD_l = \frac{n_l - n_0}{P_l}. \tag{79}$$

In equation (76),  $P_l$  represents the period of the  $l^{\text{th}}$  harmonic sinusoid and  $NRD_l$  denotes the relative delay difference between the  $l^{\text{th}}$  harmonic and the fundamental frequency sinusoid. This latter is illustrated in Figure 5.4.



**Figure 5.4.** Illustration of the relative delay  $d$  between a harmonic of a fundamental frequency sinusoid, whose delay to a time reference is  $n_1$ , and the fundamental frequency sinusoid, whose delay to a time reference is  $n_0$  [SF10].

As it can be seen in Figure 5.4,  $n_0$  is equal to  $\Delta$  plus an integer number of periods of the

harmonic sinusoid that fit within  $n_0$ . Therefore,  $n_0 = \Delta + \left\lfloor \frac{n_0}{P_1} \right\rfloor P_1$ , where  $\lfloor \cdot \rfloor$  represents the

largest integer, and the relative delay  $d$  is  $d = n_1 - \Delta = n_1 - n_0 + \left\lfloor \frac{n_0}{P_1} \right\rfloor P_1$ . If  $d < 0$ , then the

relative delay is  $d' = d + P_1$  so that  $d'$  is a positive number less than  $P_1$ . In order to obtain a normalized value, i.e.,  $0 \leq d \leq 1$  (or  $0 \leq d' \leq 1$ ),  $d$  (or  $d'$ ) is divided by  $P_1$  and it corresponds to the NRD.

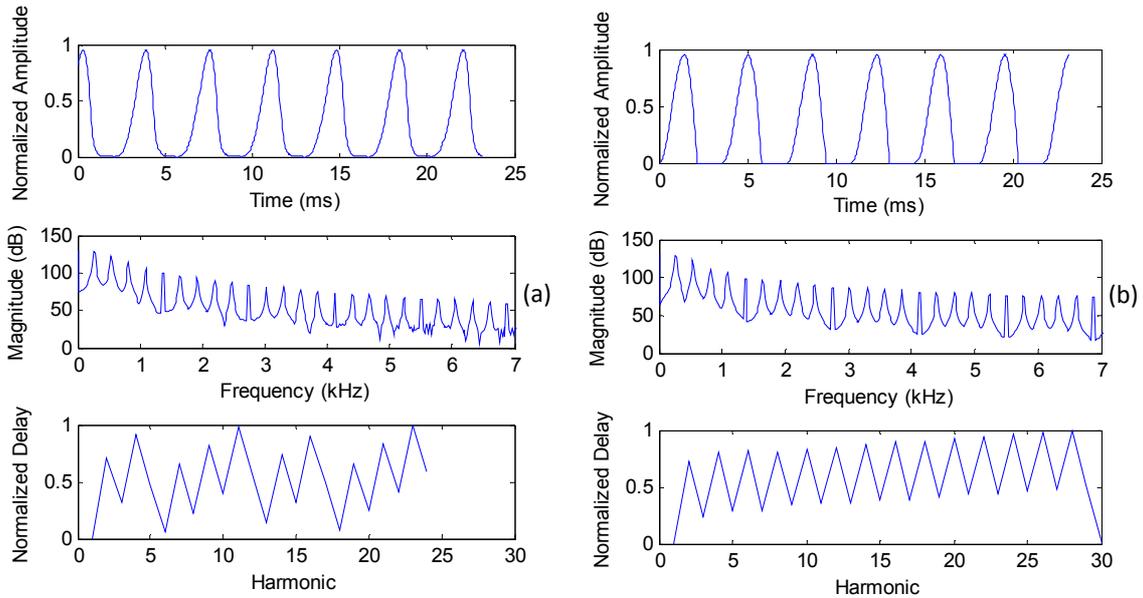
Figure 5.5. illustrates the algorithm used for the estimation of the NRDs parameters: given a signal  $x[n]$ , the first step is to implement segmentation and windowing, using the Sine Window<sup>11</sup>, and then the Odd-DFT transformation is used to transform the signal to the frequency domain. The following step involves analysing the resulting spectrum in order to identify the most relevant harmonic structure of sinusoids and, based on this, accurately estimate the magnitude and phase of each sinusoid relative to the center of the time analysis window [Fer01].

In Figure 5.6 two synthetic signals corresponding to the LF and Rosenberg glottal waveforms are represented, which were generated using the Voicebox Matlab toolbox. Their magnitude spectrum and the estimated NRD coefficients are also represented corresponding to the first 24 and 30 harmonics, respectively.

<sup>11</sup> See Appendix A for mathematic details.



**Figure 5.5.** Algorithm implementing the estimation of the NRD parameters and overall time shift ( $n_0$ ) of the waveform [SF10].



**Figure 5.6.** (a) - Time representation of the LF glottal flow model (top row), its magnitude spectrum (middle) and NRD representation (bottom row).  
 (b) - Time representation of the Rosenberg glottal flow model (top row), its magnitude spectrum (middle) and NRD representation (bottom row).

It is clear, from Figure 5.6, that the NRD representation is regular and wrapped and the unwrapping leads to a straight line, as it will shown below. Also, the first NRD coefficient is always zero since it corresponds to the reference delay of the fundamental frequency.

Another important note is that, despite the similarities between the glottal flow waveforms and the magnitude spectra of these two signals, the NRDs coefficients are clearly different which suggests that the NRD possesses relevant information. In fact, Sousa and Ferreira [SF10] state that NRD features are phase related LF only and correlate significantly with perceptual information. Moreover, we have shown [DSF11] that it is possible to implant the magnitude and NRD models on a periodic signal with the same fundamental frequency, since these two features (the relative magnitude and NRDs between all relevant upper harmonics and the fundamental frequency) completely define a wave prototype. Therefore, this procedure has potentialities to contribute to an accurate glottal source estimation, which will be used in our glottal source estimation process.

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### 5.3. PHYSIOLOGICAL SIGNAL ACQUISITION FOR SOURCE AND FILTER MODELLING

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In order to accurately estimate the glottal source from a speech signal and since its contribution is not directly observable in the speech waveform captured through a microphone outside the mouth, we devised a technique, after consulting several specialists concerning viability, feasibility, ethical and technical aspects, with the purpose to capture two time-aligned acoustic signals: the source signal as close as possible to the vocal folds and the corresponding voiced signal outside the mouth. That would allow us to characterize:

- the source signal, and compare the results with ideal (i.e., mathematical) existing models, such as the LF and Rosenberg models, whose correspondence to physiological data is not clear;
- the frequency response of the vocal tract filter, namely regarding the group delay.

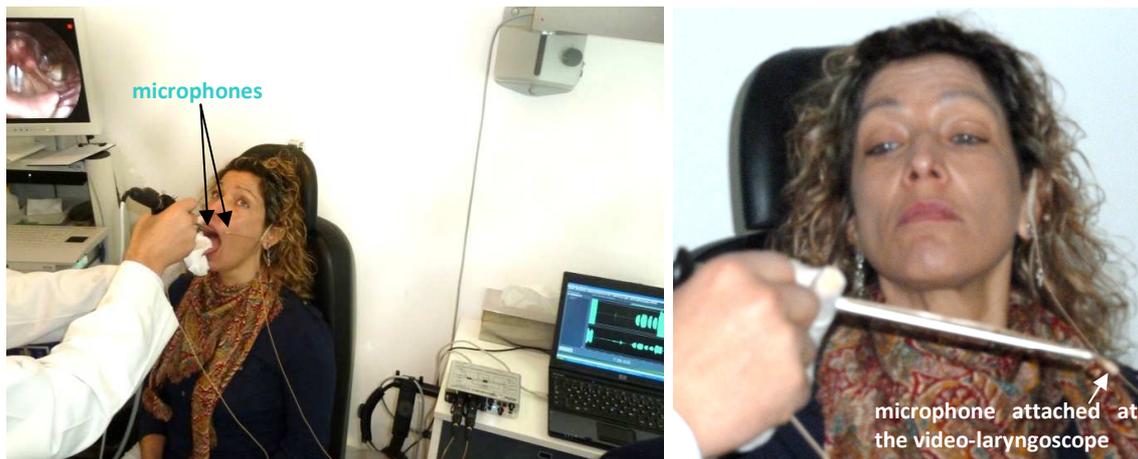
Based on these characterizations, it would be possible to design a robust frequency-domain approach for glottal source estimation, which is the main goal of our research. Also, we would know how the real shape of the glottal flow looks like and that would allow us to evaluate the quality of the estimation of the glottal source, and compare these estimations with the ones obtained using other state-of-the-art glottal flow estimation methods, as discussed in chapter 4.

This experimental procedure was carefully planned and conducted with the collaboration of an otorhinolaryngologist (ORL). We attached a tiny and high-quality microphone (of the ear-worn type) at the tip of a rigid video laryngoscope and another similar microphone was used to capture the signal outside the mouth. The literature recommendations about acquisition of voice signals [Tiz94] were followed, namely the distance to the mouth of this latter microphone was held constant, less than 10 cm (about 3 or 4 cm) and off-axis positioning ( $45^\circ$  to  $90^\circ$  from the mouth axis), as well as the equipment characteristics, as specified below.

The recording sessions took place during conventional video laryngoscopy examinations, in a quiet room, and the ORL professional acted in order to capture the glottal source signal as close as possible to the glottis, while insuring safety and ethical conditions for all volunteer subjects. The acoustic signals were recorded simultaneously with an A/D interface and audio recorder. Figure 5.7 illustrates the procedure and the equipment involved.

The equipment used in this experimental procedure was:

- a rigid video laryngoscope with 7 mm diameter and length of 180 mm (Xion);



**Figure 5.7.** Laryngoscopic exam and voice signal acquisition. On the left picture, one microphone is visible outside the mouth and a similar microphone is attached at the tip of the rigid laryngoscope (visible on the right picture) and put near the vocal folds (represented in the screen at the topright side of the left picture). The A/D interface and audio recorder are displayed at the bottom-right side of the left picture.

- two ear-worn omnidirectional pre-polarized condenser microphones, with a frequency response from 20 Hz to 20 KHz, maximum of 143 dB of SPL, and 3.3 mm of diameter of the microphone capsule (Sennheiser Ear Set 1 microphones);
- two phantom power adaptors (XLR to 3.5 mm mini-jack plug) for pre-polarized condenser microphones (Sennheiser MZA-900P);
- a stereo 24-bit/96 kHz A/D and D/A interface with phantom power, XLR inputs and USB PC connector (Cakewalk-Roland UA-25EX);
- Adobe Audition audio recorder/editor (Adobe).

Before undertaking a large data collection, we decided to use first only two subjects (a male and a female), with no voice disorders, with the purpose to assess any requirements and considerations that should be addressed or adjusted when implementing the same experimental procedure with the rest of the subjects in our data set and, perhaps, to bigger groups in the future.

For this experience some assumptions were made:

- six adult volunteer subjects (Table 5.1) participated, three of each gender and with ages from 22 to 54 years old;
- all subjects have healthy voices, i.e., no voice disorders;
- five subjects are from Portugal and the other is from Brazil, with Portuguese being their mother tongue;
- the subjects uttered (the back and front) common Portuguese vowels /a/ and /i/.

**Table 5.1.** *Characterization of the volunteer subjects.*

Subject	Gender	Age	Occupation
AF	Male	48	Teacher
RT	Male	54	Teacher/Tenor
PP	Male	22	Speech Therapist
SD	Female	31	Teacher
SF	Female	33	Teacher/Speech Therapist
CK	Female	49	Singer

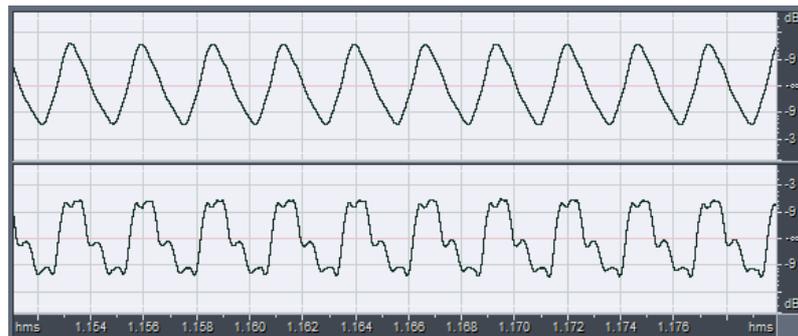
The choice of the sustained vowels /a/ and /i/ was because they represent a relatively stable condition of the phonatory system [GA05] and in their production there is a minor vocal tract influence in the glottal source, which may justify that these are maybe the most used vocal stimuli in speech studies [Sou11].

The same procedure and equipment was used for all subjects. However, some differences on the signal acquisition near the glottis were detected and were concluded to be subject dependent mainly due to the anatomy and subject collaboration. To minimize these aspects, we have made several records for each subject in order to select afterwards the ‘best’ signals, i.e., those which were captured closest to the vocal folds.

A first conclusion from this experimental procedure was that the quality of the acoustic signal captured near the glottis depended significantly on the proximity of the microphone to the epiglottis, since if too far, the influence of the vocal tract resonances was clearly perceptible.

After the recording sessions, we selected two representative segments of the time-aligned acoustic signals, using the audio editor, for each subject and vowel. These 24 time-aligned signals stereo, 16 bit, WAV files (thus, 48 acoustic signals) are about 2 seconds long and represent the data in our database.

Figure 5.8 shows one of these signals in which it is possible to observe that the waveform of the signal captured near the vocal folds does not denote the classic and ideal glottal pulse since the closed phase is not clear. However, as stated before, the existence of the closed phase is an idealistic assumption and the majority of the individuals have some glottal leakage during that phase [Cin08], as it is noticeable in Figure 2.2.



**Figure 5.8.** Time-aligned speech signals for vowel /i/ by a male subject: the signal captured near the vocal folds (top row) and the signal captured outside the mouth (bottom row).

The original recording sampling frequency was 48000 Hz but the files were down-converted to 22050 Hz in order to facilitate subsequent processing, namely in terms of spectral analysis.

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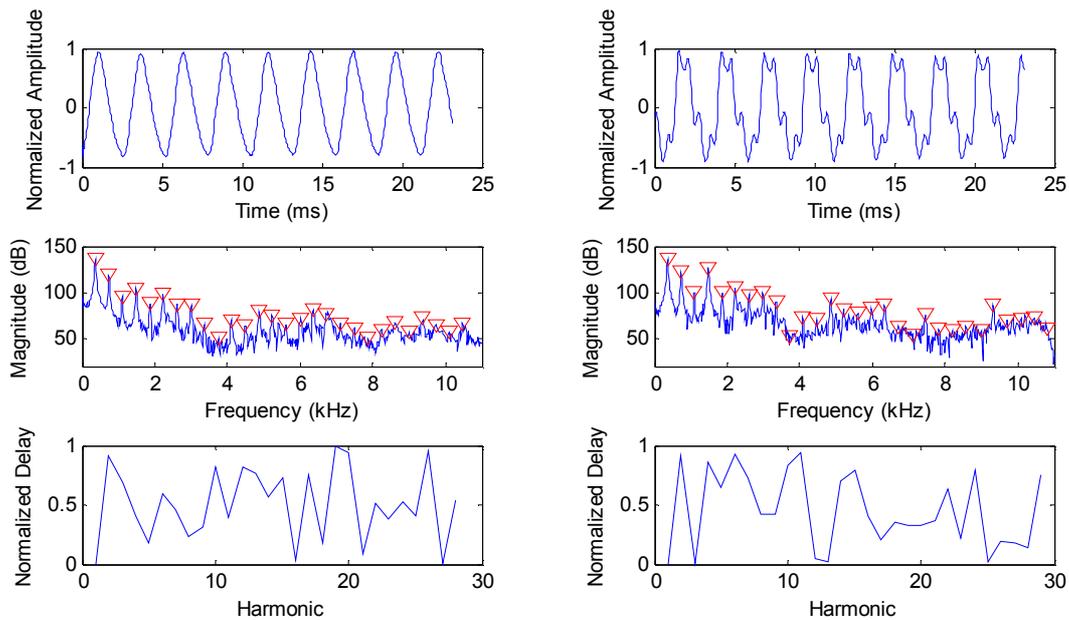
#### 5.4. GLOTTAL SOURCE ESTIMATION IN THE FREQUENCY DOMAIN

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In order to better analyse and synthesize the glottal source, for each one of the 24 acoustic signals captured near the vocal folds, we characterized in detail the magnitude and NRDs of the harmonics using the algorithm illustrated in Figure 5.5.

A first observation from the signals captured near the glottis was that the waveforms do not correspond to the idealistic glottal pulse models (as the ones illustrated in Figure 3.12). However, to our knowledge, there are no real experimental data of reference to sustain the wave shape of the idealist glottal pulse models and, therefore, the correspondence to real glottal source waveform is not clear.

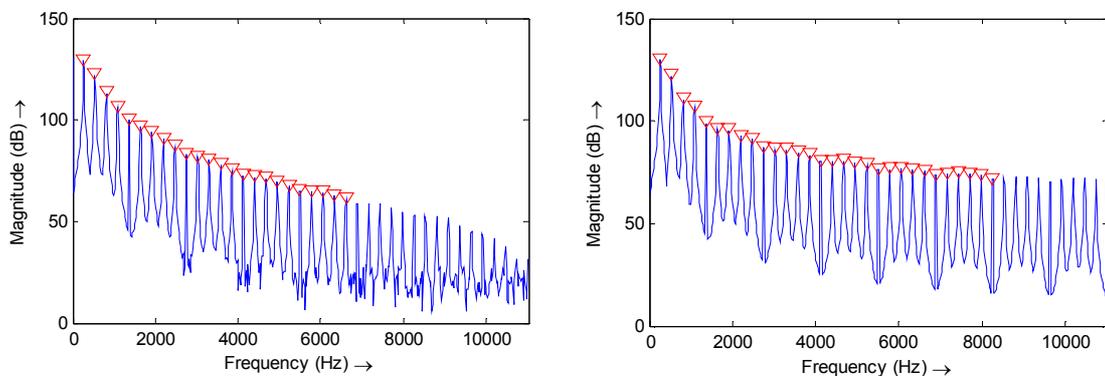
Concerning magnitude, we found the magnitude of individual harmonics for each frame of the source signal, as illustrated in Figure 5.9. The segmentation process was achieved by applying Sine Window, with  $N = 1024$  samples, and using 50% overlap between adjacent frames at the analysis, according to the framework illustrated in Figure 5.2. Then, for each vowel recorded and speaker, we determined the average normalized magnitude (relative to the magnitude of  $F_0$ ) of all detected harmonics. The following step was to obtain from this information the corresponding Least Squares Regression model in the logarithmic scale with the purpose to compare the resulting slope with the traditional -12 dB/octave reference. This slope reference is usually considered in the literature as the natural decay of the glottal pulse spectrum [Fan60]. In particular, according to [CRR<sup>+</sup>07], the LF model can be stylized in the spectral



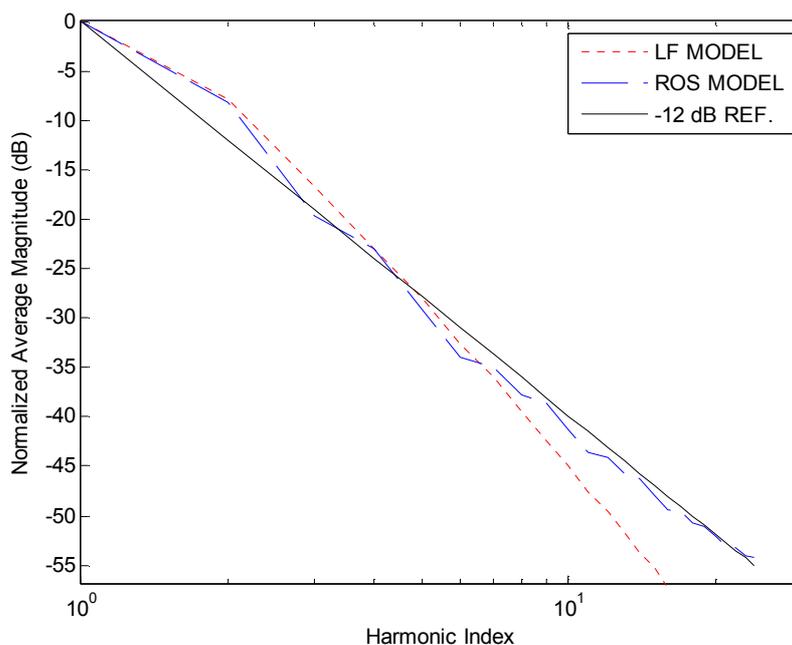
**Figure 5.9.** Waveform for vowel /i/ by a male subject (top row), the corresponding magnitude spectrum where harmonics are depicted (center) and the NRD representation (bottom row) of the signal captured near the glottis (left figure) and the signal captured outside the mouth (right figure).

domain by three asymptotic lines with  $+6$  dB/octave,  $-6$  dB/octave and  $-12$  dB/octave slopes. The crossing point of the first two asymptotes corresponds to a peak, called glottal spectral peak, centered at a frequency called the glottal formant.

However, in our research, using the first 24 and 30 harmonics, respectively, of each frame of the LF and Rosenberg glottal waveforms (Figure 5.10) and using the same segmentation process as referred above, we have found that this reference value ( $-12$  dB/octave) corresponds very approximately to the slope of the Rosenberg glottal pulse model, while for the LF glottal model the average slope is about  $-16$  dB/octave. The corresponding linear approximation models of the LF and Rosenberg glottal pulse models are shown in Figure 5.11.



**Figure 5.10.** Magnitude spectrum, where the first harmonics are depicted, of the waveform of the LF (left figure) and Rosenberg (right figure) glottal models.



**Figure 5.11.** Normalized magnitude of the first 24 harmonics of the LF glottal pulse model (red dashed line), and the 30 harmonics of the Rosenberg model (blue dashed line) and the reference line with -12 dB/octave slope (black solid line).

Table 5.2 presents the spectral decay results of the acoustic signals captured near the vocal folds according to gender and vowel. The results for each one of the 24 signals of our database are presented in Table B.1 of Appendix B and have been obtained using on average 16 harmonics for vowel /a/ and 11 harmonics for vowel /i/. This difference highlights the fact that vowel /i/ has an intrinsic pitch which is higher than that of vowel /a/.

Analysing these values it can be concluded that results per vowel are quite consistent between genders, and the standard deviation reveals there are no strong differences among subjects of the same gender. For both genders, the average slope for vowel /a/ is about -10 dB/octave and, for vowel /i/, is approximately -14 dB/octave. Thus, comparing to the -12 dB/octave reference, the average slope for vowel /a/ is lower, while the average slope for vowel /i/ falls between the slope of the Rosenberg glottal model (-11,84 dB/octave) and that of the LF glottal model (-16,43 dB/octave).

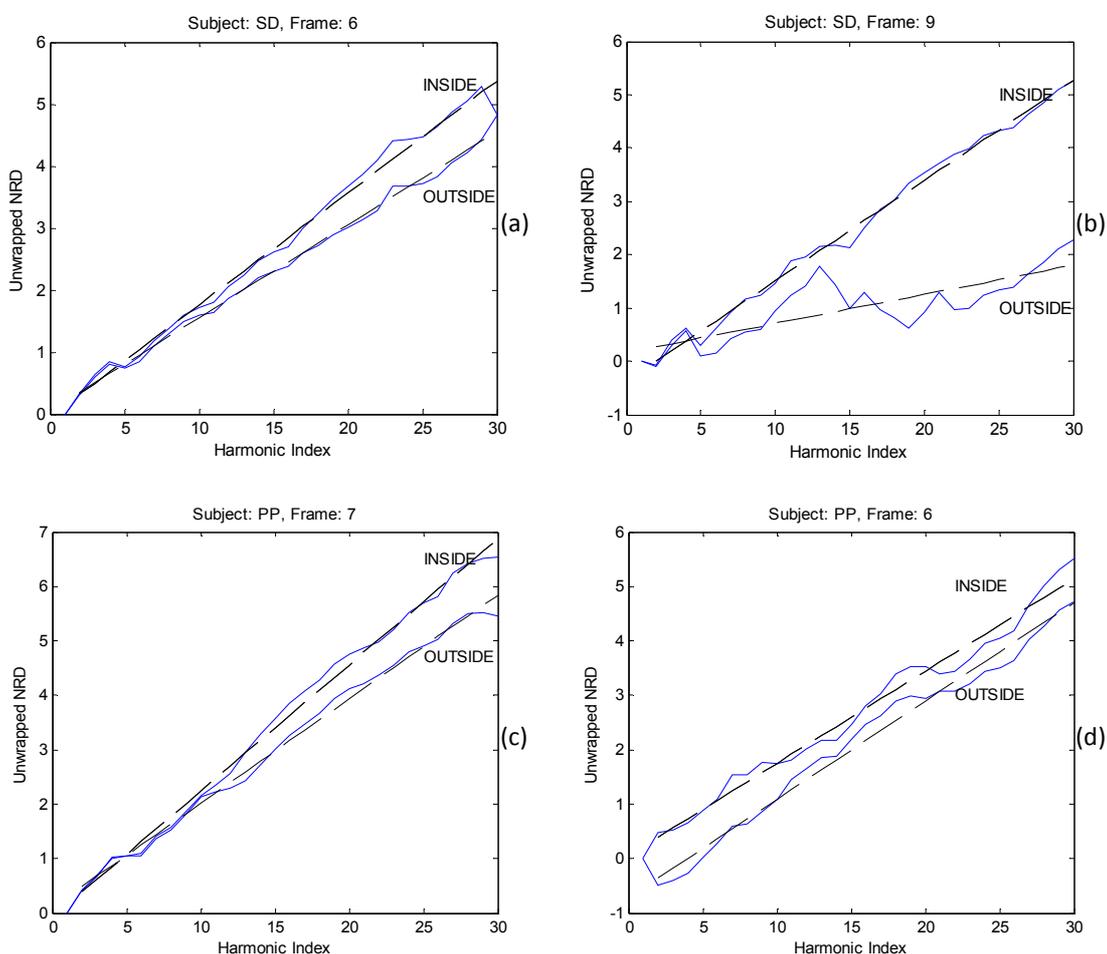
**Table 5.2.** Average (AVG) and Standard Deviation (STDev) of the spectral decay of the source harmonics, in dB/octave, as a function of gender and vowel.

	AVG /a/	STDev /a/	AVG /i/	STDev /i/
Males	-9,6443	2,3266	-13,7305	2,8674
Females	-9,9334	3,3521	-13,6694	2,2575

After the analysis concerning magnitude of the speech signals captured next to the vocal folds, the analysis concerning the NRDs for both time-aligned signals followed: the signals captured “inside”, i.e., near the vocal folds, and the signals captured outside the mouth.

The recorded signals have negative polarity which, according to the definition of the NRDs, has an impact in their behaviour [SF10].

For each signal in our database the unwrapped NRDs were determined, as illustrated in Figure 5.12. The NRD parameters are shown for different vowels and subjects, and for a particular data frame of both time-aligned speech signals. Analysing the results, it became clear that in most cases the unwrapped NRDs can be approximated by a line. Therefore, for each signal, in order to obtain the corresponding linear regression model, we selected a frame where the highest number of harmonics up to 30 could be identified.



**Figure 5.12.** Unwrapped NRDs (blue solid lines) of time-aligned signals frames captured “inside” and “outside” the mouth and the corresponding linear regression models (dashed lines) when:

- a female subject was uttering vowel /a/ (figure (a)) and vowel /i/ (figure (b));
- a male subject was uttering vowel /a/ (figure (c)) and vowel /i/ (figure (d)).

Table 5.3 and Table 5.4 present the average and the standard deviation of the slope of the linear regression model that fit the unwrapped NRDs of both genders and vowels recorded, /a/

**Table 5.3.** Average (AVG) and Standard Deviation (STDev) of the slope of the linear regression models corresponding to the unwrapped NRDs of the source signals, as a function of gender and vowel.

	AVG /a/	STDev /a/	AVG /i/	STDev /i/
Males	0,1440	0,1055	0,0563	0,0887
Females	0,1311	0,0554	0,0981	0,0712

**Table 5.4.** Average (AVG) and Standard Deviation (STDev) of the slope of the linear regression models corresponding to the unwrapped NRDs of the signals captured outside the mouth, as a function of gender and vowel.

	AVG /a/	STDev /a/	AVG /i/	STDev /i/
Males	0,1468	0,0998	0,0452	0,1023
Females	0,0889	0,0661	0,0657	0,0527

and /i/, for the signals capture near the vocal folds and outside the mouth, respectively. The results for each signal of our data are presented in Table B.2 of Appendix B and have been obtained using on average 29 harmonics for both time-aligned signals of vowel /a/ and 27 harmonics for vowel /i/.

It is clear from these results that the slope of the line corresponding to the linear approximation model of the unwrapped NRDs is strongly vowel dependent. For the source signals, we have observed slopes between almost 0/30 and 6/30, with most frequent cases falling around 4/30 and 6/30, for vowel /a/, and between 0/30 and 7/30, with most frequent cases among 4/30 and 6/30, for vowel /i/. This last range was the same observed for the signals captured outside the mouth for vowel /a/. For vowel /i/ those values were between almost 0/30 and 6/30. The average of the slope for both genders for vowel /a/ is approximately 0,14 and for vowel /i/ is about 0,08. Also, it was observed<sup>12</sup> that the slope of the linear regression model of the source signals is, in most cases, higher than that of the signals captured outside the mouth. The few exceptions are maybe explained by the idiosyncrasy of the subject.

Moreover, it was noticed that in most speech signals of our data set, the first 10 NRDs of time-aligned signals were very close and, therefore, differences in the corresponding linear models are more dependent on the values after that range. This is noticeable, for example, in the unwrapped NRD representation in Figures 5.12 (a) and 5.12 (b).

<sup>12</sup> For more details, see Table B.2 of Appendix B.

Analysing the difference, in modulus, between the slopes of the linear regression models corresponding to the unwrapped NRDs of the signals captured near the vocal folds and outside the mouth, it was observed that the values were between 0,02 and 0,06 for vowel /a/ and between 0,01 and 0,14 for vowel /i/.

According to the results presented in Table 5.5, the average of these differences, for vowel /a/, is about 0,04 for both genders and, for vowel /i/, is approximately 0,05 and 0,09 for male and female, respectively. Therefore, the average of this latter difference, for both genders, is about 0,04 for vowel /a/ and 0,07 for vowel /i/.

**Table 5.5.** Average (AVG) and Standard Deviation (STDev) of the difference, in modulus, between the slopes of the linear regression models that fit the unwrapped NRDs of the signals captured near the vocal folds and outside the mouth, as a function of gender and vowel.

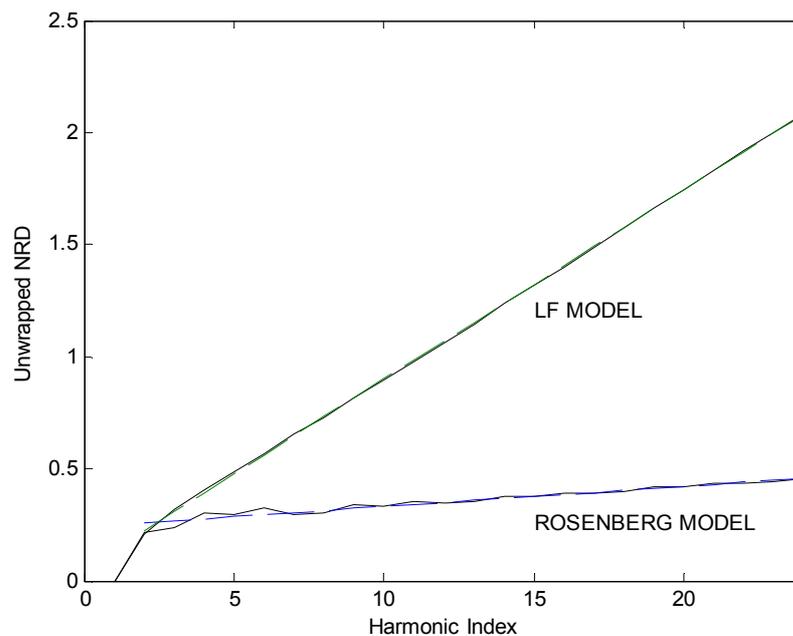
	AVG /a/	STDev /a/	AVG /i/	STDev /i/
Males	0,0436	0,0063	0,0527	0,0463
Females	0,0422	0,0148	0,0868	0,0326

#### 5.4.1. HYBRID LF-ROSENBERG GLOTTAL SOURCE MODEL

Our glottal source estimation requires a default glottal model and, in order to find the one that better matches our physiological data, we analysed two glottal source models of reference, LF and Rosenberg.

Using the same procedure explained previously, the unwrapped NRDs coefficients as well as the corresponding linear regression models were obtained for both glottal pulse models, as illustrated in Figure 5.13. It can be observed that the slope of the linear regression model of the LF glottal model is significantly higher than that of the Rosenberg model. In fact, the linear approximation for the LF model is given by  $y = 0,0849x + 0,0511$ , where  $x$  represents the index of the harmonic, for  $x \geq 2$ , since by definition the NRD of F0 is always zero, and for the Rosenberg model is given by  $y = 0,0090x + 0,2412$ .

However, according to the results presented in the previous section, neither of the two glottal source models of reference – LF and Rosenberg – fits our data, and thus a new problem aroused: which glottal pulse model should be used that better matches our physiological data? The spectral decay of the LF model (about -16 dB/octave) is significantly higher than the spectral decays obtained for vowels /a/ and /i/ in our data. On the other hand, the Rosenberg

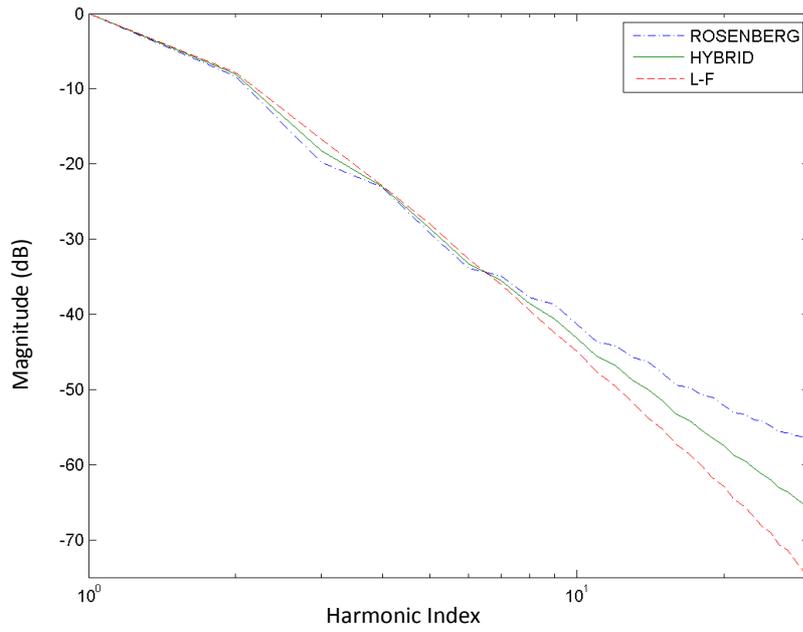


**Figure 5.13.** Unwrapped NRDs of the LF and Rosenberg glottal pulse models (solid lines) and the corresponding linear regression models (dashed lines).

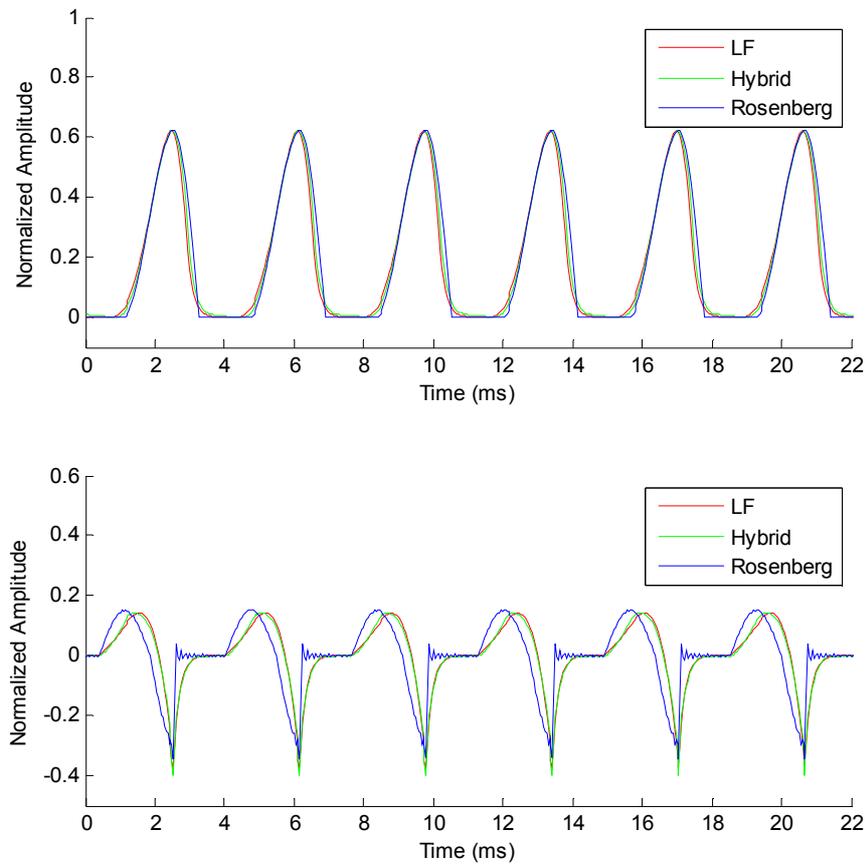
model has a discontinuity in its derivative and, thus, is not a realistic model. Therefore, using the normalized magnitude of the first 24 harmonics of each model, LF and Rosenberg, and the corresponding unwrapped NRDs coefficients, we decided to devise a hybrid model. This model was built using the average of the normalized spectral magnitudes of the harmonics of the LF and Rosenberg glottal models and we have used different combinations of linear regressions in order to build an NRD model. The smoothest result was obtained for the LF NRD model.

One advantage of this approach, as stated before, is that the normalized spectral magnitudes and NRDs of the harmonics allow to thoroughly define a time waveform shape independently of its fundamental frequency, time-shift or amplitude, which is essential for a glottal source model.

Figure 5.14 illustrates the normalized spectral magnitude of the first 24 harmonics of all three models: LF model, hybrid model and Rosenberg model. The time domain representation of these glottal pulse models and its corresponding derivatives are shown in Figure 5.15. The derivative signals were obtained in the frequency domain using the analysis-synthesis processing framework illustrated in Figure 5.2. In particular, since the derivation in the time domain corresponds to multiplying by  $j\Omega$  in the frequency domain, before the synthesis we shifted the phases of all harmonics by  $\pi/2$  and scaled their magnitude by  $|\Omega|$  at the exact frequency of each harmonic sinusoid.



**Figure 5.14.** Normalized magnitude of the first 24 harmonics pertaining to the LF glottal pulse model (red dashed line), the Rosenberg model (blue dash-dotted line) and a hybrid model (green solid line).



**Figure 5.15.** Time representation of the glottal pulse models (left figure) and the corresponding derivative: LF (top), hybrid (center), and Rosenberg (bottom).

It can be observed in Figure 5.15 that the hybrid model is smoother on the closing phase than LF and Rosenberg models, but quite approaches the LF model and does not have the discontinuity on the derivative signal, as the Rosenberg glottal model.

#### 5.4.2. GLOTTAL SOURCE ESTIMATION APPROACH

According to previous sections, at this point we have:

- a new prototype of glottal pulse, whose magnitude model is hybrid of the LF and Rosenberg glottal models, and whose NRD model matches that of the LF model;
- the spectrum of a sustained voiced signal captured outside the mouth, from which we determined the magnitude and NRD coefficients from the spectral peaks;
- an estimation of the difference between the slope of the linear regression model of the NRDs of the signals captured “inside” and “outside”, based on an experimental procedure with real subjects.

Therefore, since the spectral magnitude information is independent of the phase information, from which the NRDs are obtained, we developed the algorithm of estimation of the glottal pulse represented in Figures 5.16 and 5.17.

This process consists of the following steps:

1. A smooth magnitude interpolation of the spectral envelope ( $ceps$ ) is determined based on the spectral peaks of the harmonics of the voiced speech signal ( $mS$ ), using the Matlab function *interp1*. The smooth envelope is achieved by “short-pass liftering” the output signal of *interp1*.
2. The difference ( $dif$ ) between the magnitude of the spectral peaks and the magnitude of the model resulted from step 1 ( $ceps$ ) is estimated:

$$dif = mS - ceps . \quad (80)$$

3. Based on the assumption that the unique requirement associated to the magnitude frequency response of the (vocal tract) filter is smoothness, the spectral peaks of the glottal source ( $mG$ ) are estimated by adding the difference obtained in step 2 to the magnitude of the spectral peaks of the hybrid glottal model ( $mG_{HM}$ ):

$$mG = mG_{HM} + dif . \quad (81)$$

The magnitude of the filter ( $mF$ ) is, therefore, given as:

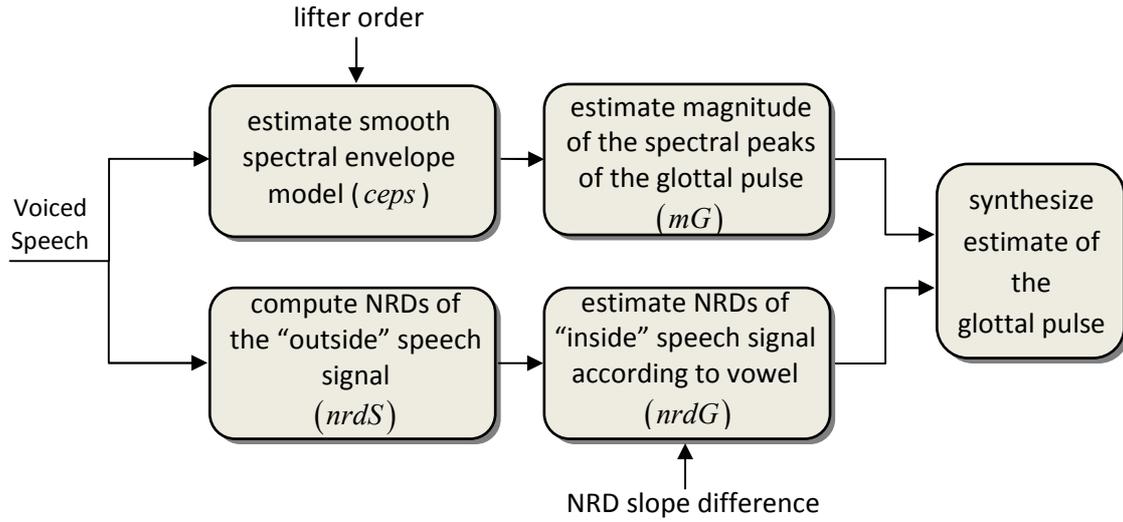


Figure 5.16. Glottal source estimation algorithm.

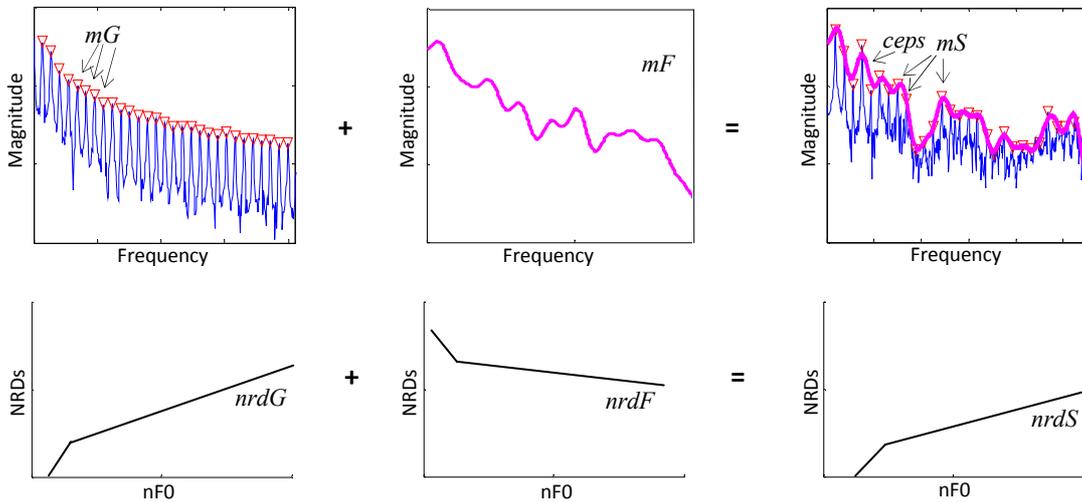


Figure 5.17. Illustration of the glottal source estimation.

$$\begin{aligned}
 mF &= mS - mG = mS - mG_{HM} - dif \\
 &= mS - mG_{HM} - mS + ceps \\
 &= ceps - mG_{HM}.
 \end{aligned} \tag{82}$$

4. The NRD coefficients of the voiced speech signal ( $nrdS$ ) are computed and then the NRDs of the source signal ( $nrdG$ ) are estimated as follows:

$$nrdG = nrdS + NRD_{slope\ dif} \times h\_index \tag{83}$$

where  $NRD_{slope\ dif}$  corresponds to the difference between the slope of the NRDs of the speech signal and that of the source signal (mentioned in section 5.4), and  $h\_index$  corresponds to the harmonic index.

5. Using the estimated NRDs (equation 83) and the magnitude of the spectral peaks (equation 81), the glottal pulse is synthesized.

In step 1, the magnitude spectral envelope is estimated using the cepstral approach instead of the popular LPC method because it better matches the poles and the zeros while the LPC method insures a good match only to the poles.

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## 5.5. TESTING THE NEW APPROACH TO GLOTTAL SOURCE ESTIMATION

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In this section the new approach to glottal source estimation described previously is tested with twelve speech signals including four synthetic and eight real (five from our data base), and also one male singing signal. The results are evaluated and compared with the ones obtained using two main state-of-the-art methods: IAIF and CC decomposition. These two techniques were chosen not only because they are very popular in glottal source estimation research, but also because they had better performances in the estimation of the glottal source presented in chapter 4.

It should be noted that the CC decomposition only delivers the estimation of the glottal source derivative (and the estimation of the vocal tract filter). Although we could implement the integration step in order to achieve the glottal source signal, it would be a modification of the result of the original procedure. Therefore, in this section the estimations of the glottal source derivative using the CC decomposition will be presented, will be compared to the ones obtained using IAIF (that are not necessarily results of reference) and will only be evaluated qualitatively.

In order to assess the quality of the estimations, the evaluation of the estimations using IAIF and our glottal source estimation approach will be complemented with an objective quantitative measure: the Signal to Noise Ratio (SNR), defined by equation 69. This measurement compares the signal and the noise resulting from the difference between the estimated and the reference signal, and efficient glottal flow estimations are then reflected in higher SNR values.

According to the definition of SNR, this value is only computed when the glottal source signal is known, as it happens in the case of synthetic signals. On the other hand and concerning real signals, we can not fully guarantee that the signals of our data base captured near the glottis correspond to the correct glottal source. In fact, we have remarked that if captured far from

the epiglottis, the influence of the vocal tract resonances becomes somehow noticeable. Thus, the signals were chosen with the criterion of being captured as close as possible to the glottis. We are however confident that the similarities of the waveforms for the majority of the captured signals, as well as the similarities to classic and ideal glottal source models, except on the closing and closed phases, enhance the validity of those signals as glottal source signals. Furthermore, the ideal or analytical glottal source models are not sustained with real data and, as previously mentioned, the existence of the closed phase seems to be an idealistic assumption since during the closed phase the majority of the individuals have some glottal leakage. Thus, according to these considerations, the SNR will be computed for nine signals (four synthetic and five from our data base).

### 5.5.1. TESTS WITH SYNTHETIC SPEECH SIGNALS

Four synthetic signals will be used in order to compare and evaluate the estimations of the glottal source: one of each gender, for vowels /a/ and /i/. These signals were generated using the Voicebox Matlab toolbox and having the LF model as glottal impulse. The fundamental frequency is 110 Hz and 300 Hz, for the male and the female synthetic signals, respectively. Figures 5.18<sup>13</sup> and 5.19 present the results for male signals and Figures 5.20 and 5.21 show the results for female signals, for vowels /a/ and /i/, respectively. In each figure (from left to right) we show first the LF flow waveform (top row) and the corresponding glottal flow derivative (bottom row). Then, we first present the estimations performed by the state-of-the-art methods – IAIF and CC decomposition – and, finally, the estimation using our glottal source estimation.

The SNR values for the glottal source estimations using IAIF and our approach are presented in Table 5.6.

Analysing all the estimations of the glottal pulse derivative using the CC decomposition, it is clear that they approach the LF glottal pulse derivative, except from the minimum, where the estimations are significantly smoother. This implies that the corresponding glottal pulses would not have an abrupt closure as the LF glottal pulse. Also, it is noticeable that this estimation method is less effective in the case of female signals, which corroborates that the CC decomposition efficiency reduces significantly in high frequency signals [Dru11].

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<sup>13</sup> This synthetic signal corresponds to the signal shown in Figure 4.19.

When comparing the estimations performed by CC decomposition to the glottal pulse derivative estimations using IAIF, the differences are obvious, namely on the nonexistence of ripples as in the results by IAIF, and the former method clearly outperforms in these signals.

**Table 5.6.** SNR values for the glottal source estimations of synthetic speech signals, using the IAIF method and our glottal source estimation approach.

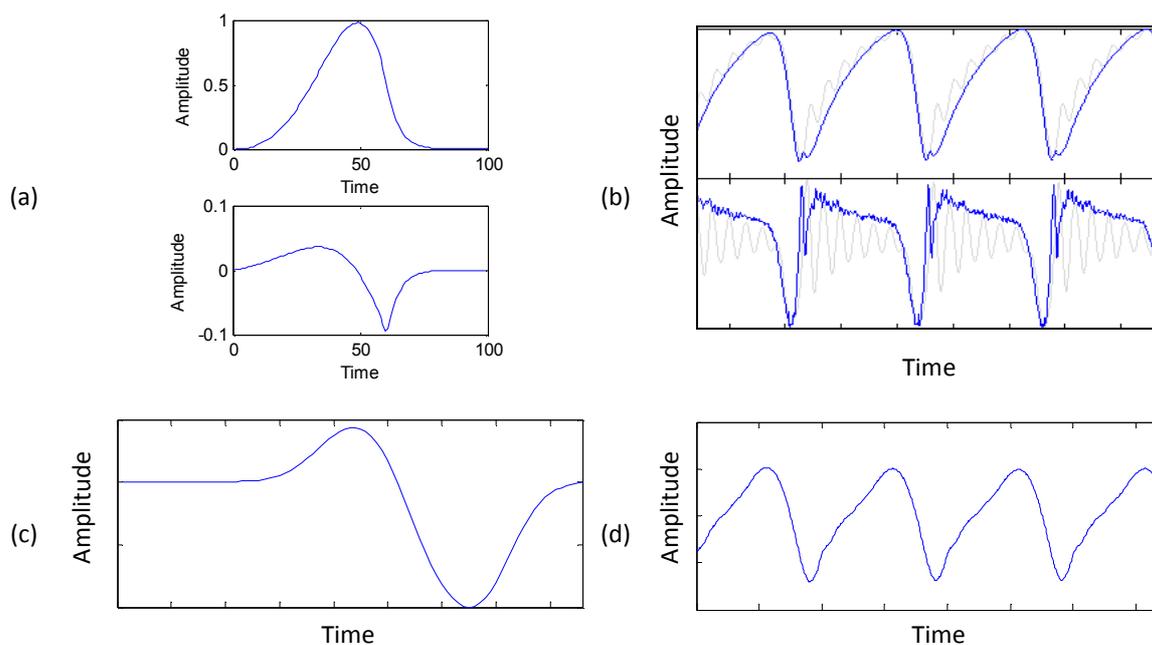
	Male synthetic vowel /a/	Male synthetic vowel /i/	Female synthetic vowel /a/	Female synthetic vowel /i/
IAIF	6,3832	6,0905	9,7968	8,7182
Our approach	7,3010	8,7168	9,7475	8,8672

The estimations of the glottal source using our proposed approach are close to the LF flow waveform but, like the estimations using IAIF, do not denote the closed phase of the glottal pulse.

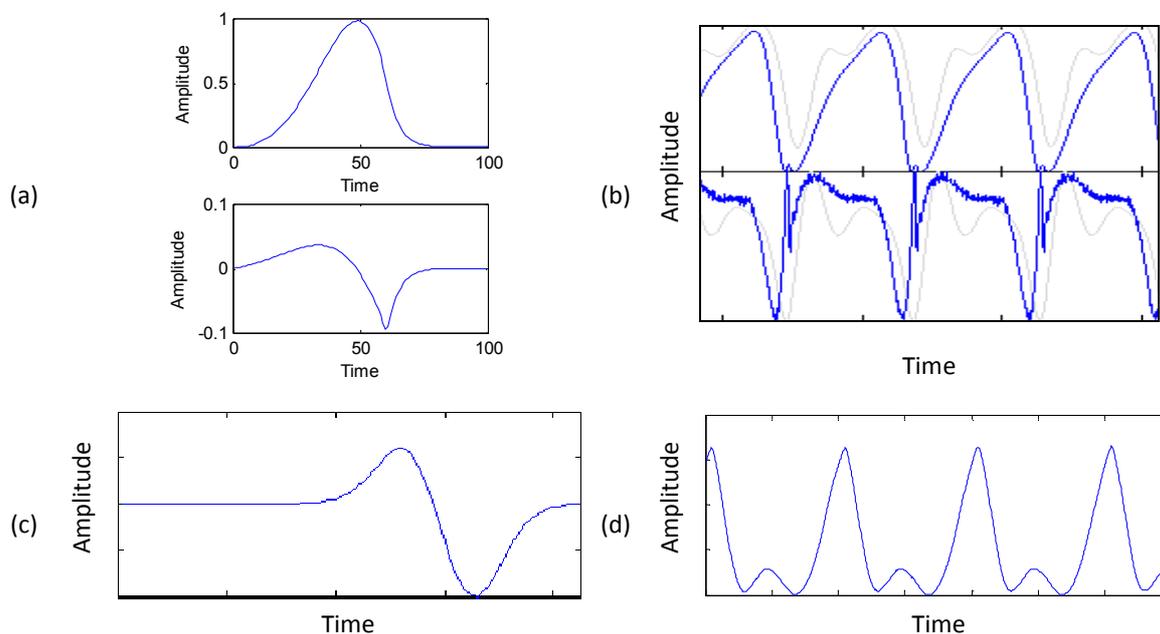
While the glottal flow estimations performed by IAIF are relatively similar between vowels and for the same gender, the results of our approach are significantly different for gender and vowel. Nevertheless, some features are common: the abrupt closure, as in the LF glottal pulse, and the asymmetric and bell-shape of the glottal pulses.

It can be also observed from Figures 5.20 and 5.21 that both estimation procedures outperform in the female synthetic signals, which is emphasized by the corresponding SNR values. These are interesting results since IAIF is usually less efficient on high frequency speech signals.

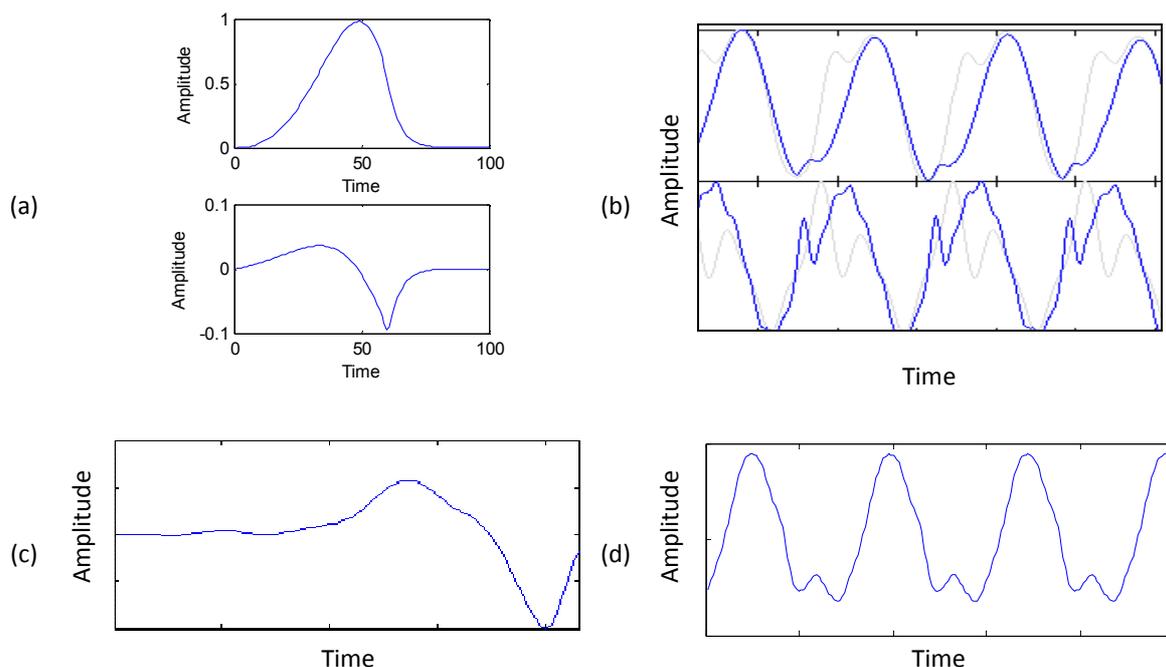
Also, according to the SNR values from Table 5.6, the performance of our approach is more effective in most test signals than the IAIF method, which highlights the robustness of our glottal source estimation process.



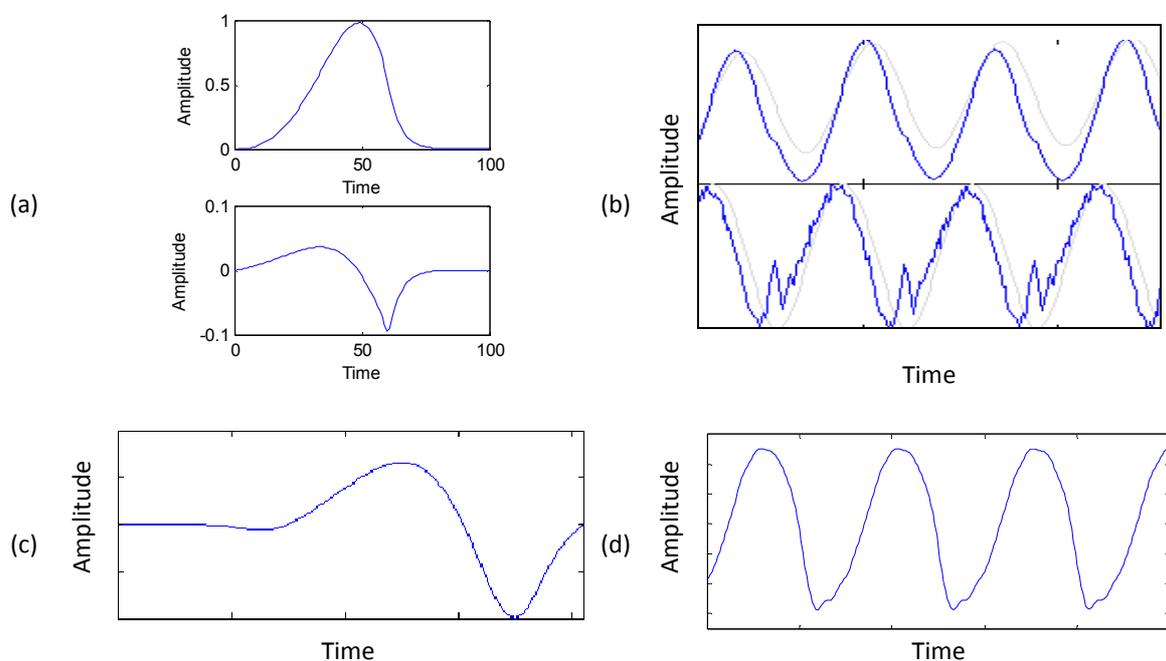
**Figure 5.18.** Glottal flow estimation of a male synthetic vowel /a/ using the LF model.  
 (a) Glottal flow waveform (top) and glottal flow derivative (bottom) ( $F_0 = 110$  Hz);  
 (b) The glottal flow (top row) and derivative (bottom row) waveforms estimated by IAIF;  
 (c) The glottal flow derivative estimation (maximum-phase component) using CC decomposition;  
 (d) The glottal flow waveform estimated by our glottal source estimation approach.



**Figure 5.19.** Glottal flow estimation of a male synthetic vowel /i/ using the LF model.  
 (a) Glottal flow waveform (top) and glottal flow derivative (bottom) ( $F_0 = 110$  Hz);  
 (b) The glottal flow (top row) and derivative (bottom row) waveforms estimated by IAIF;  
 (c) The glottal flow derivative estimation (maximum-phase component) using CC decomposition;  
 (d) The glottal flow waveform estimated by our glottal source estimation approach.



**Figure 5.20.** *Glottal flow estimation of a female synthetic vowel /a/ using the LF model.*  
 (a) *Glottal flow waveform (top) and glottal flow derivative (bottom) ( $F_0 = 300$  Hz);*  
 (b) *The glottal flow (top row) and derivative (bottom row) waveforms estimated by IAIF;*  
 (c) *The glottal flow derivative estimation (maximum-phase component) using CC decomposition;*  
 (d) *The glottal flow waveform estimated by our glottal source estimation approach.*



**Figure 5.21.** *Glottal flow estimation of a female synthetic vowel /i/ using the LF model.*  
 (a) *Glottal flow waveform (top) and glottal flow derivative (bottom) ( $F_0 = 300$  Hz);*  
 (b) *The glottal flow (top row) and derivative (bottom row) waveforms estimated by IAIF;*  
 (c) *The glottal flow derivative estimation (maximum-phase component) using CC decomposition;*  
 (d) *The glottal flow waveform estimated by our glottal source estimation approach.*

### 5.5.2. TESTS WITH REAL SPEECH SIGNALS

In this section eight real speech signals and one male singing signal are used, with normal phonation, in order to evaluate the quality of the glottal source estimations. Three of these speech signals, illustrated in Figures 5.22 to 5.24, were also used in chapter 4<sup>14</sup>, and the remaining five signals are from our data base:

- a female vowel /a/ (subject SF) with  $F_0=372$  Hz (Figure 5.26);
- a female vowel /i/ (subject SD) with  $F_0=489$  Hz (Figure 5.27);
- a female vowel /i/ (subject SF) with  $F_0=464$  Hz (Figure 5.28);
- a male vowel /a/ (subject RT) with  $F_0=261$  Hz (Figure 5.29);
- a male vowel /i/ (subject RT) with  $F_0=266$  Hz (Figure 5.30).

An advantage of these latter signals is that, as explained above, a representation of the source signal is known and, therefore, it is easy to evaluate the estimations provided by the different techniques.

Following the same procedure of the previous section, in each figure (from left to right) we first present the speech waveform, for the first three speech signals and for the singing signal, or the signal captured near the glottis, for the five speech signals of our data set. The estimates follow and are shown in the same order: IAIF, CC decomposition and our glottal source estimation approach.

Due to the unavailability of the glottal source signals for the first three speech signals and for the singing signal, it is more difficult to assess the quality of the estimations. Still, we will compare the estimations performed by the different techniques between each other.

Analysing Figures 5.22 to 5.25, strong similarities between the glottal source estimations using IAIF and our approach can be noted. While for the first two speech signals, the estimations performed by these two methods show the classic asymmetry and bell-shape of the glottal pulse, often referred to in the literature, the estimations for the third signal show a modification on the closing phase. This modification is also present either in all signals of our data captured near the glottis analysed here (as in most of our data base) and in all corresponding estimations performed using our approach.

Concerning the estimations performed by CC decomposition for the same signals, they quite approximate classic glottal pulse derivative models, except on the closing phase, however they are significantly different from the estimations using IAIF, namely in the closed phase.

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<sup>14</sup> The signals are shown in Figures 4.20 to 4.22.

It is interesting to notice, in particular, that the estimations performed by the three techniques of the singing signal have similarities.

The analysis of the estimations performed by IAIF and our approach, related to the signals from our data base, will be also assessed with the SNR values exhibited in Table 5.7.

According to Figures 5.26 to 5.30, it is clear that the glottal flow estimations resulted from our approach are significantly identical to the waveforms of the corresponding signals captured near the glottis and the SNR values enhance the quality of those estimations. For most of these signals, the estimations performed by IAIF and our approach are close, with outperformance of our approach, which is corroborated by the higher SNR values from Table 5.7.

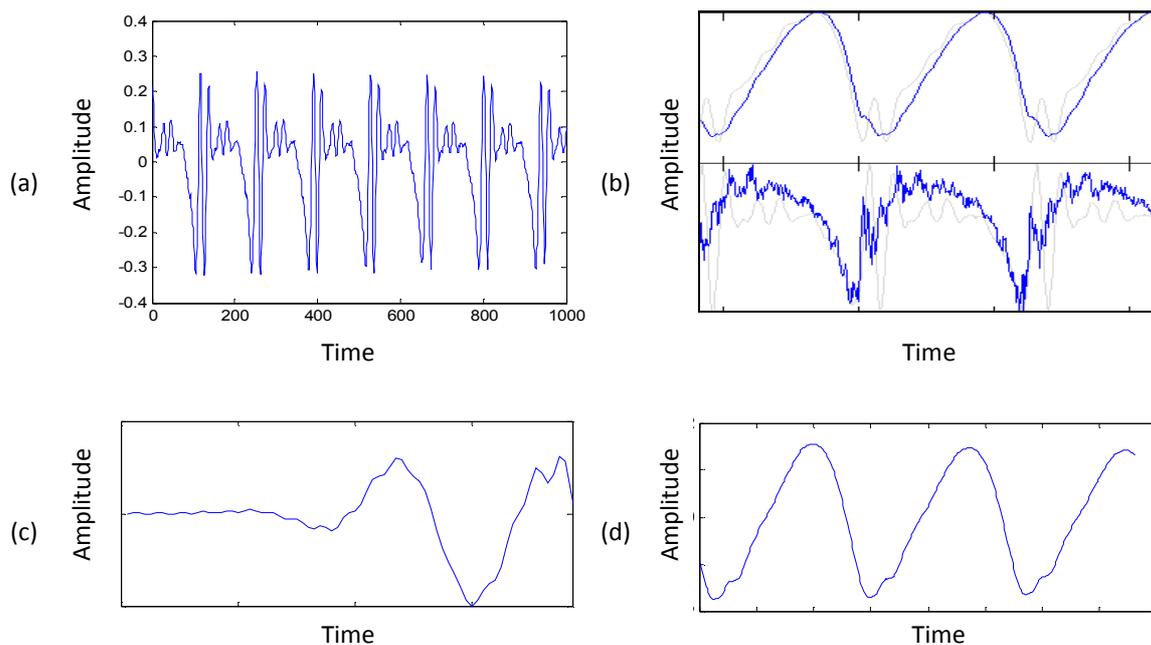
**Table 5.7.** SNR values for the glottal source estimations using the IAIF method and our glottal source estimation approach.

	<b>Female vowel /a/ (subject SF)</b>	<b>Female vowel /i/ (subject SD)</b>	<b>Female vowel /i/ (subject SF)</b>	<b>Male vowel /a/ (subject RT)</b>	<b>Male vowel /i/ (subject RT)</b>
IAIF	8,9982	9,5403	10,3138	9,6980	11,3175
Our approach	11,8187	15,8266	11,2107	14,6801	13,3643

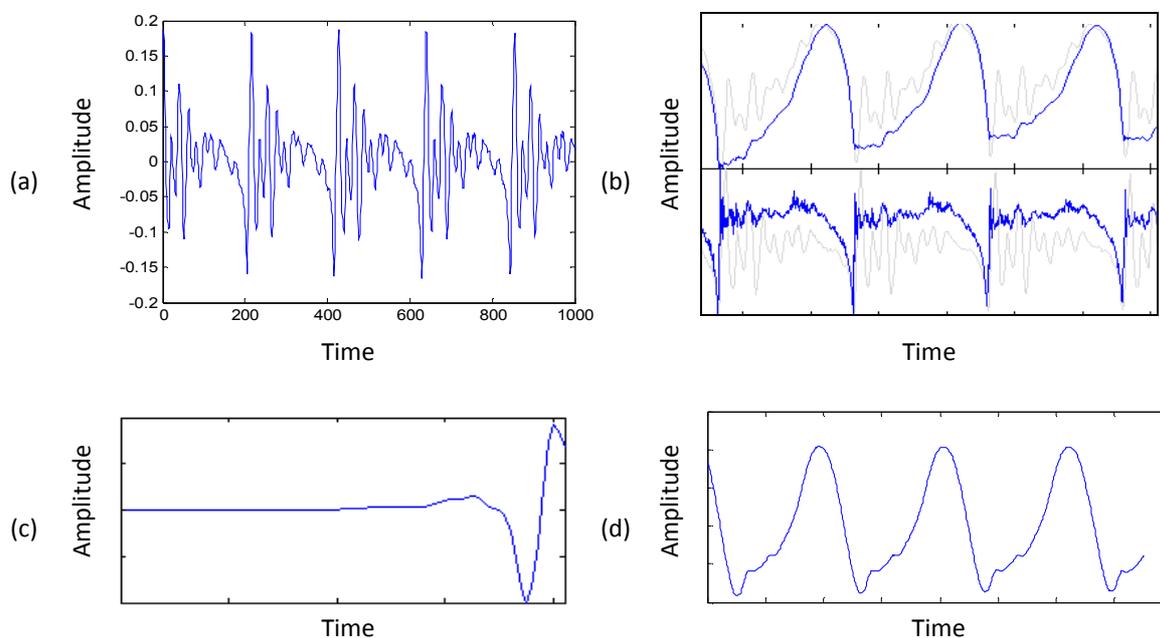
It can also be noticed that the estimations by CC decomposition are quite consistent and, despite the differences when compared to the glottal flow derivative waveforms estimated using IAIF, the positive and negative parts are identical.

An important and common feature of most of these glottal flow estimations is the shape of the waveform on the closing phase. This is noticeable in Figures 5.24, 5.26, 5.27, 5.28, 5.29 and 5.30, and, as mentioned above, it was clear in most of the signals of our data base captured “inside”, i.e., near the vocal folds. This maybe highlights the fact that mathematical glottal pulse models do not entirely correspond to realistic glottal pulses, namely on the closing and closed phases.

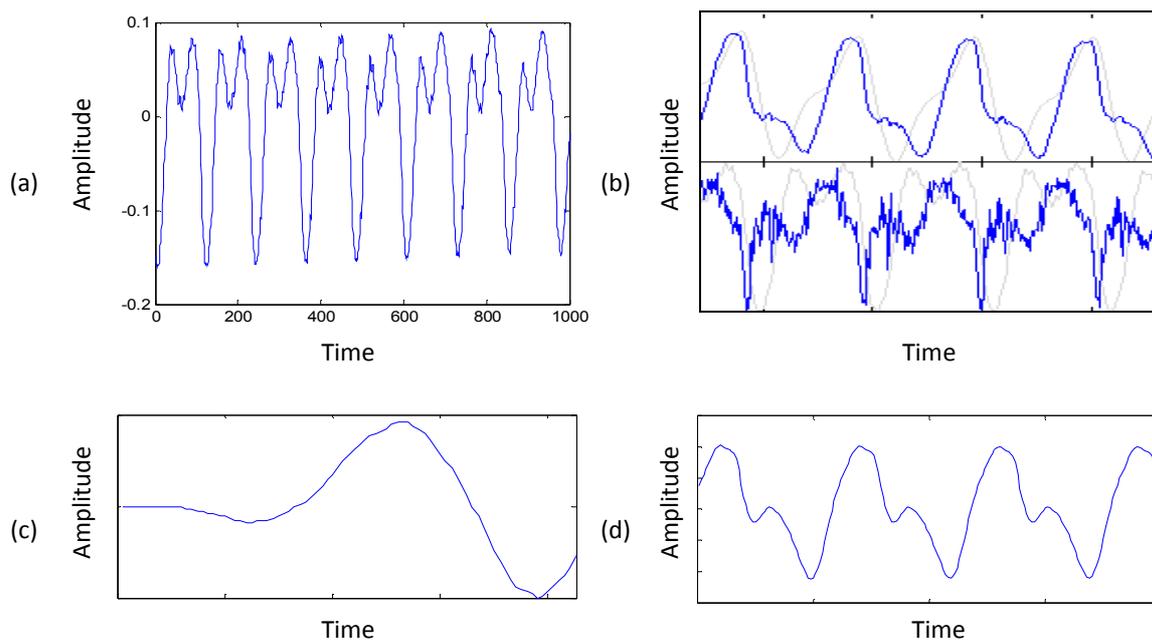
The similarities between the glottal source estimations performed by our approach and the corresponding glottal flow waveforms of the signals, as well as the higher SNR values comparatively to the ones related to the IAIF performances, emphasize that our proposed approach performs robust glottal source estimations and, therefore, confirm this new glottal source estimation method as a promising technique.



**Figure 5.22.** *Glottal flow estimation of a female vowel /a/.*  
 (a) *Speech signal;*  
 (b) *The glottal flow (top row) and derivative (bottom row) waveforms estimated by IAIF;*  
 (c) *The glottal flow derivative estimation (maximum-phase component) using CC decomposition;*  
 (d) *The glottal flow waveform estimated by our glottal source estimation approach.*

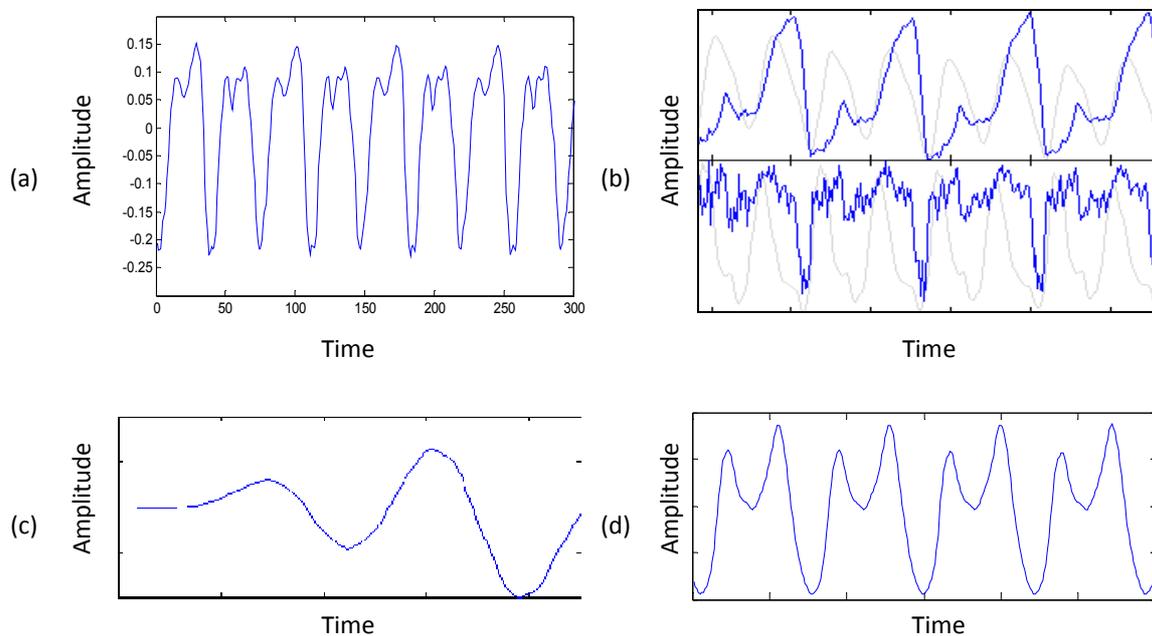


**Figure 5.23.** *Glottal flow estimation of a male vowel /a/.*  
 (a) *Speech signal;*  
 (b) *The glottal flow (top row) and derivative (bottom row) waveforms estimated by IAIF;*  
 (c) *The glottal flow derivative estimation (maximum-phase component) using CC decomposition;*  
 (d) *The glottal flow waveform estimated by our glottal source estimation approach.*



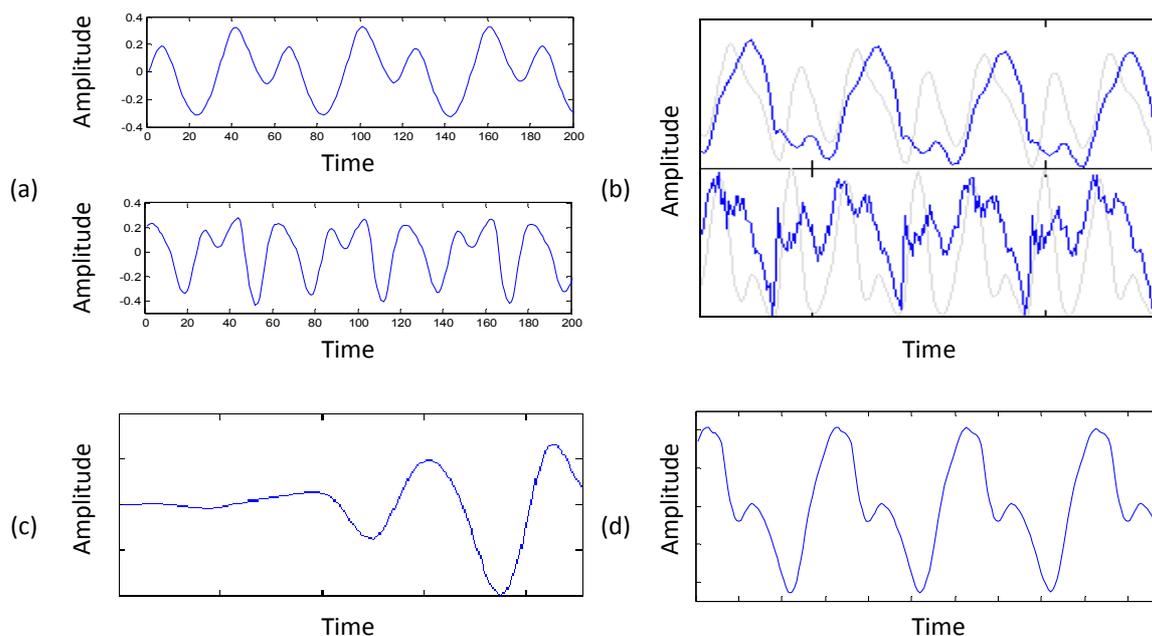
**Figure 5.24.** Glottal flow estimation of a female vowel /i/.

- (a) Speech signal;
- (b) The glottal flow (top row) and derivative (bottom row) waveforms estimated by IAIF;
- (c) The glottal flow derivative estimation (maximum-phase component) using CC decomposition;
- (d) The glottal flow waveform estimated by our glottal source estimation approach.

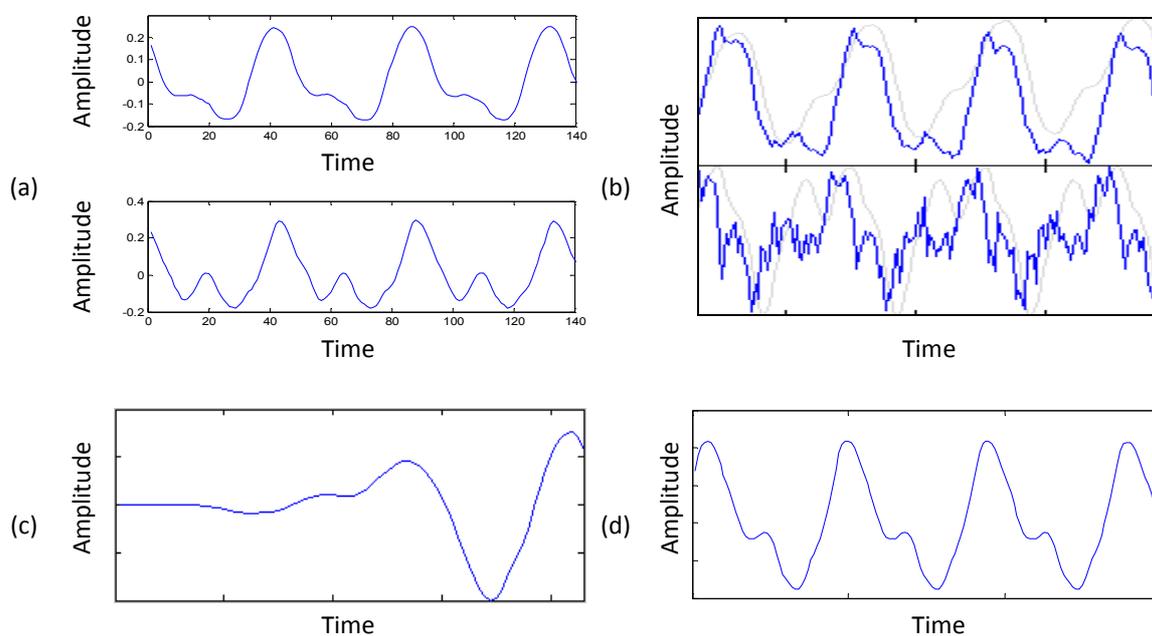


**Figure 5.25.** Glottal flow estimation of a singing signal of a male voice.

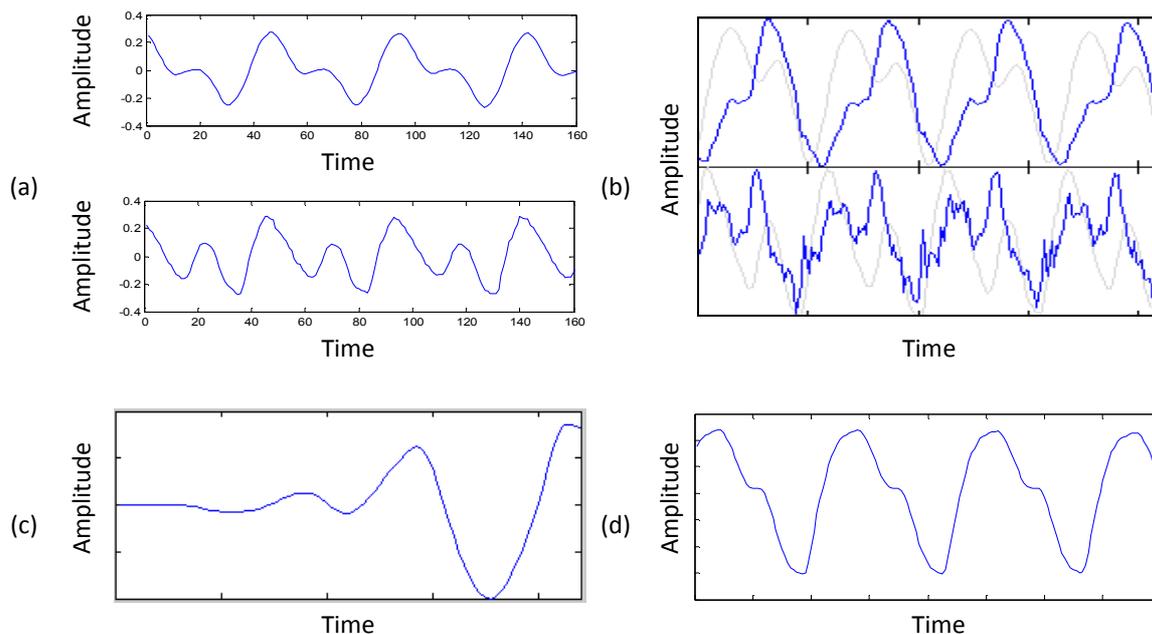
- (a) Speech signal;
- (b) The glottal flow (top row) and derivative (bottom row) waveforms estimated by IAIF;
- (c) The glottal flow derivative estimation (maximum-phase component) using CC decomposition;
- (d) The glottal flow waveform estimated by our glottal source estimation approach.



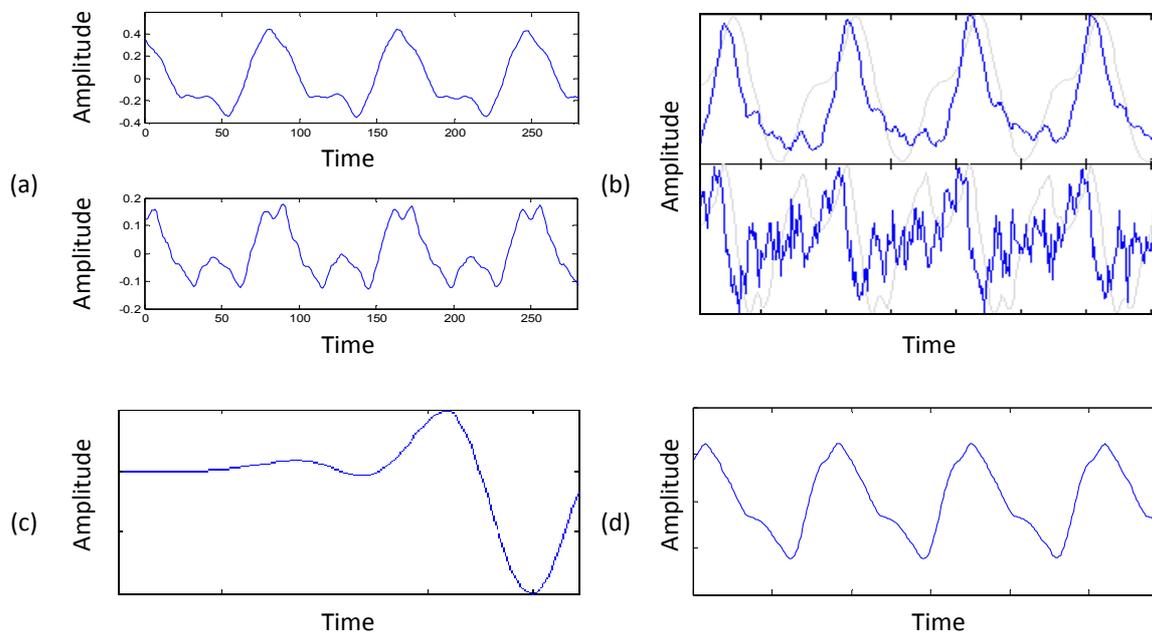
**Figure 5.26.** *Glottal flow estimation of a female vowel /a/ from our data base (subject SF).*  
 (a) *Signal captured near the glottis (top row) and signal captured outside (bottom row);*  
 (b) *The glottal flow (top row) and derivative (bottom row) waveforms estimated by IAIF;*  
 (c) *The glottal flow derivative estimation (maximum-phase component) using CC decomposition;*  
 (d) *The glottal flow waveform estimated by our glottal source estimation approach.*



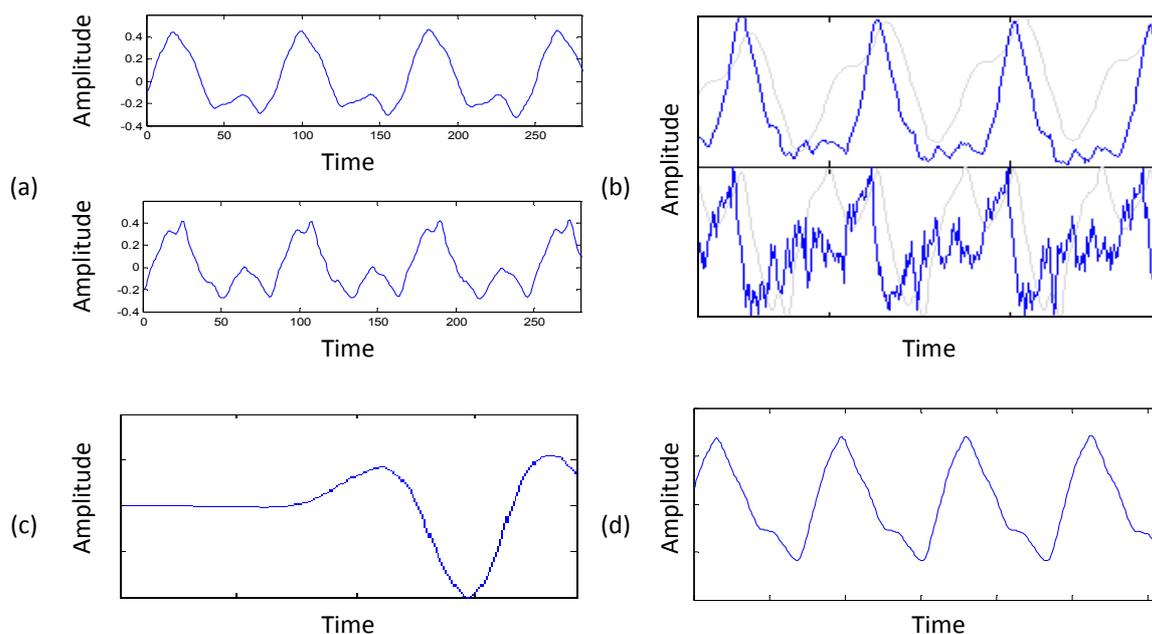
**Figure 5.27.** *Glottal flow estimation of a female vowel /i/ from our data base (subject SD).*  
 (a) *Signal captured near the glottis (top row) and signal captured outside (bottom row);*  
 (b) *The glottal flow (top row) and derivative (bottom row) waveforms estimated by IAIF;*  
 (c) *The glottal flow derivative estimation (maximum-phase component) using CC decomposition;*  
 (d) *The glottal flow waveform estimated by our glottal source estimation approach.*



**Figure 5.28.** *Glottal flow estimation of a female vowel /i/ from our data base (subject SF).*  
 (a) *Signal captured near the glottis (top row) and signal captured outside (bottom row);*  
 (b) *The glottal flow (top row) and derivative (bottom row) waveforms estimated by IAIF;*  
 (c) *The glottal flow derivative estimation (maximum-phase component) using CC decomposition;*  
 (d) *The glottal flow waveform estimated by our glottal source estimation approach.*



**Figure 5.29.** *Glottal flow estimation of a male vowel /a/ from our data base (subject RT).*  
 (a) *Signal captured near the glottis (top row) and signal captured outside (bottom row);*  
 (b) *The glottal flow (top row) and derivative (bottom row) waveforms estimated by IAIF;*  
 (c) *The glottal flow derivative estimation (maximum-phase component) using CC decomposition;*  
 (d) *The glottal flow waveform estimated by our glottal source estimation approach.*



**Figure 5.30.** *Glottal flow estimation of a male vowel /i/ from our data base (subject RT)*  
 (a) *Signal captured near the glottis (top row) and signal captured outside (bottom row);*  
 (b) *The glottal flow (top row) and derivative (bottom row) waveforms estimated by IAIF;*  
 (c) *The glottal flow derivative estimation (maximum-phase component) using CC decomposition;*  
 (d) *The glottal flow waveform estimated by our glottal source estimation approach.*

### 5.5.3. CONCLUSIONS

In the previous sections, our glottal source estimation approach was tested in several speech signals, synthetic and real, with the purpose to evaluate its performance and to compare the effectiveness of this procedure with two state-of-the-art glottal flow estimation techniques: IAIF and CC decomposition.

It was clear that most of the glottal flow estimations performed by IAIF and our approach were similar and revealed some particularities and common shapes, namely on the closing and closed phases. These characteristics were also noticeable in most of the signals captured near the glottis from our data set and maybe indicate that the real glottal pulse has not a bell-shape as in the reference classic glottal flow models.

The results performed by CC decomposition do not allow substantial conclusions since this method only gives the glottal source derivative estimation and, therefore, the estimations for the real signals were only compared to the ones using IAIF. However, in the synthetic speech tests, the effectiveness of the CC decomposition was rather higher than IAIF, although the estimations were significantly smoother on the closing phase when compared to the reference

LF glottal source derivative. In real speech tests, the results of this method were consistent and revealed some particularities similar to the IAIF results.

Despite the fact that the glottal flow estimations by IAIF and our approach for the synthetic speech signals have in general, an asymmetric and bell-shape, we observed that in the case of real signals the results shown a common characteristic: a variation on the closing phase, also noticeable in the majority of the signals of our data base captured near the glottis.

We also observed that the estimations of the glottal source using our approach were, in the majority of the tests, similar to the ones delivered by IAIF, however our approach outperformed this method which is corroborated by the higher SNR values.

Therefore, our glottal source estimation approach exhibits promising results, which motivates the improvement in future developments of our initial approach illustrated in Figure 5.1.

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## 5.6. SUMMARY

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In this chapter a new glottal pulse estimation procedure, implemented in the frequency-domain, was proposed based on an accurate spectral magnitude modelling and estimation of the Normalized Relative Delays (NRDs) of the harmonics of the voiced signal.

This approach was developed using the results from accurate sinusoidal/harmonic analysis and synthesis of two time aligned acoustic signals for vowels /a/ and /i/: the glottal source signal captured near the glottis and the corresponding voiced signal captured outside the mouth. The experimental procedure in which these signals were captured was thoroughly described.

The results of the data set analysis were presented, namely concerning the magnitude of the spectral peaks and the NRDs of the harmonics, and a new hybrid glottal pulse prototype was devised, combining features of two reference glottal models - the Liljencrants-Fant and the Rosenberg models.

The performance of the new glottal source approach was assessed on several voiced signals, synthetic and real, and the results look competitive taking into consideration results by other reference algorithms, namely IAIF. Moreover, in almost all the tests where the glottal source was known, our estimation approach led to the best results, as evidenced by higher SNR values.

It was noticeable in most glottal source estimations and in the majority of the signals from our data base captured near the glottis, a common shape that exhibits a variation on the closing

phase. This maybe highlights that the real glottal pulse has not a bell-shape, often assumed in the literature and as usually considered in classic glottal pulse models.

Despite the fact that our glottal source estimation approach does not implement the first order integration step, common in most inverse filtering techniques in order to eliminate the lip/nostrils radiation effect from the voiced signal and usually implemented in time domain, we reviewed also in this chapter that this procedure can be accurately implemented in the frequency domain avoiding some of the pitfalls of the integration in time domain.

# Chapter 6

## CONCLUSION

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## 6.1. OVERVIEW

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Over the years, the voice has been an important object of study in different areas but it still remains an open field for investigation. In particular, the estimation of the glottal pulse from a speech signal raised the interest of many researchers due to its great potential in speech science. However, due to the concealed location of the vocal folds and, therefore, to the difficulties on capturing directly and non-invasively the glottal source signal, computational alternatives have been proposed over the years in order to accurately estimate the glottal source directly from speech signals. Most of the glottal source estimation procedures are based on the source-filter model and, thus, the glottal source is estimated by reversing the voice production, i.e., the glottal source and the vocal tract filter are separated in order to obtain the voice source generated at the glottis.

In this dissertation a new frequency-domain approach to glottal source estimation was proposed, using a phase-related feature based on the Normalized Relative Delays (NRDs) of the harmonics and an accurate determination of the magnitude of the spectral peaks of the harmonics of the speech signal. From these values, the magnitude of the spectral peaks and the NRDs corresponding to the glottal source are estimated and the glottal pulse is synthesized, using a new hybrid model combining features of two reference glottal models - the Liljencrants-Fant and Rosenberg - and that represents a better fit to our experimental data, whose special acquisition was also described.

The performance of our approach has been evaluated and compared on a significant number of speech signals, synthetic and real, using two representative state-of-the-art techniques for the same purpose - IAIF and CC decomposition. For the synthetic signals and signals of our data base, an objective measure (SNR) was used in order to assess the quality of the glottal source estimations.

The results have shown that for synthetic signals, the estimations of our approach were similar to the ones obtained by IAIF and the SNR values revealed that, in the majority of these signals, our approach was more effective.

For real signals, our approach to glottal source estimation also exhibited better performance when compared to other techniques. On the other hand, results also suggested that the glottal pulse estimations do not have the bell-shape, usually assumed in the literature and common in mathematical glottal pulse models, but revealed a variation on the closing phase. Also, the closed phase was not perceptible in any glottal flow estimations. These results maybe suggest

that idealistic glottal pulse models do not entirely correspond to real glottal pulse, namely on the closing and closed phases.

Finally, it is important to emphasize the importance of phase features in speech analysis and synthesis, namely the NRDs, and the promising results presented in this work corroborate that our glottal source approach has a great potential in glottal source estimation. Therefore, this dissertation work added an important contribution in this research direction.

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## 6.2. FUTURE DIRECTIONS

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In the following list, possible future direction of research are proposed.

- Capture time-aligned speech signals (the signal “inside” as close as possible to the glottis and the signal outside the mouth), as implemented in this study, for a larger number of subjects, with and without speech disorders, and not only for sustained vowels. This would allow to better characterize the relation between the NRDs of the harmonics of the voiced signal and the respective glottal source signal. Also, it would be interesting to use a third signal, as the EGG, to improve the estimation.
- Implement an iterative procedure in the proposed algorithm for the estimation of the glottal source in order to obtain even more accurate estimations.
- Explore the potential of the NRDS in the development of a robust algorithm for speaker identification.
- Explore the potentialities of our approach in the independent manipulation of the spectral magnitude and of the NRDs, characterizing the phase, in order to improve the naturalness of synthetic speech and implant the sound signature of a specific speaker.

## APPENDIX A – FUNDAMENTALS OF DIGITAL SIGNAL PROCESSING

- **WINDOW FUNCTIONS**

### Blackman

$$w_B(n) = 0.42 + 0.5 \cos\left(\frac{2\pi n}{N-1}\right) + 0.08 \cos\left(\frac{4\pi n}{N-1}\right), \quad 0 \leq n \leq N-1$$

### Hamming

$$w_{HM}(n) = 0.54 - 0.46 \cos\left(\frac{2\pi n}{N-1}\right), \quad 0 \leq n \leq N-1$$

### Hanning

$$w_{HN}(n) = 0.5 - 0.5 \cos\left(\frac{2\pi n}{N-1}\right), \quad 0 \leq n \leq N-1$$

### Hanning-Poisson

$$w_{HP}(n) = 0.5 \left[ 1 + \cos\left(\frac{2\pi n}{N}\right) \right] e^{-\alpha \frac{2|n|}{N}}, \quad |n| \leq \frac{N}{2}$$

### Sin

$$w_S(n) = \sin\left(\frac{\pi}{N} \times \left(n + \frac{1}{2}\right)\right), \quad 0 \leq n \leq N-1$$

### Triangular

$$w_T(n) = \frac{2}{N-1} \left( \frac{N-1}{2} - \left| n - \frac{N-1}{2} \right| \right), \quad |n| \leq \frac{N-1}{2}$$

- **DISCRETE TIME FOURIER TRANSFORM (DTFT)**

The Fourier transform represents a signal in terms of complex exponentials (or sinusoids), because  $e^{-j\omega n} = \cos(\omega n) - j \sin(\omega n)$ .

The discrete time Fourier transform (DTFT) of a discrete signal  $x[n]$  is defined as:

$$X(e^{j\omega}) = \sum_{n=-\infty}^{+\infty} x[n] e^{-j\omega n}.$$

The inverse of the discrete time Fourier transform (IDTFT) is given by:

$$x[n] = \frac{1}{2\pi} \int_{-\pi}^{\pi} X(e^{j\omega}) e^{j\omega n} d\omega.$$

- **DISCRETE FOURIER TRANSFORM (DFT)**

The discrete Fourier transform (DFT) of a periodic signal  $x[n]$ , with period  $N$ , is defined as:

$$X[k] = \sum_{n=0}^{N-1} x[n] e^{-jkn\frac{2\pi}{N}}$$

and the corresponding inverse (IDFT) is given by:

$$x[n] = \frac{1}{N} \sum_{k=0}^{N-1} X[k] e^{jkn\frac{2\pi}{N}}.$$

- **FAST FOURIER TRANSFORM (FFT)**

The fast Fourier transform (FFT) of a signal produces exactly the same result as evaluating the DFT definition directly but is much faster.

There are several algorithms of FFT, as the function *fft.m* in Matlab.

- **DISCRETE COSINE TRANSFORM (DCT)**

The discrete cosine transform (DCT) of a signal  $x[n]$ , with length  $N$ , is defined as:

$$X[n] = c(n) \sum_{m=0}^{N-1} x[m] \cos \left[ \frac{(2m+1)n\pi}{2N} \right]$$

where

$$c(n) = \begin{cases} \sqrt{1/N}, & n = 0 \\ \sqrt{2/N}, & n \neq 0 \end{cases}.$$

The inverse of a discrete cosine transform (IDCT) is:

$$x[n] = \sum_{m=0}^{N-1} c(m) X[m] \cos \left[ \frac{(2m+1)n\pi}{2N} \right]$$

- **ODD-FREQUENCY DISCRETE FOURIER TRANSFORM (ODD-DFT)**

The odd-frequency discrete Fourier transform (ODFT) of a signal  $x[n]$ , with length  $N$ , is defined as:

$$X[k] = \sum_{n=0}^{N-1} x[n] e^{-j \left( k + \frac{1}{2} \right) n \frac{2\pi}{N}}$$

- **Z-TRANSFORM**

The z-transform is a generalization of the Fourier transform.

The z-transform of a discrete signal  $x[n]$  is defined as

$$X(z) = \sum_{n=-\infty}^{+\infty} x[n] z^{-n}$$

and a sufficient condition for convergence of the infinite series is:

$$\sum_{n=-\infty}^{+\infty} |x[n]| |z^{-n}| < \infty$$

which is true only for a region of converge in the complex z-plane.

The inverse z-transform is defined as:

$$x[n] = \frac{1}{2\pi j} \oint X(z) z^{n-1} dz$$

where the contour integral is evaluated on a closed contour, within the region of convergence for  $z$  and enclosing the origin.

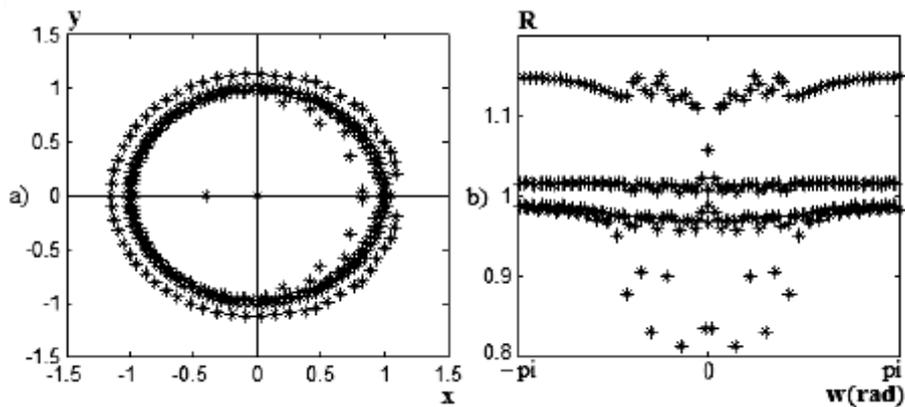
### • ZEROS OF THE Z-TRANSFORM

For a series of  $N$  samples  $(x(0), x(1), \dots, x(N-1))$  taken from a discrete time signal  $x(n)$ , the zeros of z-transform (ZZT) representation is defined as set of roots (zeros),  $(Z_1, Z_2, \dots, Z_{N-1})$  of the corresponding z-transform polynomial  $X(z)$ :

$$X(z) = \sum_{n=0}^{N-1} x(n) z^{-n} = x(0) z^{-N+1} \prod_{m=1}^{N-1} (z - Z_m)$$

considering that  $x(0)$  is non-zero.

Figure A1 shows an example of a ZZT representation of a signal.



**Figure A.1.** ZZT representation of a signal in (a) cartesian coordinates and (b) polar coordinates [BDA<sup>+</sup>05].

Adapted from [Ort05], [HAH01], [Gol00] and [Boz05].

## APPENDIX B – DATA ANALYSIS

**Table B. 1.** Spectral decay of the source harmonics, in dB/octave, Average (AVG) and Standard Deviation (STDev), as a function of vowel per subject.

Subject	Speech file	Vowel	Spectral decay	AVG	STDev
AF	AF_1_a_d	/a/	-10,14	-8,80	1,89
	AF_2_a_d	/a/	-7,46		
	AF_1_i_d	/i/	-16,43	-16,90	0,66
	AF_2_i_d	/i/	-17,36		
RT	RT_1_a_d	/a/	-12,03	-12,27	0,35
	RT_2_a_d	/a/	-12,52		
	RT_1_i_d	/i/	-12,02	-12,99	1,38
	RT_2_i_d	/i/	-13,96		
PP	PP_1_a_d	/a/	-4,99	-7,86	4,05
	PP_2_a_d	/a/	-10,72		
	PP_1_i_d	/i/	-11,41	-11,31	0,14
	PP_2_i_d	/i/	-11,21		
SD	SD_1_a_d	/a/	-5,20	-6,06	1,23
	SD_2_a_d	/a/	-6,93		
	SD_1_i_d	/i/	-15,00	-14,44	0,79
	SD_2_i_d	/i/	-13,88		
SF	SF_1_a_d	/a/	-7,63	-11,94	6,10
	SF_2_a_d	/a/	-16,25		
	SF_1_i_d	/i/	-15,12	-15,44	0,46
	SF_2_i_d	/i/	-15,76		
CK	CK_1_a_d	/a/	-12,55	-11,79	1,08
	CK_2_a_d	/a/	-11,03		
	CK_1_i_d	/i/	-10,82	-11,13	0,43
	CK_2_i_d	/i/	-11,43		

**Table B.2.** Linear Regression Models of the unwrapped NRDs of the time-aligned acoustics signals.

Subject	Speech file	Vowel	Linear Regression Models	
			Signal "Inside"	Signal "Outside"
AF	AF_1_a	/a/	$y = 0,2238x - 0,0534$	$y = 0,1825x + 0,1595$
	AF_2_a	/a/	$y = 0,1883x + 0,4167$	$y = 0,2381x + 0,0689$
	AF_1_i	/i/	$y = 0,0261x - 1,0575$	$y = -0,1118x + 0,3822$
	AF_2_i	/i/	$y = -0,0159x - 0,3962$	$y = 0,0521x - 0,3554$
RT	RT_1_a	/a/	$y = -0,0305x + 1,3573$	$y = 0,0223x + 1,3314$
	RT_2_a	/a/	$y = 0,0600x - 0,7097$	$y = 0,0192x + 0,6805$
	RT_1_i	/i/	$y = -0,0381x - 0,0803$	$y = 0,0078x + 0,8469$
	RT_2_i	/i/	$y = 0,0351x + 0,0207$	$y = 0,0139x + 0,5292$
PP	PP_1_a	/a/	$y = 0,1905x + 0,4204$	$y = 0,2270x + 0,1061$
	PP_2_a	/a/	$y = 0,2316x - 0,07551$	$y = 0,1915x + 0,1032$
	PP_1_i	/i/	$y = 0,1613x + 0,1656$	$y = 0,1290x + 0,6859$
	PP_2_i	/i/	$y = 0,1694x + 0,0585$	$y = 0,1802x - 0,7163$
SD	SD_1_a	/a/	$y = 0,1734x - 0,0358$	$y = 0,1445x + 0,0644$
	SD_2_a	/a/	$y = 0,1935x + 0,0076$	$y = 0,1707x + 0,0782$
	SD_1_i	/i/	$y = 0,1885x - 0,3764$	$y = 0,0545x + 0,1660$
	SD_2_i	/i/	$y = 0,1160x - 1,6171$	$y = 0,0624x - 0,1611$
SF	SF_1_a	/a/	$y = 0,1349x - 0,0432$	$y = 0,0863x + 0,4515$
	SF_2_a	/a/	$y = 0,0730x - 0,2096$	$y = 0,0345x + 0,6166$
	SF_1_i	/i/	$y = 0,0780x + 0,4522$	$y = 0,0196x - 0,1176$
	SF_2_i	/i/	$y = 0,1331x - 0,0207$	$y = 0,0217x - 0,2003$
CK	CK_1_a	/a/	$y = 0,0560x + 1,0618$	$y = -0,0054x + 1,4035$
	CK_2_a	/a/	$y = 0,1558x - 0,0139$	$y = 0,1030x + 0,2788$
	CK_1_i	/i/	$y = 0,0981x - 0,2047$	$y = 0,1638x - 0,2437$
	CK_2_i	/i/	$y = -0,0253x + 0,8328$	$y = 0,0722x + 0,4273$

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